# Constraining the Higgs width at the LHC

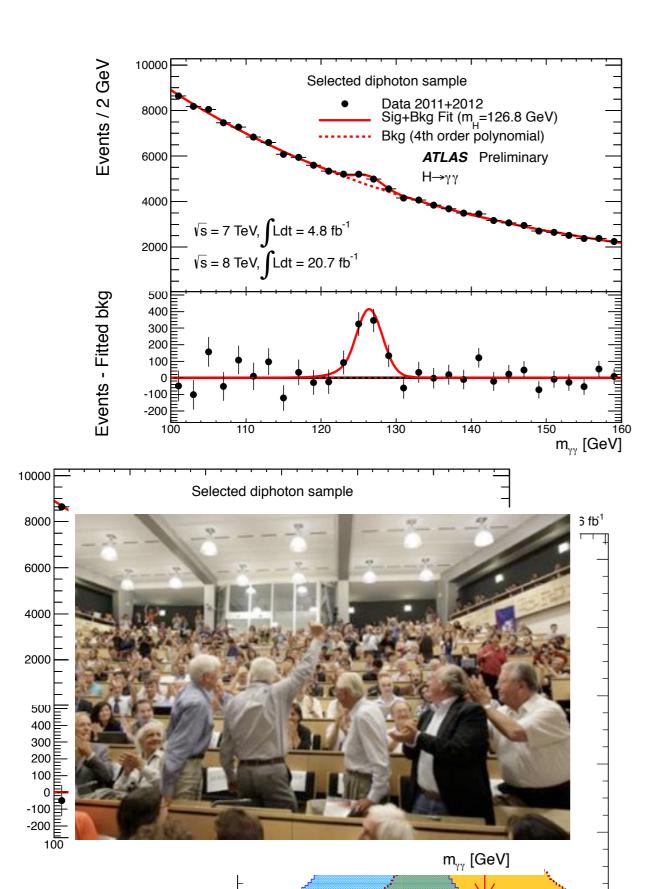
Fabrizio Caola, CERN



Graduiertenkolleg GRK 2044 Mass and Symmetries after the Discovery of the Higgs Particle at the LHC

FREIBURG, DECEMBER 16TH 2015

# The Higgs: a remarkable achievement



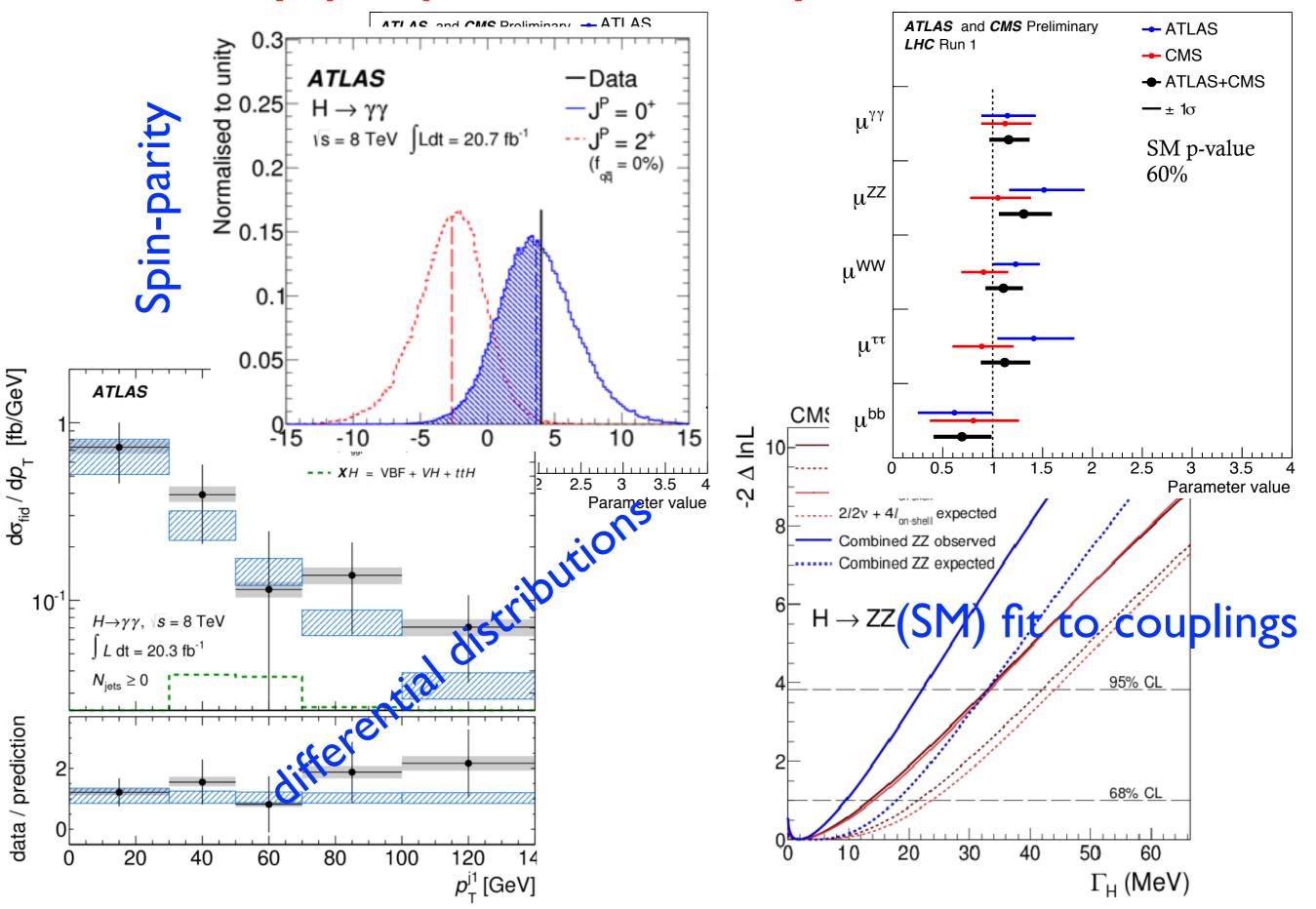
Events / 2 GeV

Events - Fitted bkg

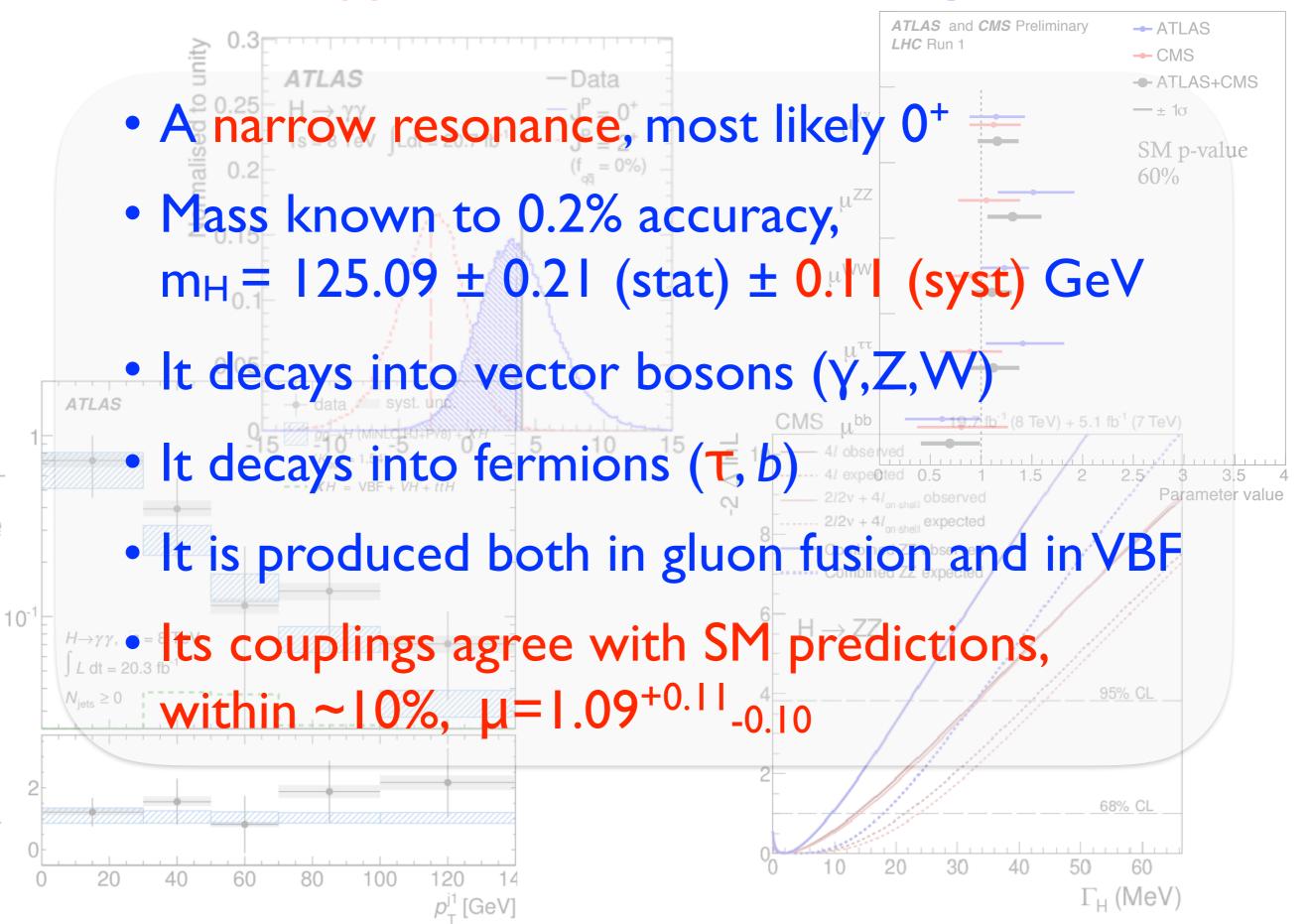
GeV-♦Ĭ♦♦ ٥n 100 100 110 160 180 CMS Preliminary  $\sqrt{s} = 7 \text{ TeV}, L = 5.1 \text{ fb}^{-1}; \sqrt{s} = 8 \text{ TeV}, L = 19.6 \text{ fb}^{-1}$ eV] 35 Events / 3 GeV Data 30 Z+X Zγ<sup>\*</sup>,ZZ 5 GeV 25 m<sub>H</sub>=126 GeV 20 15 10 80 100 120 160 180 140 m<sub>4l</sub> [GeV]

CMS Preliminary  $\sqrt{s} = 7 \text{ TeV}, L = 5.1 \text{ fb}^{-1}; \sqrt{s} = 8 \text{ TeV}, L = 19.6 \text{ fb}^{-1}$ 

# Many properties already constrained



# The Higgs: what to we already know

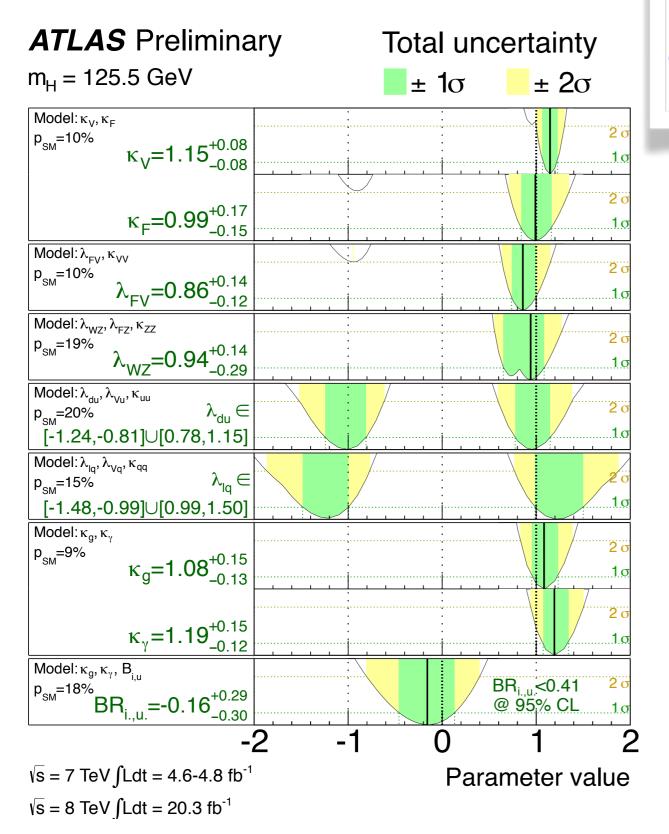


predictior

data /

do<sub>fid</sub> / dp<sub>T</sub> [fb/GeV]

# Higgs couplings: a closer look



$$\sigma_{i \to H \to f} \approx \frac{\sigma_{i \to H} \Gamma_{H \to f}}{\Gamma_{H}} \approx \frac{g_i^2 g_f^2}{\Gamma_{H}}$$

Naively, we only have access to coupling ratios A pragmatic approach:

- I. take cross-section rations to isolate desired production/ decay mode
- 2. fit assuming (rescaled) SM-like behavior

[see e.g. LHC XS WG, arXiv: 1209.0040]

CAN WE OBTAIN EXTRA INFORMATION?

# Higgs couplings: a closer look

$$\sigma_{i \to H \to f} \approx \frac{\sigma_{i \to H} \Gamma_{H \to f}}{\Gamma_{H}} \approx \frac{g_i^2 g_f^2}{\Gamma_{H}}$$

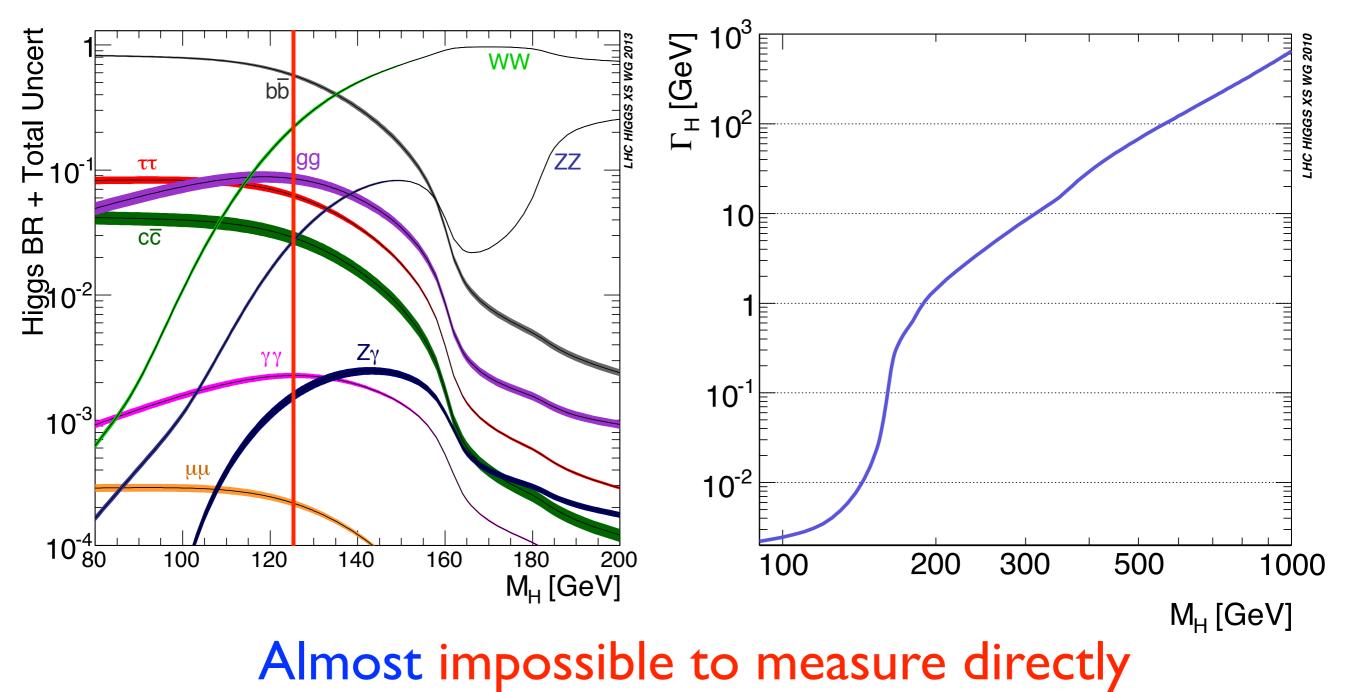
The Higgs cross section x BR is invariant under the rescaling

 $g \to \xi g, \ \Gamma_H \to \xi^4 \Gamma_H \implies \sigma_{i \to H \to f} \to \sigma_{i \to H \to f}$ 

Any measurement on the Higgs peak, only determines a family of  $\infty$  degenerate solutions for g,  $\Gamma_H$ 

To resolve this ambiguity, the width/couplings need to be measured independently from each other

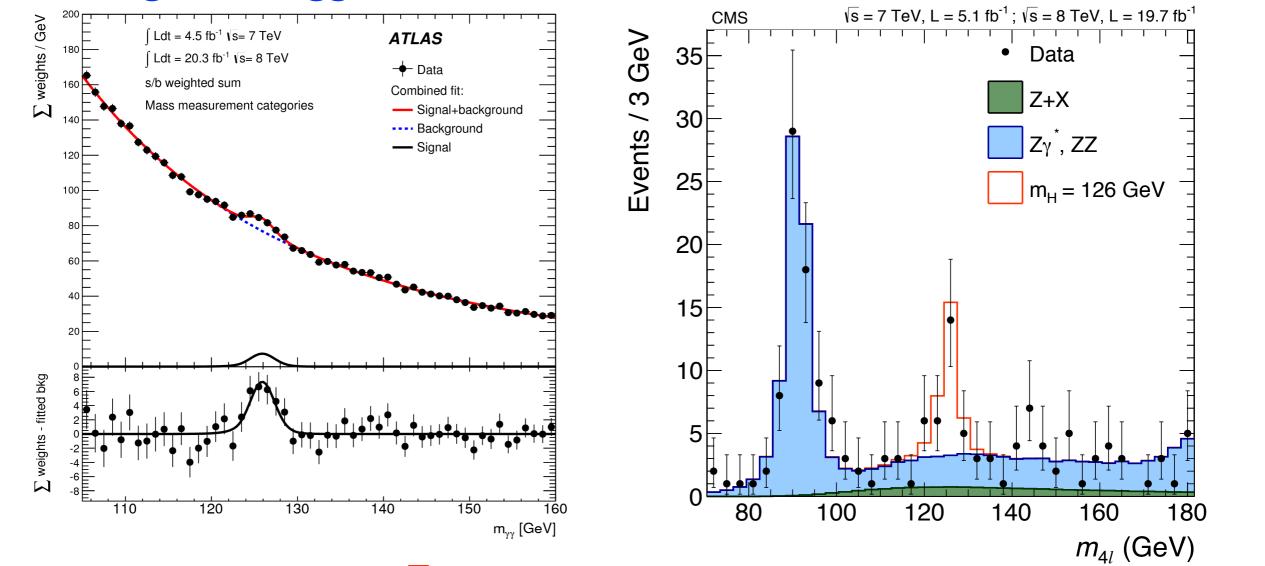
# The SM width: extremely small In the SM for $m_H \sim 125$ GeV, $\Gamma_H \sim 4$ MeV



(with possible exception of muon collider)

# Direct measurement at the LHC

#### Profiling the Higgs resonance limited by detector resolution



Current direct bound:  $\Gamma_{H} \leq \sim 5_{ATLAS,YY} / 2.6_{ATLAS,ZZ} / 1.7_{CMS} \text{ GeV}$ LHC estimated reach: ~ 1 GeV TO BE SENSITIVE TO SM WIDTH (~4 MEV), MUST BE IMPROVED BY FACTOR 1000 The Higgs width: constraints at the LHC We know the Higgs decays  $-> \Gamma_H > 0$ More in general, the Higgs cannot be too narrow ->long-lived particle -> displaced vertex

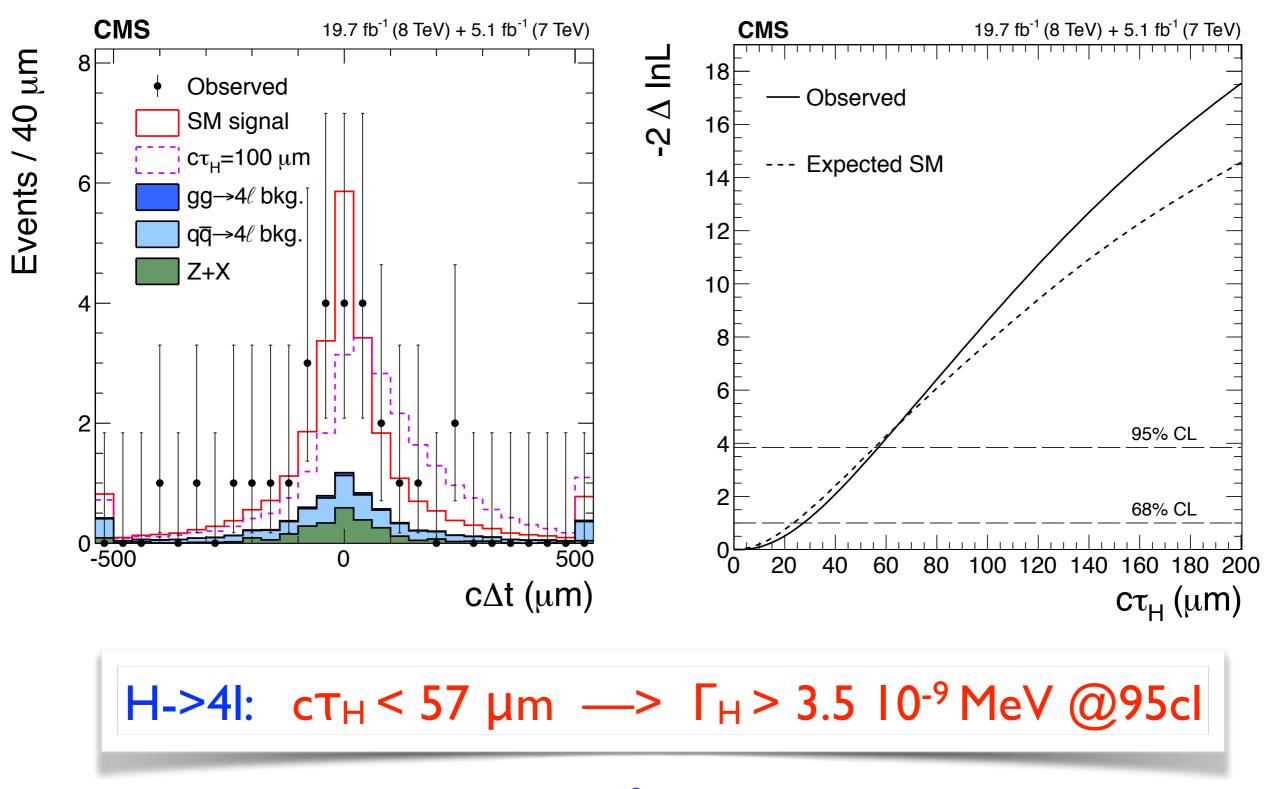
> Lower bound can be obtained by LIFETIME MEASUREMENTS

> > In the Higgs rest frame:

$$\Delta t = \frac{m}{p_{\perp}} \left( \Delta \vec{r}_{\perp} \cdot \hat{p}_{\perp} \right) \qquad \langle \Delta t \rangle = \tau_H = \frac{1}{\Gamma_H}$$

In the SM:  $\tau_H \sim 4.8 \ 10^{-8} \,\mu$ m/c, well below exp. sensitivity

# CMS: bounds on the Higgs lifetime



(SM:  $cT_H \sim 4.8 \ 10^{-8} \mu m$ ,  $\Gamma_H \sim 4.2 \ MeV$ )

# Higgs couplings and width: a closer look

$$\sigma_{i \to H \to f} \approx \frac{\sigma_{i \to H} \Gamma_{H \to f}}{\Gamma_{H}} \approx \frac{g_i^2 g_f^2}{\Gamma_{H}}$$

 $\sigma$  is invariant under  $g \to \xi g, \ \Gamma_H \to \xi^4 \Gamma_H$ 

To avoid imposing SM-like behavior: we must break this degeneracy

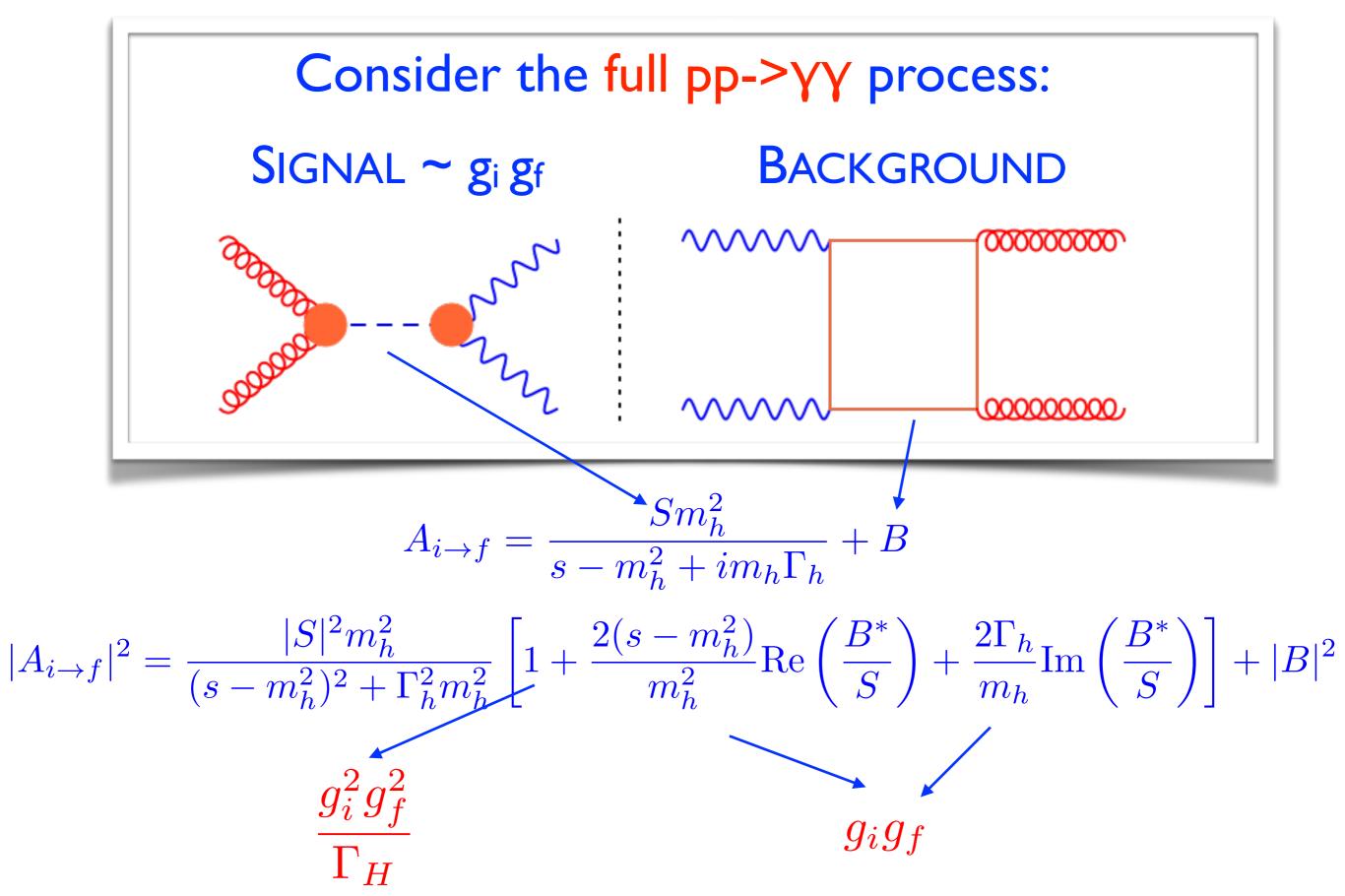
A direct measurement of the Higgs width: • LHC sensitivity: ~  $10^{-9}$  MeV <  $\Gamma_H$  < 1 GeV • SM width: ~ 4 MeV

We need an indirect way of measuring  $\Gamma_H$ Key point: search for an observable with different dependence on  $g_{i,f}$  and  $\Gamma_H$ 

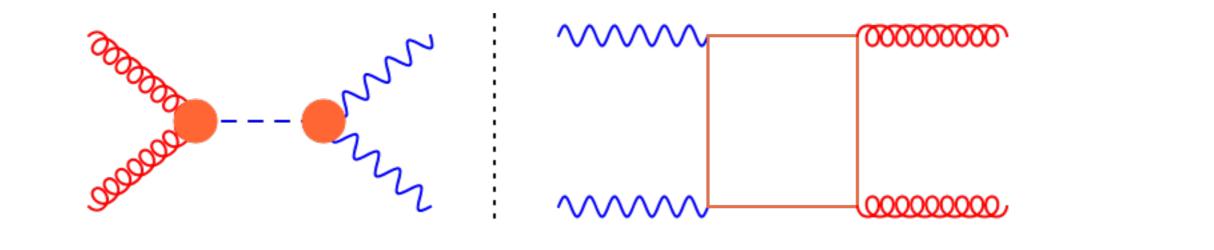
# An example: H-> YY interference

[Martin; Dixon, Li (2013)]

# Typical interference scaling: g vs g<sup>2</sup>



#### Interference: the imaginary part



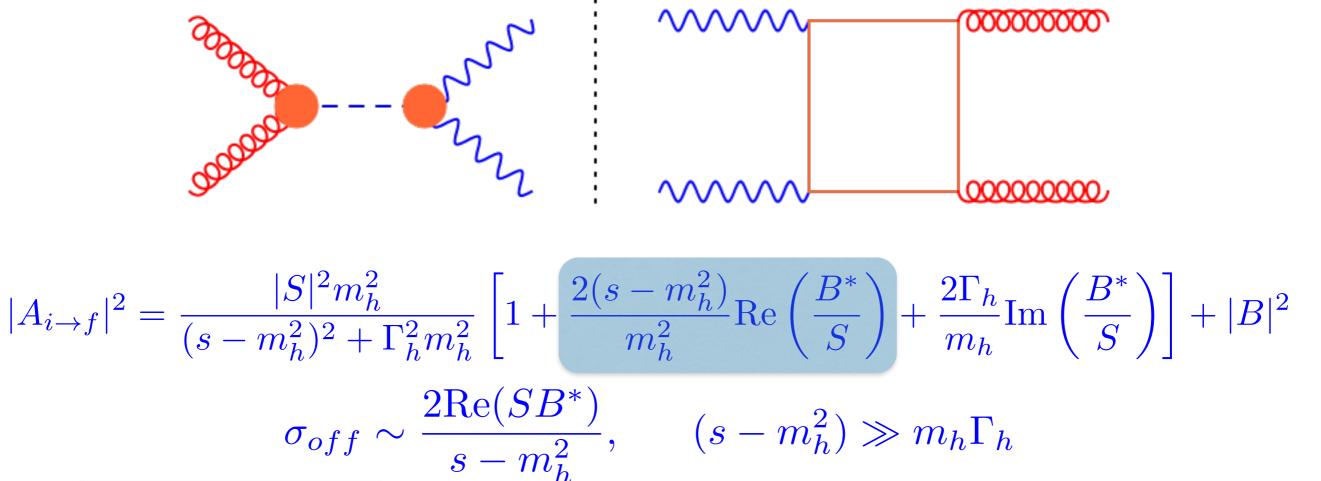
$$|A_{i\to f}|^2 = \frac{|S|^2 m_h^2}{(s-m_h^2)^2 + \Gamma_h^2 m_h^2} \left[ 1 + \frac{2(s-m_h^2)}{m_h^2} \operatorname{Re}\left(\frac{B^*}{S}\right) + \frac{2\Gamma_h}{m_h} \operatorname{Im}\left(\frac{B^*}{S}\right) \right] + |B|^2$$

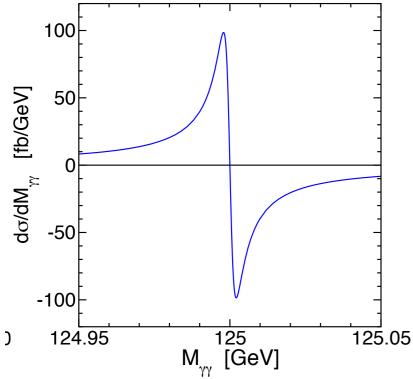
symmetric around the peak -> contribute to σ
Naively: loop enhanced (S -> 2 loop, B-> 1 loop)

$$S \sim \frac{g_s^2 e^2}{(16\pi^2)^2} \frac{m_h^2}{v^2} \quad B \sim \frac{g_s^2 e^2}{(16\pi^2)} \quad \left[\sigma_{\rm int} / \sigma_H\right]_{\rm naive} \approx c \frac{2\Gamma_h}{m_h} \frac{(4\pi v)^2}{m_h^2} \approx 0.1$$

- In reality: interference starts at two-loop (no ±± cut for the background amplitude)
- Small effect (~ few percent) in the SM

#### Interference: the real part





Asymmetry in the  $m_{\gamma\gamma}$  distribution

- more events below the peak
- asymmetric -> irrelevant for  $\sigma$

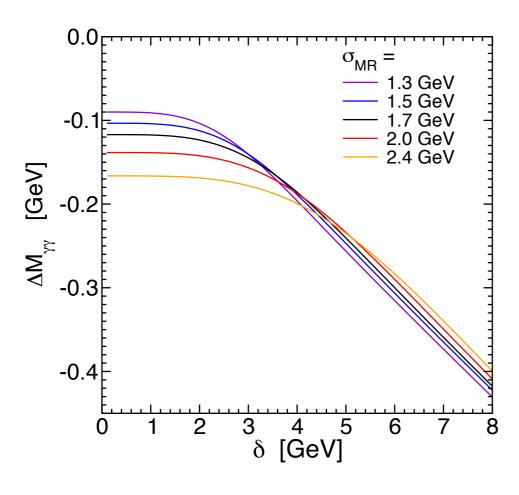
however, interesting physical effects

[Martin (2012)]

Interference: the real part and the mass-shift [Martin (2012); Dixon and Li; de Florian et al (2013)]

#### Higgs mass:

- ~ first moment of the invariant mass distribution
- extraction affected by real part of interference
- independent on  $\Gamma$ , dependent on environmental parameters (energy resolution)  $d\sigma$  A  $(s-m_h^2)I$



$$\frac{d\sigma}{ds} = \frac{A}{(s-m_h^2)^2 + m_h^2 \Gamma_h^2} + \frac{(s-m_h^2)I}{(s-m_h^2)^2 + m_h^2 \Gamma_h^2}$$
$$\left\langle M^2 \right\rangle = \frac{1}{\sigma_0} \int ds \ s \frac{d\sigma}{ds} = m_h^2 + \frac{I}{\sigma_0} \int_{s_-}^{s^+} ds$$
$$\delta m_h = \frac{2I\delta}{\sigma_0}, \quad s_{\pm} = (m_h \pm \delta)^2$$

Simple analysis: shift ~ 80-100 MeV Shift proportional to I ~ g<sub>i</sub> g<sub>f</sub>

#### From the mass shift to the Higgs width [Martin (2012); Dixon and Li; de Florian et al (2013)]

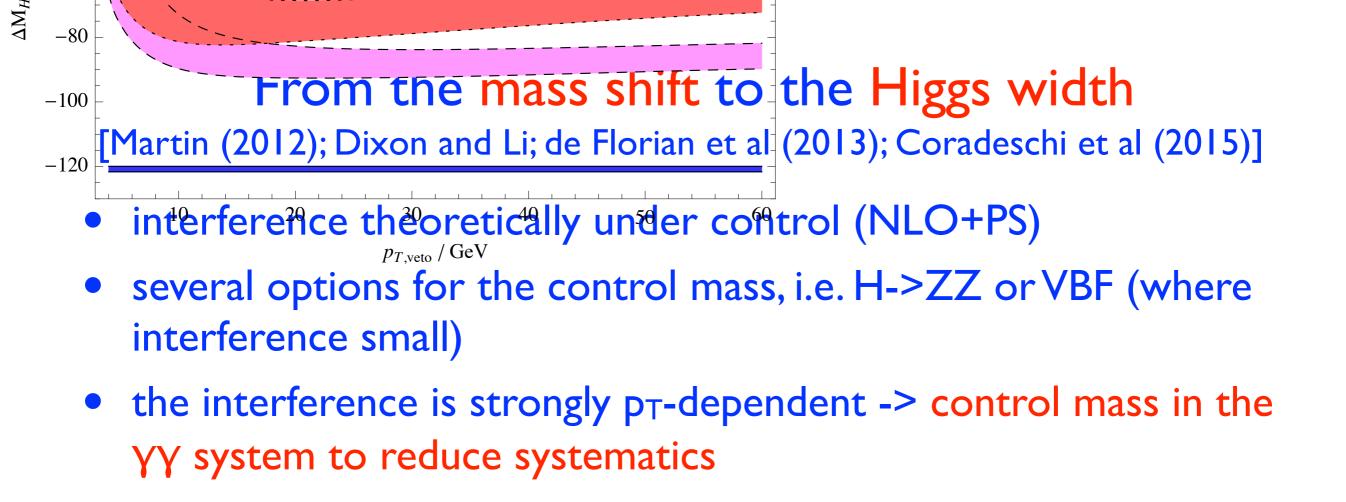
- compare mass measurement in  $H \rightarrow \gamma \gamma$  with control mass
- mass shift gives access to the real part of the interference,  $\delta m_h = 2I\delta/\sigma_h \sim g_i g_f$
- LHC: Higgs peak cross section is SM-like

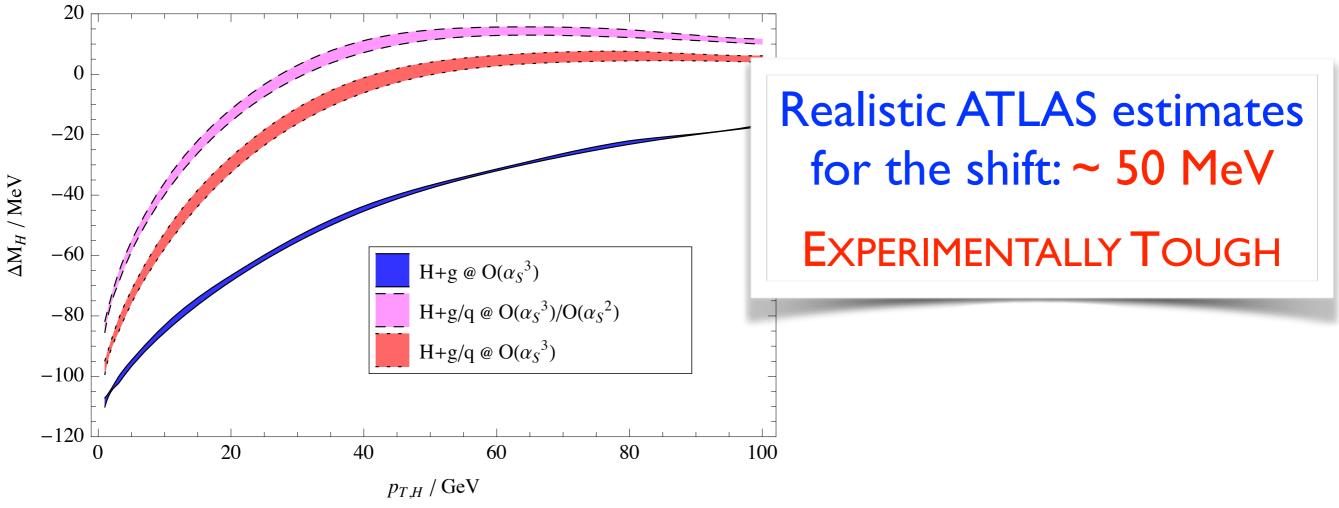
$$\sigma_{H} \sim \frac{g_{i}^{2}g_{f}^{2}}{\Gamma_{H}} = \sigma_{H,\text{SM}} \rightarrow \frac{g_{i}g_{f}}{(g_{i}g_{f})_{\text{SM}}} = \sqrt{\frac{\Gamma_{H}}{\Gamma_{H,\text{SM}}}}$$

• This implies

$$\delta m_H = (\delta m_H)_{\rm SM} \times \sqrt{\frac{\Gamma_H}{\Gamma_{H,SM}}} \approx -100 {
m MeV} \times \sqrt{\frac{\Gamma_H}{\Gamma_{H,SM}}}$$

Mass shift measurement gives access to the Higgs width

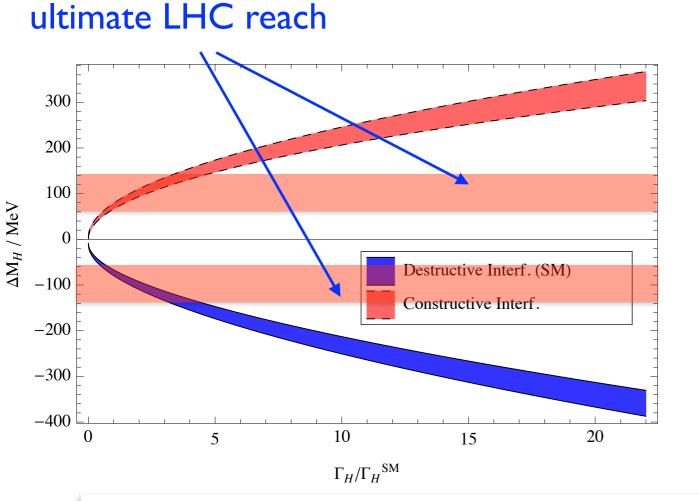


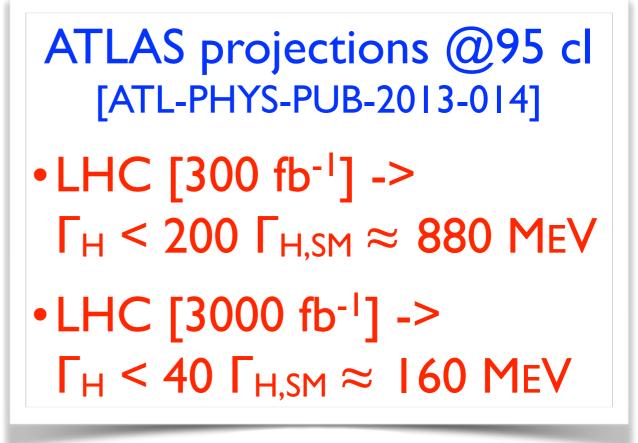


#### $\Delta M_{\gamma\gamma}$ : indirect determination of $\Gamma_H$ [Dixon and Li (2013)]

$$\delta m_H \approx -[50:80] \text{ MeV} \times \sqrt{\Gamma_H / \Gamma_{H,SM}}$$

#### The mass-sensitivity right now: $m_H = 125.09 \pm 0.21$ (stat) $\pm 0.11$ (syst) GeV





MUCH BETTER THAN ULTIMATE DIRECT LIMIT ~  $\Gamma_{H}$  < 1 GeV

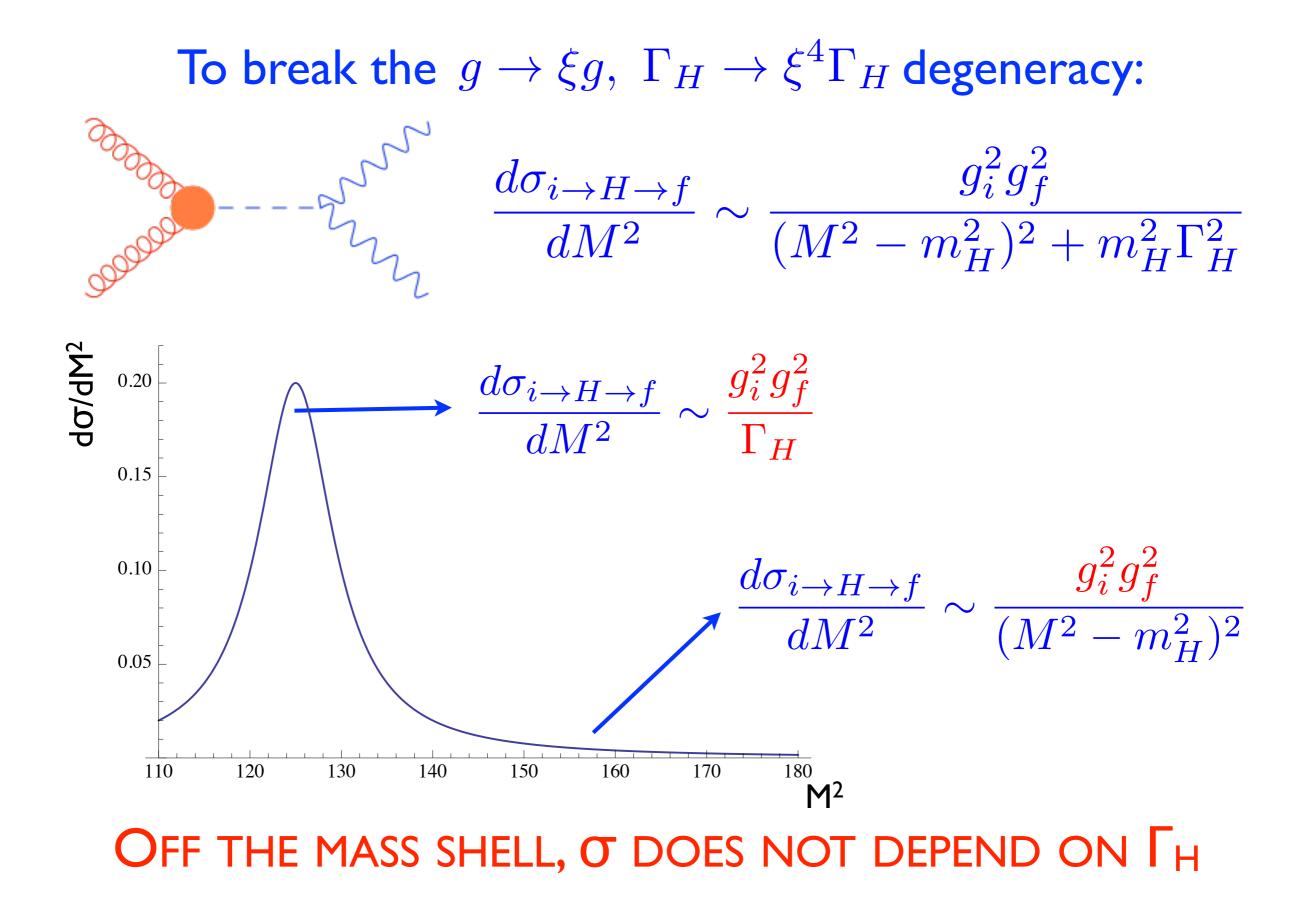
#### From the mass shift to the Higgs width: recap

- in the di-photon channel, observable effect of the signal/ background interference -> mass shift
- the mass shift ~ g<sub>i</sub> g<sub>f</sub> does not depend on the width -> break the width/coupling degeneracy.
- combining the peak measurement,  $\sigma \sim g_i^2 g_f^2 / \Gamma_H \approx g_{i,SM}^2 g_{f,SN}^2 / \Gamma_{H,SM}$ ->  $\delta m \sim g_i g_f \approx g_{i,SM} g_{f,SM} \sqrt{\Gamma_H / \Gamma_{H,SM}}$  -> ACCESS TO THE WIDTH [UNFORTUNATELY: MILD ~ SQUARE-ROOT DEPENDENCE]
- theoretically very clean. Signal / background well-known
- experimentally challenging. Systematic-dominated
- current projections for the HL-LHC:  $\Gamma_H < 40 \ \Gamma_{H,SM} \approx 160 \ MeV$
- ~ I order of magnitude better than direct limit
- new ideas for analysis, theory may lead to better constraints

Another example: bounds from off-shell measurements

[FC, Melnikov (2013)]

# Another option: use the cross-section itself



Using the off-shell cross-section to bound  $\Gamma_{\rm H}$ 

# LHC results: on the Higgs peak, the number of events is compatible with the SM expectation

$$\frac{g_i^2 g_f^2}{\Gamma_H} = \frac{g_{i,\text{SM}}^2 g_{f,\text{SM}}^2}{\Gamma_{H,\text{SM}}} \longrightarrow g = \xi g_{\text{SM}}, \ \Gamma_H = \xi^4 \Gamma_{H,\text{SM}}$$

$$\text{Look for off-peak events:} \ \sigma_{off} \sim g_i^2 g_f^2$$

$$N_{obs}^{off} \propto g_i^2 g_f^2 = \xi^4 g_{i,\text{SM}}^2 g_{f,\text{SM}}^2 \propto \xi^4 N_{\text{SM}}^{off} = \frac{\Gamma_H}{\Gamma_{H,\text{SM}}} N_{\text{SM}}^{off}$$

**ASSUMPTION:** 

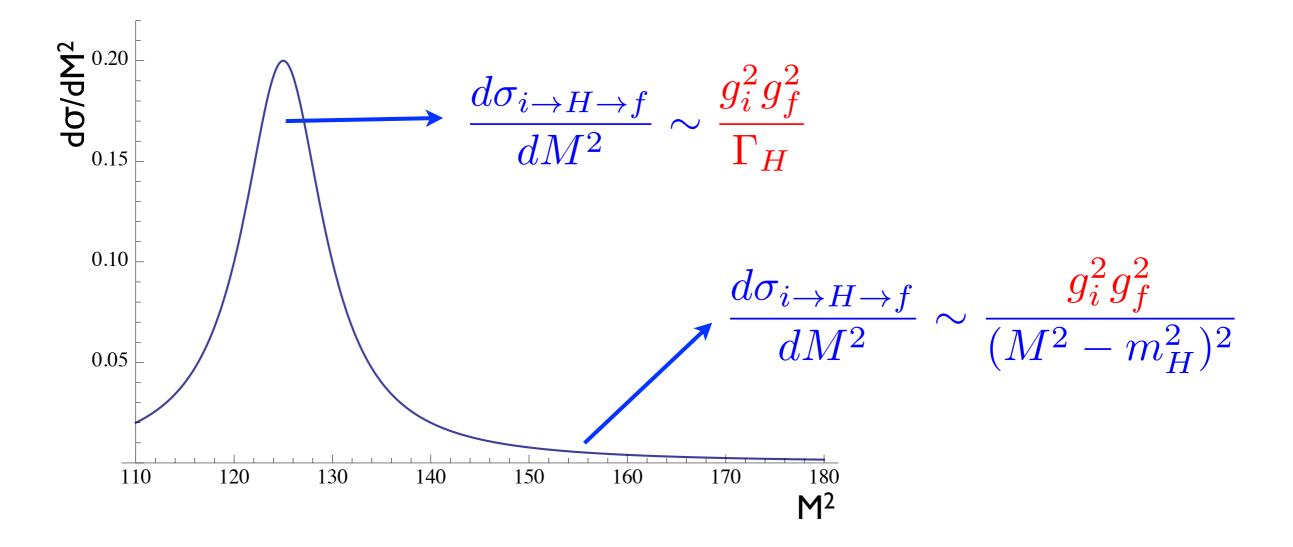
 $[g_i^2 g_f^2]_{[off]} =$ 

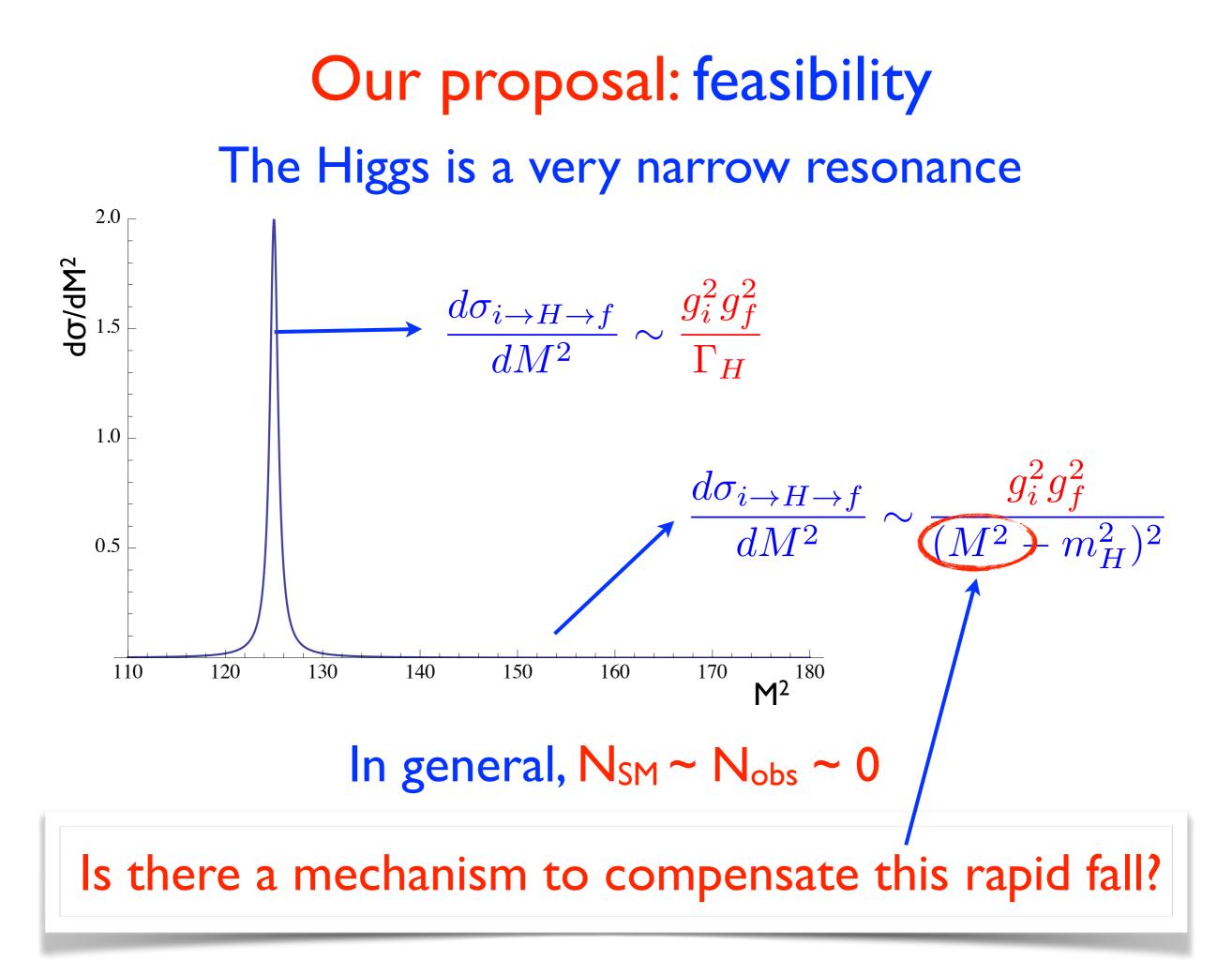
[gi<sup>2</sup>gf<sup>2</sup>][125 GeV]

DIRECT ACCESS TO THE WIDTH  

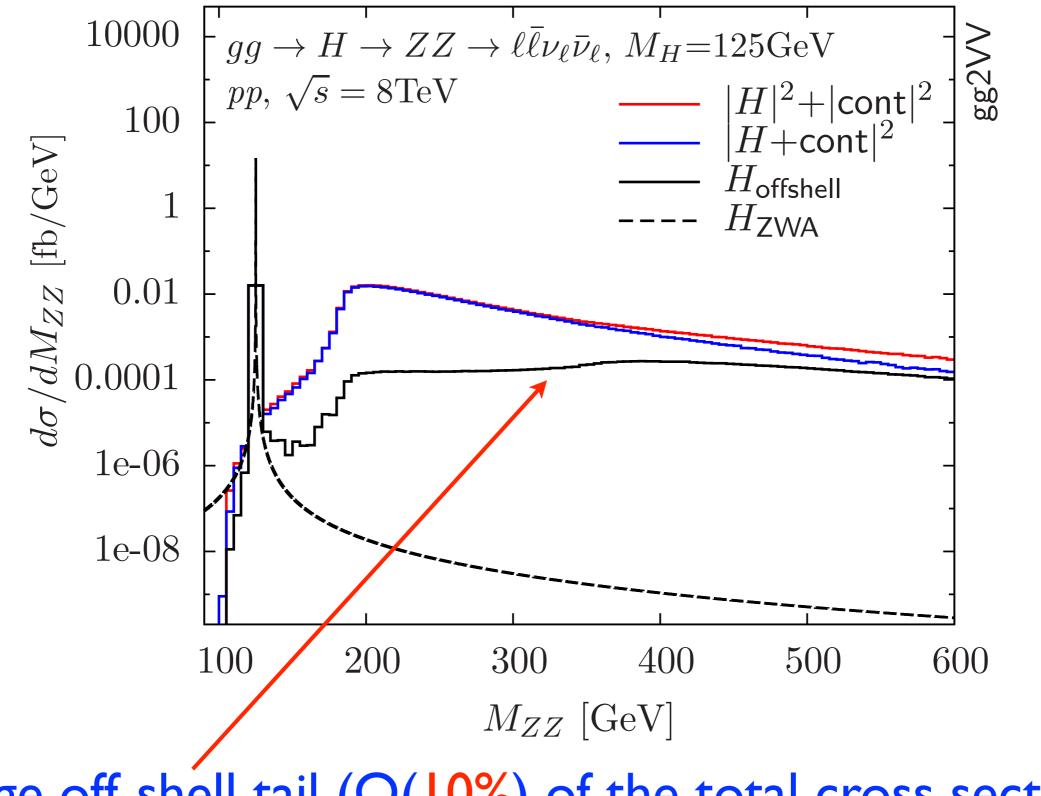
$$\Gamma_{H} = \frac{N_{obs}^{off}}{N_{SM}^{off}} \Gamma_{H,SM}$$
LINEAR DEPENDENCE

Off-shell measurement: feasibility The Higgs is a very narrow resonance





# Yes: look at VV decay modes [Kauer, Passarino (2012)]



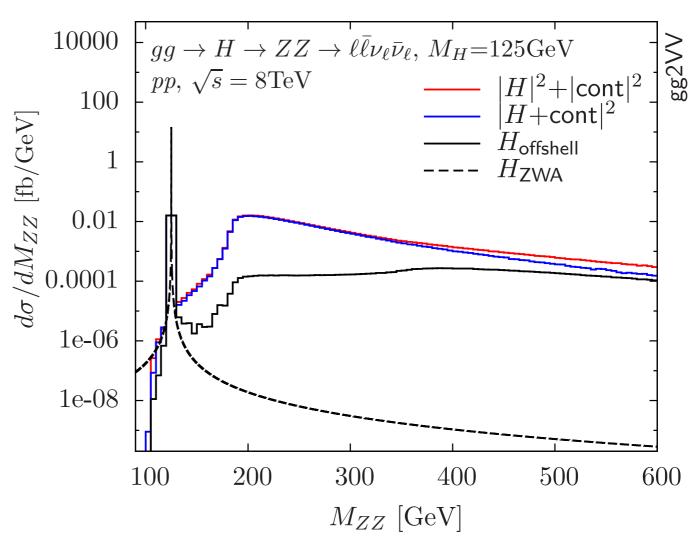
Large off-shell tail (O(10%)) of the total cross section)

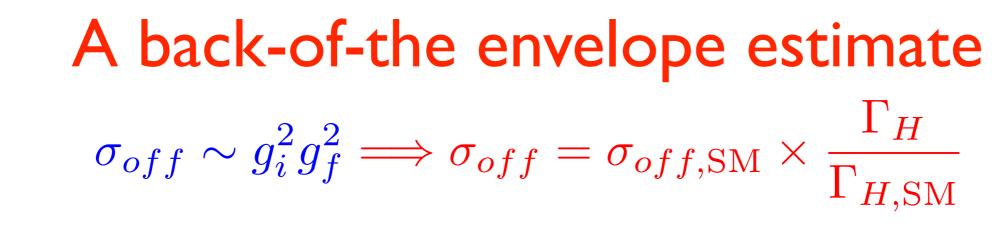
# Yes: look at VV decay modes [Kauer, Passarino (2012)]

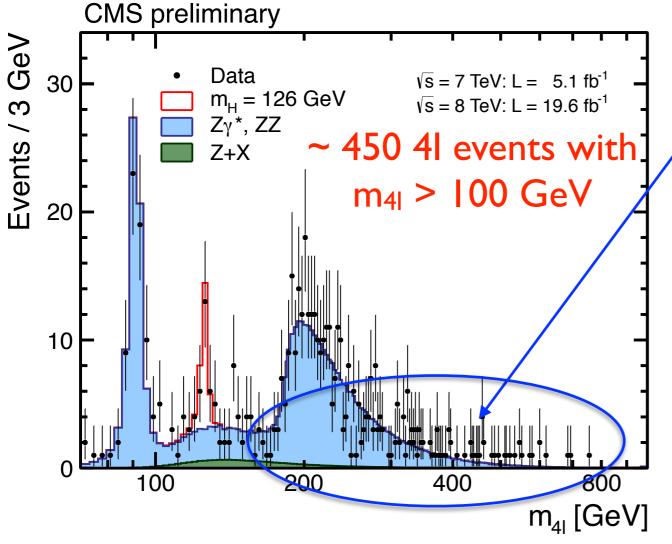
 $\mathcal{N}^{\mathcal{W}_L, Z_L}$  $\sim M_{VV}^3$  $\mathcal{V}_{W_L, Z_L}$ 

Above the VV threshold: enhanced decay into longitudinal gauge bosons

Large plateau, eventually washed away by parton luminosities





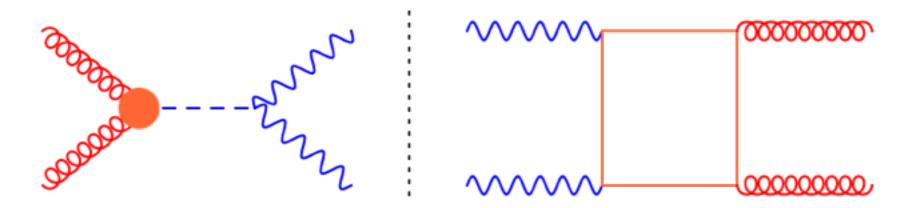


- Look at the high-tail of the M<sub>ZZ</sub> distribution
- A SM-like peak cross-section + deviation in  $\Gamma_H$  lead to excess/ deficit of ZZ events
- If  $\Gamma_H = 1.7$  GeV (direct bound), then  $\Gamma_H/\Gamma_{H,SM} \sim 400$  and

 $\begin{aligned} N_{\text{off}} &\approx \left[ 0.1 \times N_{\text{peak}} \right] \times 400 \\ &\approx 800 \gg N_{\text{4l,total}} \end{aligned}$ 

The off-shell cross-section is very sensitive to  $\Gamma_{\rm H}$ 

# A more careful analysis: large interference



In the SM: large destructive interference at high invariant mass  $\sigma^{int} \sim -50\%$  off peak (unitarity) [on-peak: negligible] [Kauer, Passarino (2012), Ellis, Campbell, Williams (2013)]

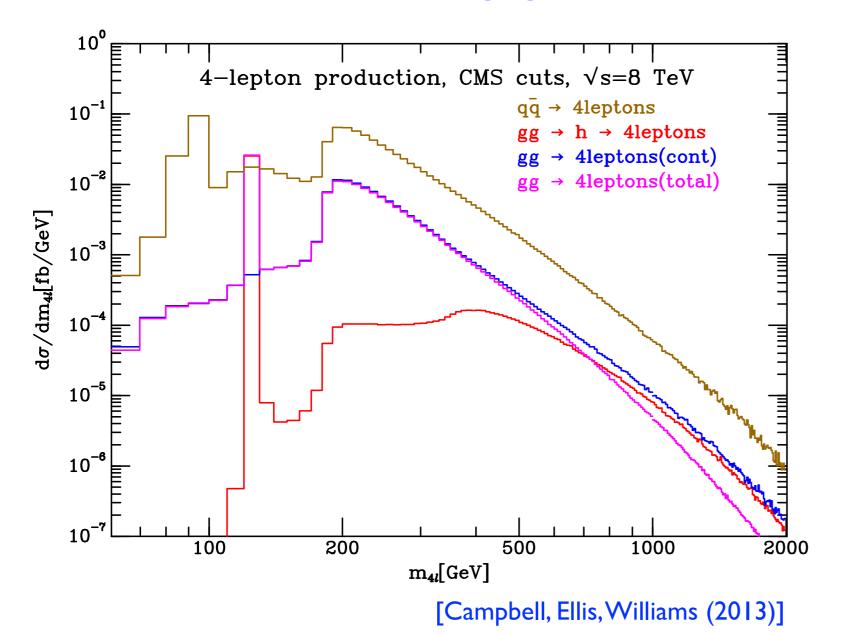
$$\sigma^{int} \sim g_{Hgg} g_{HVV} = [e^{i\theta}] \sqrt{\frac{\Gamma_H}{\Gamma_{H,SM}}} \sigma_{SM}^{int}$$

PUTTING EVERYTHING TOGETHER:  $N^{off} = \frac{\Gamma_H}{\Gamma_{H,SM}} N^{off}_{SM} - [e^{i\theta}] \sqrt{\frac{\Gamma_H}{\Gamma_{H,SM}}} N^{int}_{SM}$ 

Negative interference -> less off-shell events -> decrease sensitivity

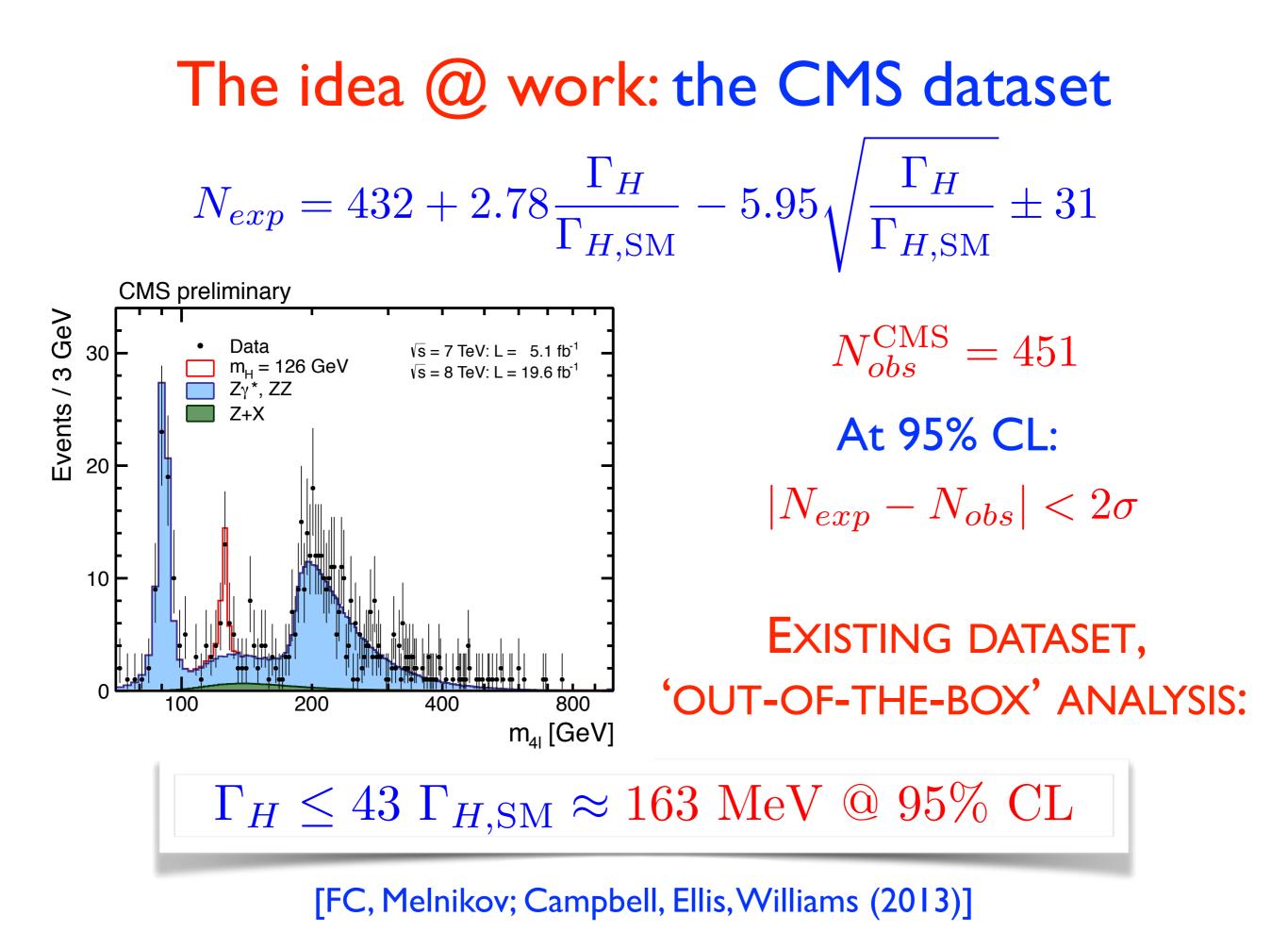
# The 4I spectrum at high invariant mass

- In Run I, CMS observed 451  $m_{41}$  > 100 GeV events
- SM prediction: 429 ± 31 events
- Dominated by pp->ZZ background (mostly qq)
- Off-shell tail negligible if not looked for

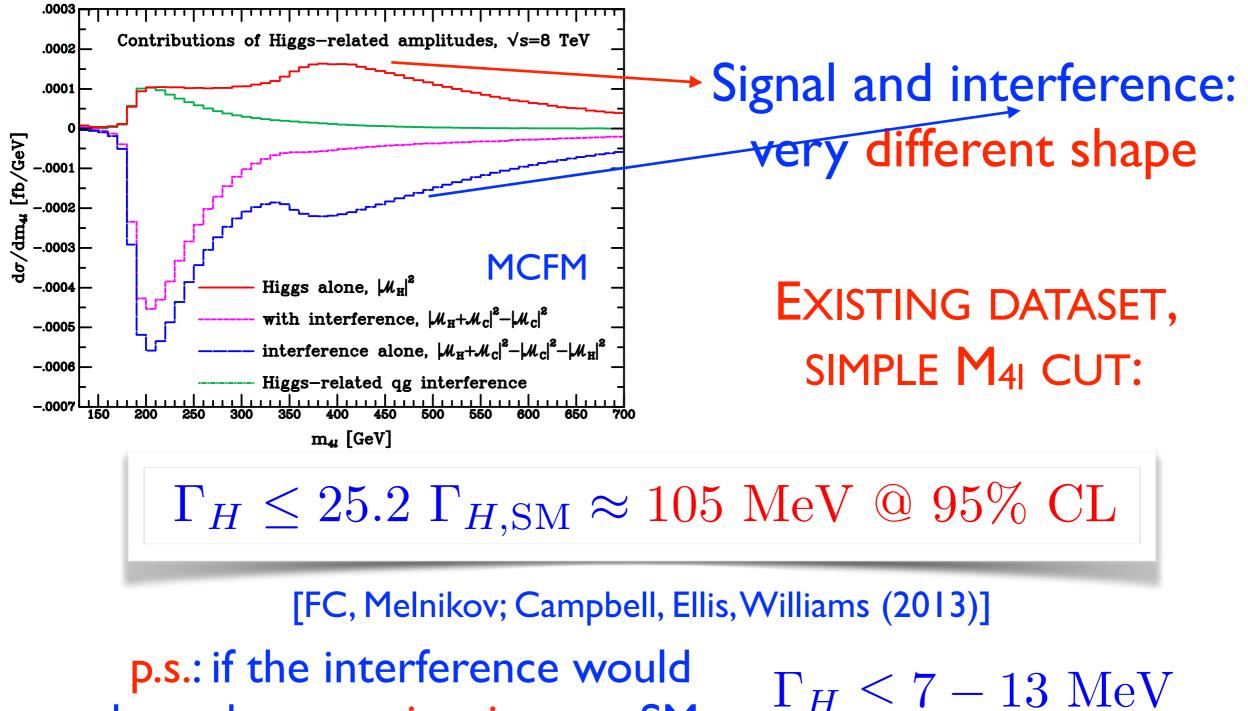


 $N_{qq \rightarrow ZZ} \approx N_{tot}$   $N_{gg} \sim 10^{-1} \times N_{tot}$   $N_H \sim 5 \times 10^{-2} \times N_{tot}$   $N_{off} \sim 10^{-2} N_{tot}$  $N_{int} \sim -2 \times 10^{-2} N_{tot}$ 

How does the picture change if  $\Gamma_{\rm H} \neq \Gamma_{\rm H,SM}$ ?



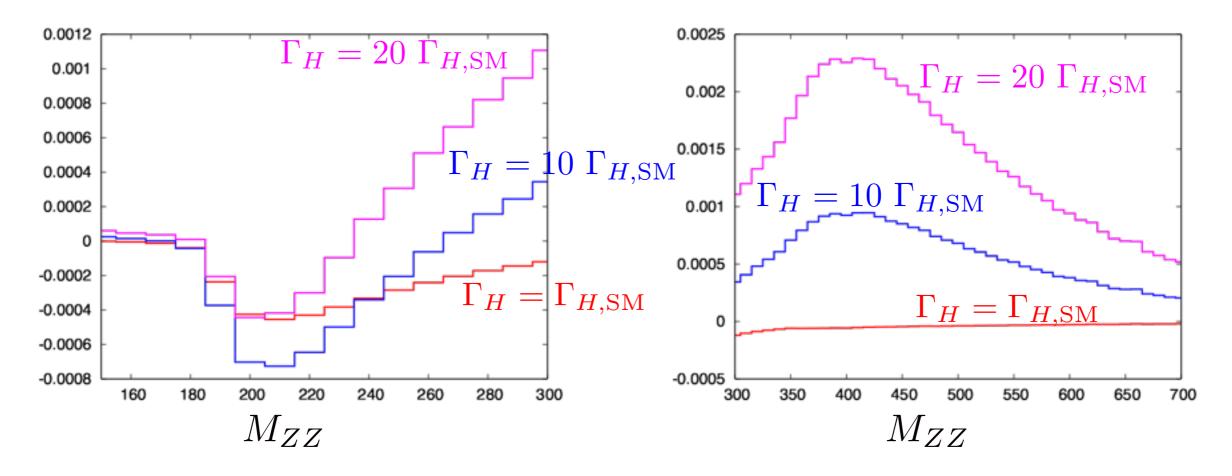
# The idea @ work: look at CMS data Simple improvement: reduce the interference



have the opposite sign wrt SM:

# Other possible improvements

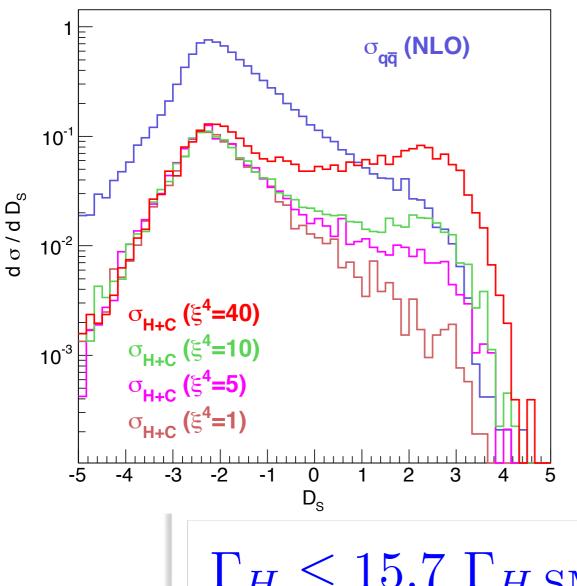
Profit even more from different shape of signal and interference, and shape dependence on  $\Gamma_H$ 



To reduce qq contamination: select longitudinal polarizations -> study angular correlations of the leptons.

# Other possible improvements

Apply a kinematic discriminant (ME method) [Campbell, Ellis, Williams (2013)]



$$D_{S} = \log \left[ \frac{P_{gg \to H \to ZZ}}{P_{gg \to ZZ} + P_{q\bar{q} \to ZZ}} \right]$$
$$P_{i} \sim |M_{i}|^{2}$$

'Interesting' events: large Ds

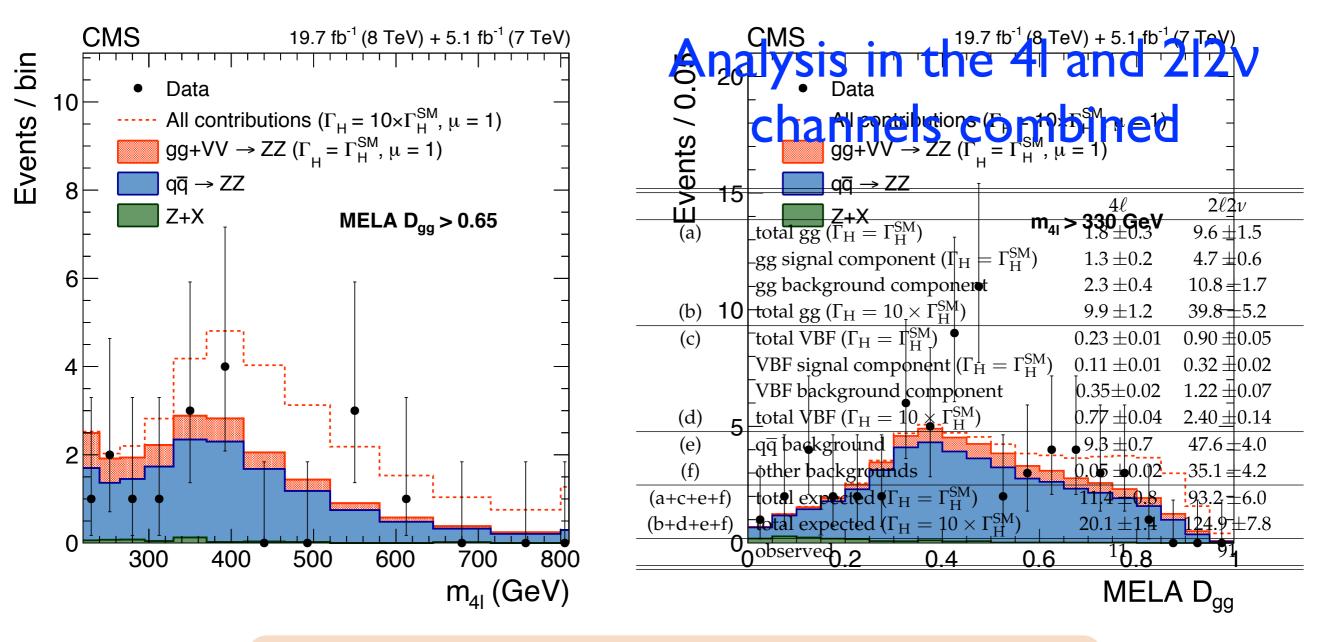
JUST BY CUTTING D<sub>S</sub> > 1:

 $\Gamma_H \leq 15.7 \ \Gamma_{H,SM} \approx 66 \ MeV @ 95\% \ CL$ 

**Recall direct bound ~ I GeV** 

# **Experimental results: CMS**

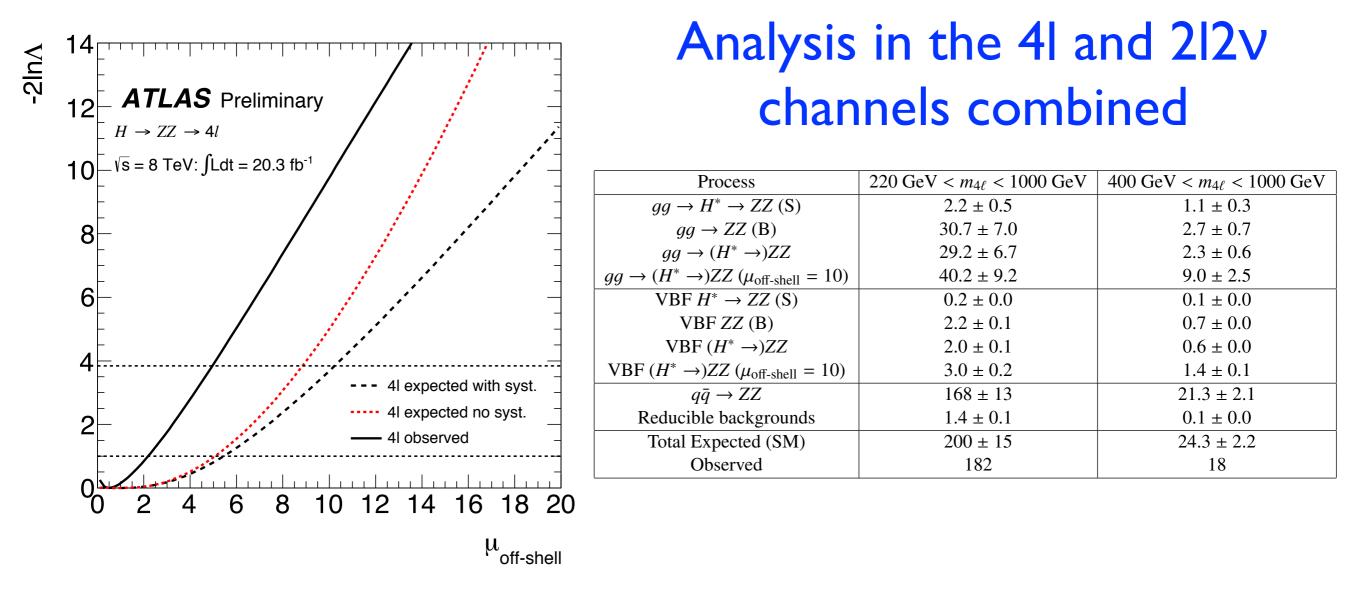
[PLB 736 (2014) 64]



Г<sub>Н</sub> < 5.4 Г<sub>Н,SM</sub> = 22 MeV @ 95CL

(Even better than anticipated)

### Experimental results: ATLAS [EP] (2015) 75:335]



# Г<sub>Н</sub> < 4.8-7.7 Г<sub>Н,SM</sub> = 20-32 MeV @ 95CL

(depending on the gg->ZZ background K-factor)

### Γ<sub>H</sub> from the off-shell tail: issues

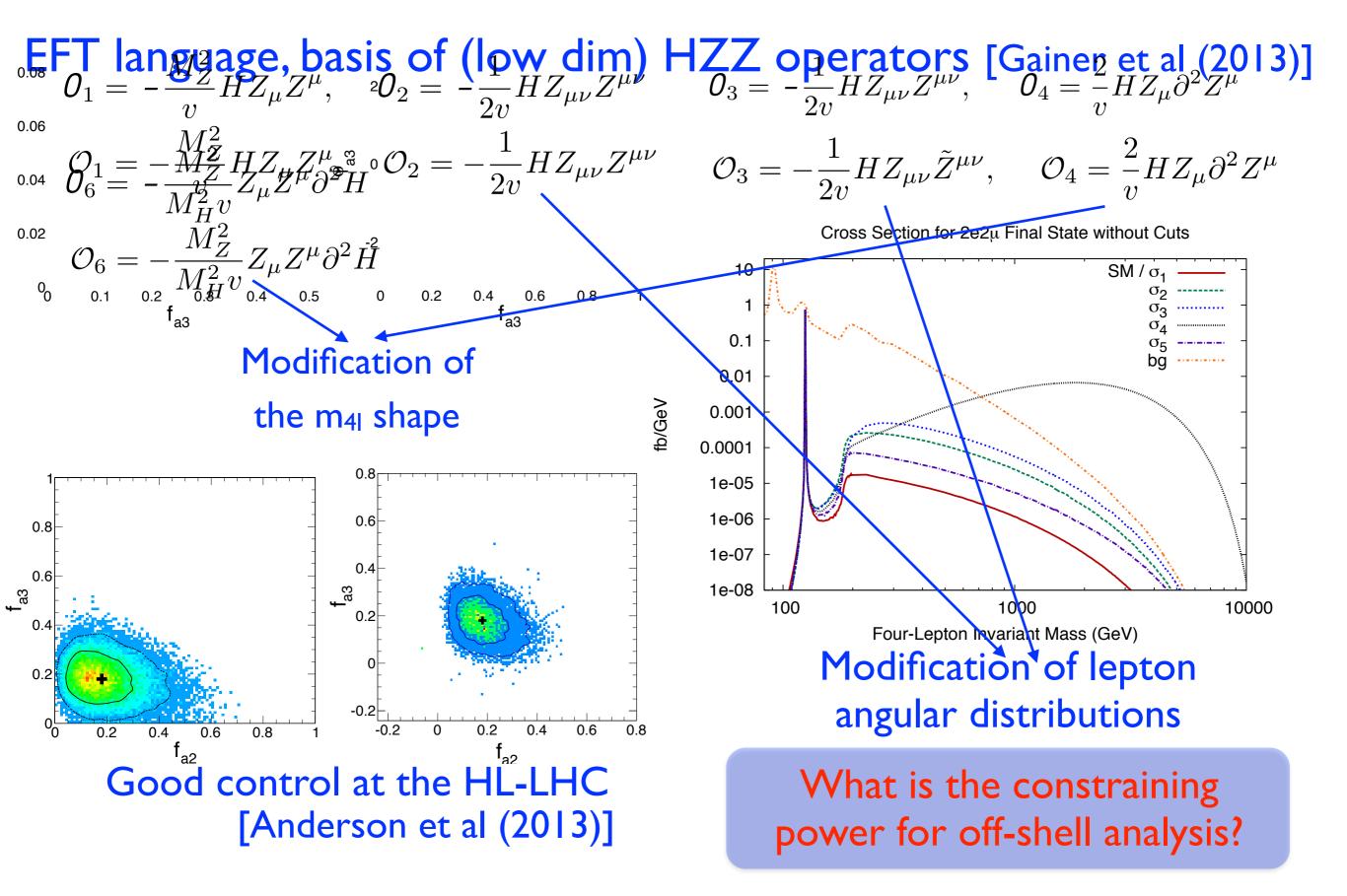
- the technique is very promising, bounds 2 order of magnitude better than direct measurements accessible.
   Eventually, values as low as the SM width within reach.
- However, there are TWO BIG ISSUES to be addressed
  - the method assumes [g<sub>i</sub><sup>2</sup>g<sub>f</sub><sup>2</sup>]<sub>[off]</sub> ≈ [g<sub>i</sub><sup>2</sup>g<sub>f</sub><sup>2</sup>]<sub>[peak]</sub>. This is true in the SM, but it may be violated by BSM physics. If a violations do indeed occur, off-shell measurement still very solid but interpretation in terms of Γ<sub>H</sub> problematic
  - even with all MEM improvements, the method boils down to count events in the high-mass tail and compare with SM predictions -> very good theoretical control on pp->4l processes is needed

#### Interpretation issues

- Large de-correlation of on-shell and off-shell couplings make the width interpretation problematic
- In the SM: logarithmic running, negligible effect (taken into account in all the analysis)
- De-correlation however possible if strong (energydependent) modifications of the Hgg / HVV couplings.
  - large anomalous HZZ couplings
  - light colored d.o.f. in the Hgg vertex [Englert, Spannowksy (2014)]
  - extra Higgses to restore unitarity [Logan (2014)]

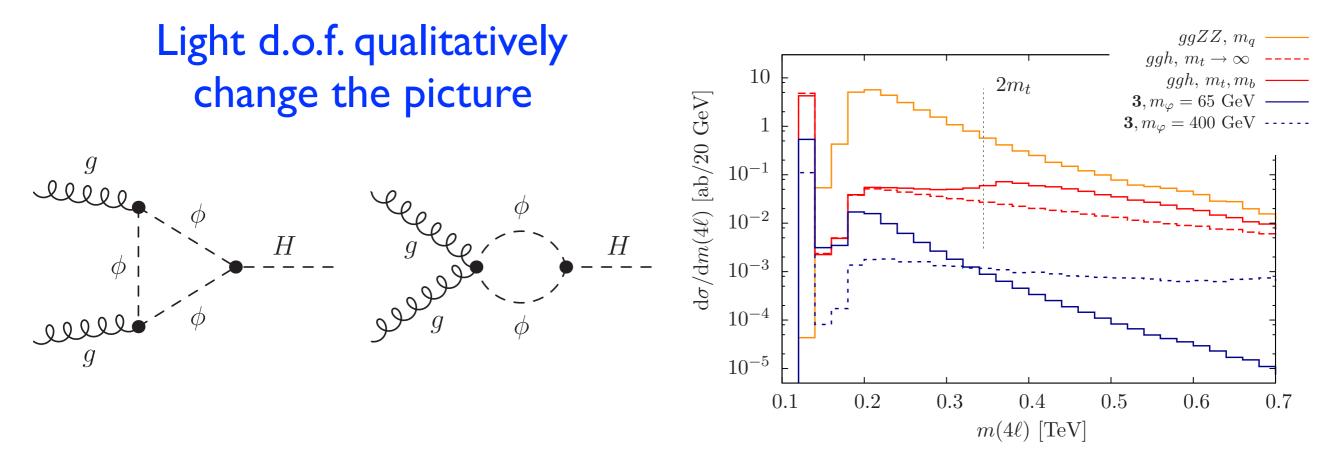
To which extent these effects can be classified and constrained by other measurements is a then an interesting BSM phenomenology open problem

### Example: anomalous HZZ couplings



# Example: light d.o.f. in the Hgg coupling

[Englert, Spannowski (2014)]

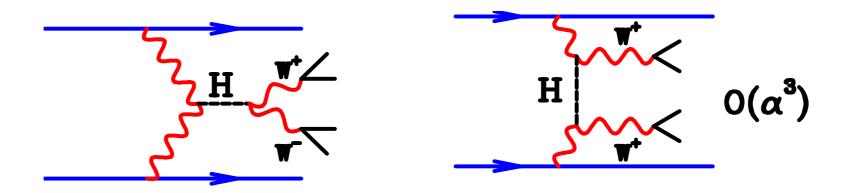


Complementary constraints from other measurements?

- Will also affect other observables e.g. Higgs pT ([Arnesen et al (2008)])
- Information from boosted Higgs regime? ([Buschmann et al (2014)])
- finite mt effects crucial -> need theoretical improvement
- Can (very large) S/B interference in the γγ channel give constraints? (along the lines of [Dixon, Siu (2003)])

#### A complementary approach:VBF [Campbell, Ellis (2014)]

- Different theory systematics w.r.t. gluon fusion
- At least in the SM, good theoretical control
- The most promising channel: W<sup>+</sup>W<sup>+</sup> (small background)

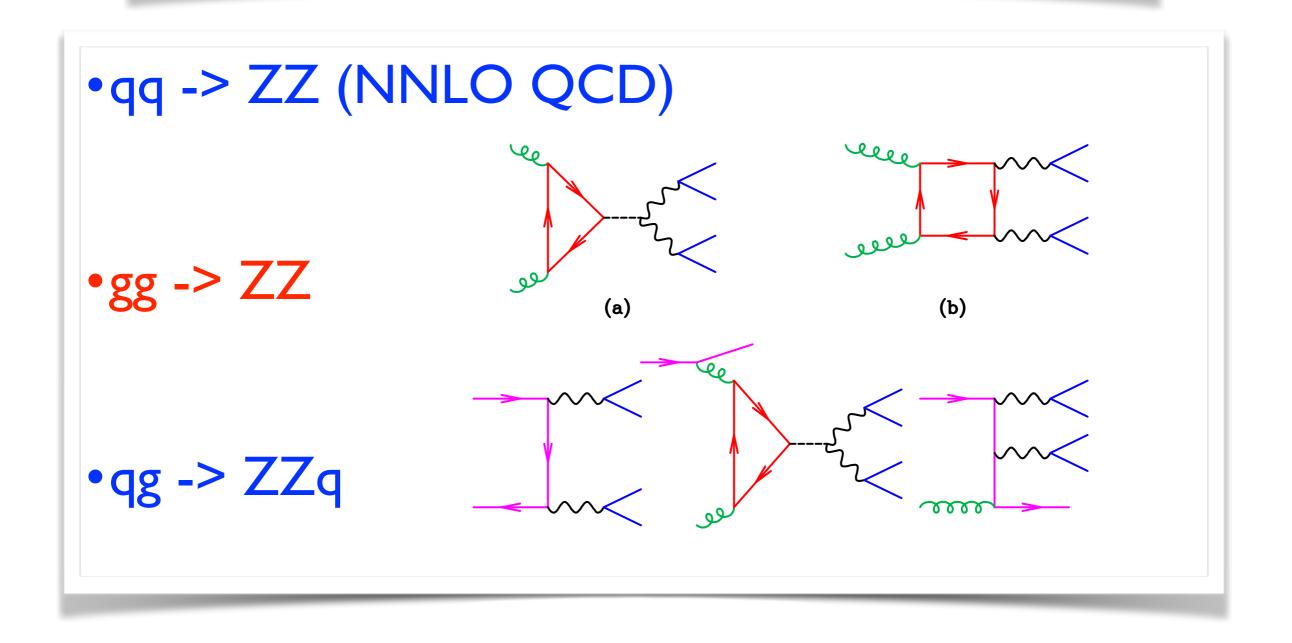


 Although much smaller rates, at the end of Run II: sensitivity ~ to gluon fusion right now

VERY INTERESTING COMPLEMENTARY PROCESS

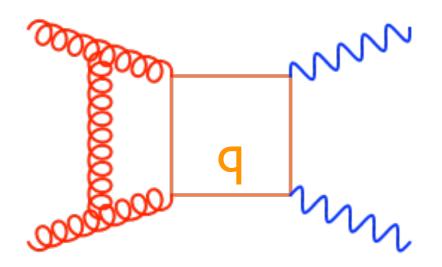
### The second issue: SM theoretical predictions

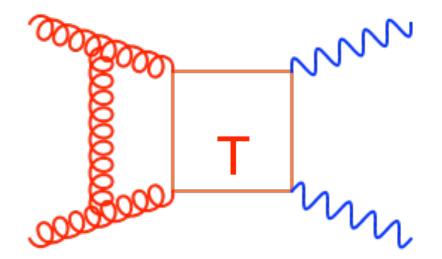
Method based on counting ZZ events in the high invariant-mass tail -> good predictions for 4I final state required



### The second issue: SM theoretical predictions

- right now, we have NNLO for the qq channel and N<sup>3</sup>LO (inclusive) for the signal, but LO ONLY FOR THE FULL GG->ZZ BACKGROUND AND INTERFERENCE
- gluon-initiated process -> expect large corrections
- the problem: loop induced process, NLO involves (very complicated) 2-loop amplitudes

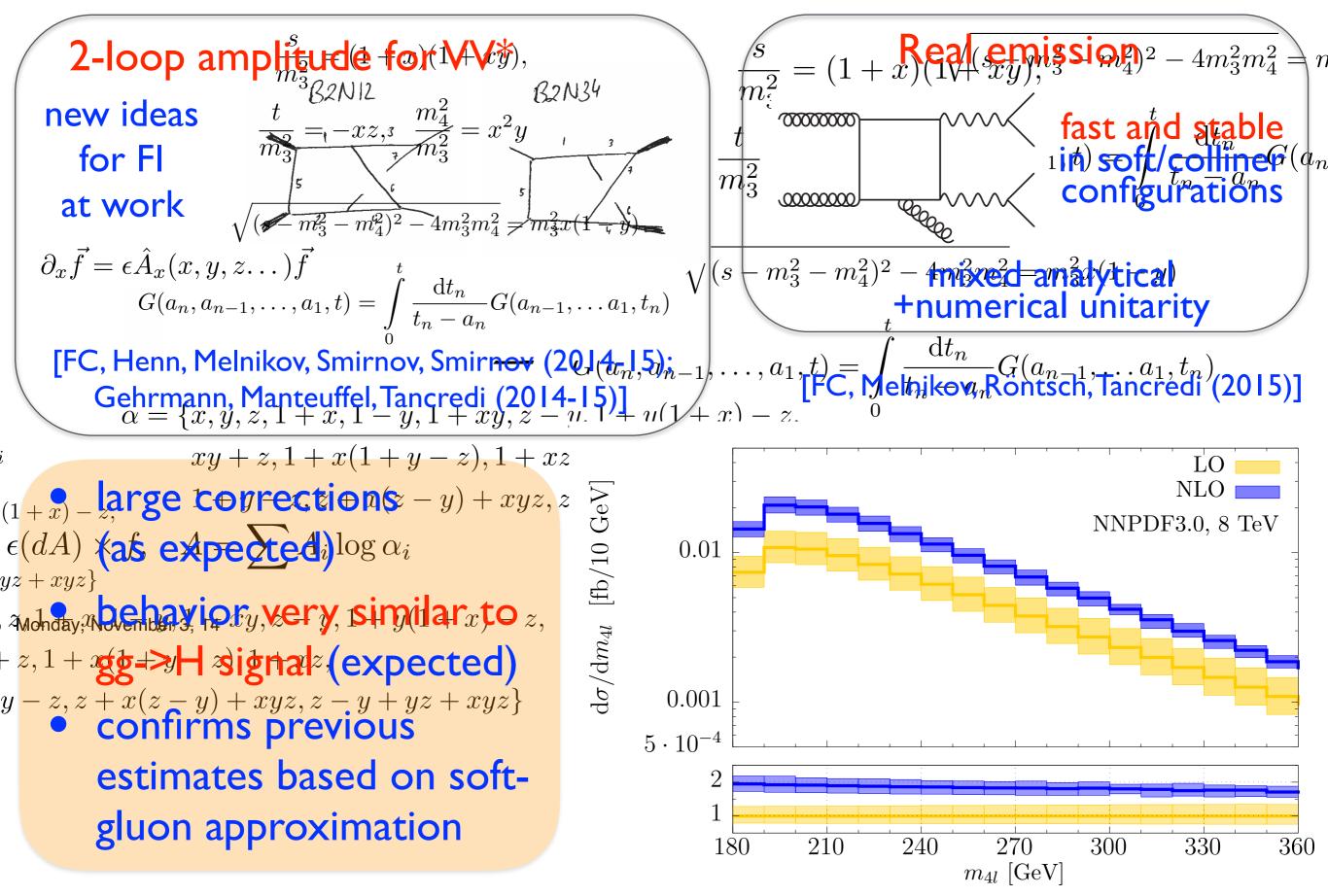




**Recently computed** 

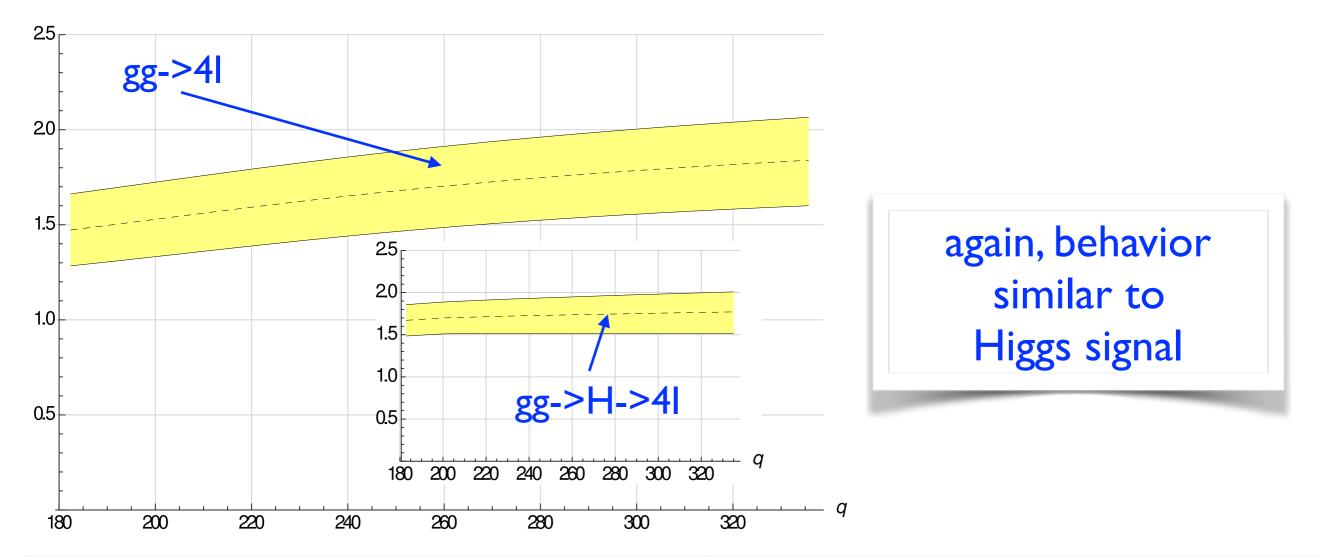
VERY HARD [important in the off-shell region]

# **gg->V(@NLO: massless quarter s** $xz, \quad \frac{m_4^2}{m_3^2} = x^2y$



# gg->VV@NLO: top loops

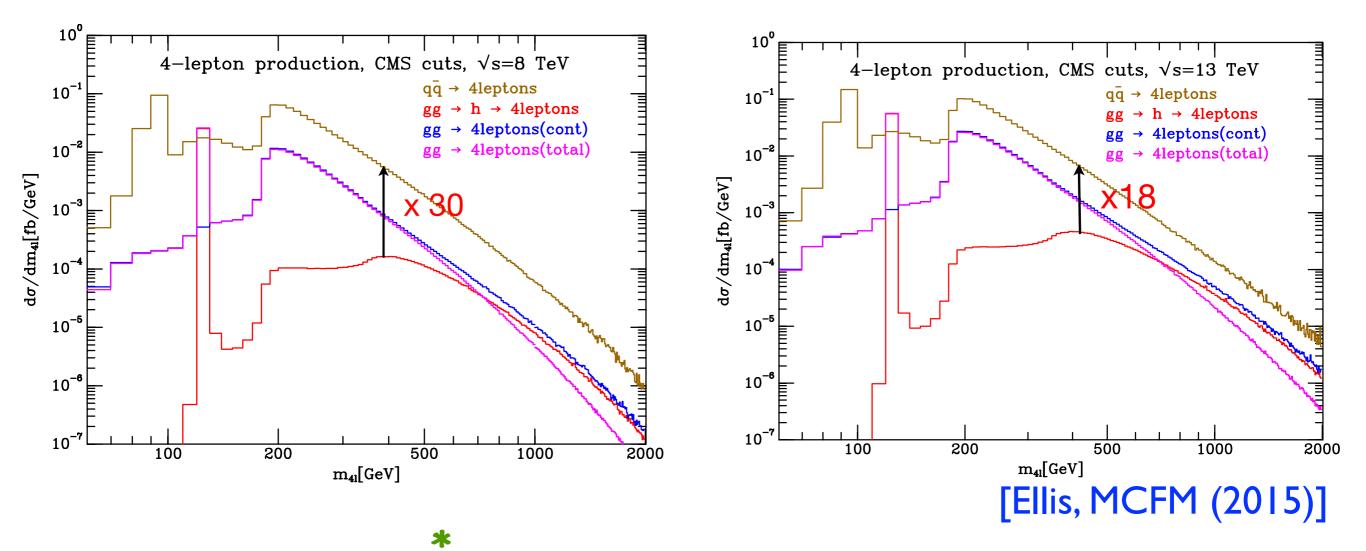
- exact result beyond reach right now
- estimates: 1/mt expansions [Dowling, Melnikov (2015)]



Both for NLO (massless) prediction and for massive 1/m<sub>t</sub> expansion, off-shell phenomenology not known yet (ongoing)

### Off-shell measurements: Run II

#### Gluon PDF groves High energy than quark PDF



S/B enhancement, \* nteresting off-shell phenomenology ahead

### Conclusions

- the Higgs is a very narrow resonance -> direct measurement of its width is not possible at hadron colliders
- still, under some assumptions it is possible to obtain indirect constraints for it
  - in the YY channel, by looking at mass shift from signal/ background interference. Theoretically clean, but experimentally challenging
  - in the ZZ channel, by measuring couplings away from the resonant peak. Big potential, but delicate theoretical issues
- if theoretical control improves, bounds as low as the SM width  $\Gamma_H \sim 4.2$  MeV may be possible at the LHC

### Outlook

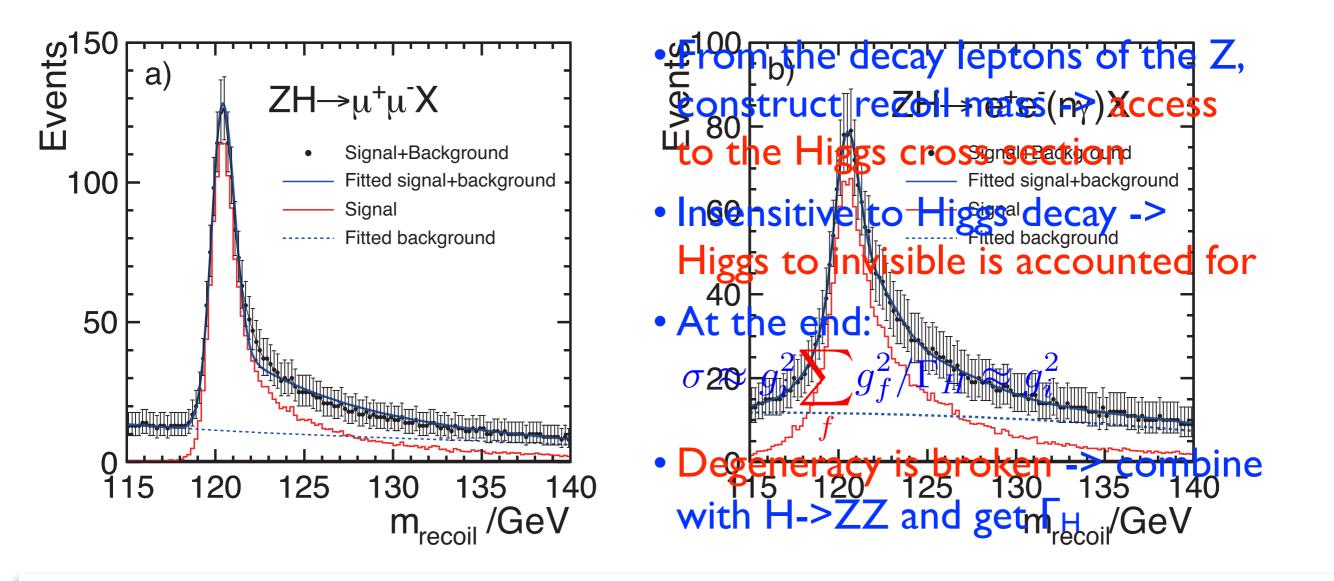
Many work still needs to be done:

- for experimentalists (better handle on the γγ interference, qq/gg->4l separation, discriminants...)
- for BSM phenomenologists (interpretation of the offshell signal, anomalous couplings, interplay off-shell vs boosted...)
- for SM theorists/phenomenologists (massive loop amplitudes, gg->m4I, Higgs pT spectrum...)

IMPACT OF THESE STUDIES WELL BEYOND THE WIDTH MEASUREMENT Thank you!

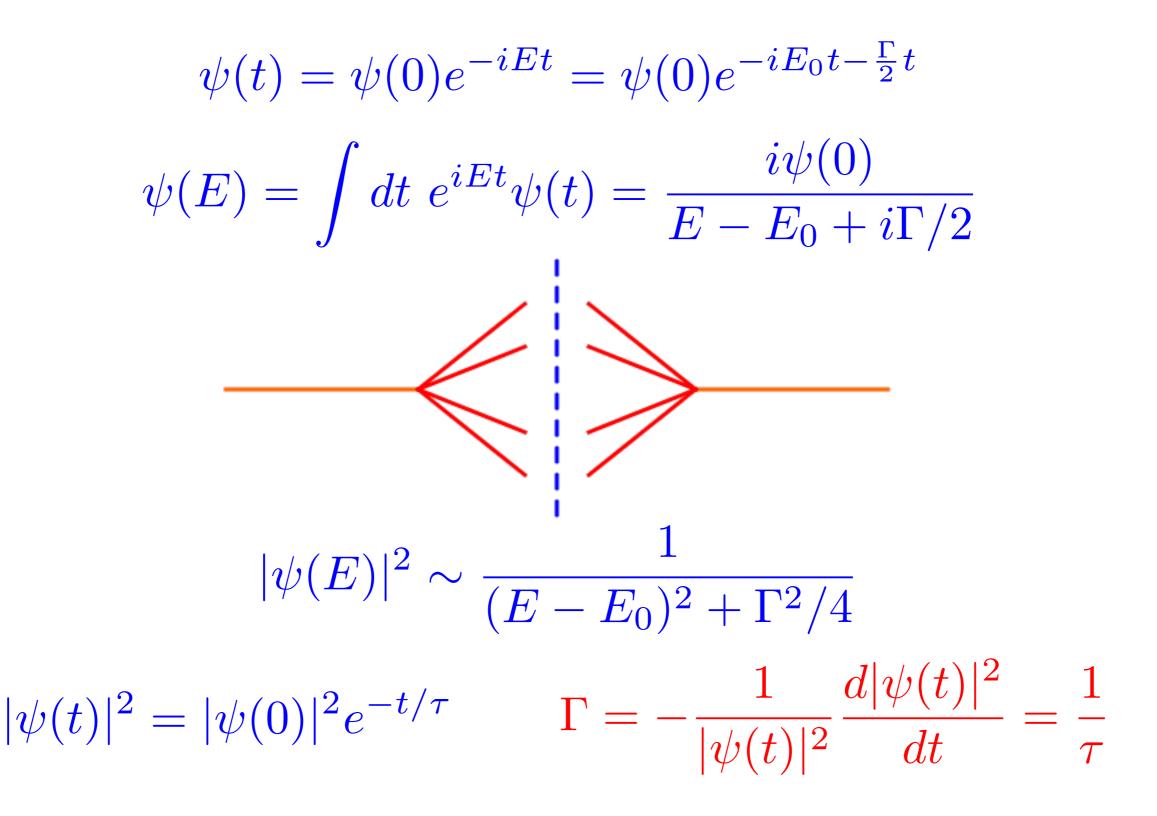


# The Bjorken process at $e^+e^-$ colliders Consider the process $e^+e^- \rightarrow Z^* \rightarrow HZ$



Measurement with few percent precision may be possible

#### Lifetime and width



### VBF rates [Ellis, talk given at MITP 2015] Rates for signal and background

#### Signal, $O(\alpha^6)$

#### Factor takes into account sum over e, $\mu$ and v<sub>e</sub>,v<sub> $\mu$ </sub>,v<sub> $\tau$ </sub>

Background,
$O(\alpha^4 \alpha_s^2)$

Process	Nominal	Cut	$\sigma$ [fb]	Factor	Events
	process		$O(\alpha^6)$		in 100 $\rm fb^{-1}$
$pp \rightarrow e^- \mu^+ \nu_\mu \bar{\nu}_e jj$	$W^-W^+$	$m_T^{WW} > 300 \text{ GeV}$	0.2378	x4	95
$pp \rightarrow \nu_e e^+ \nu_\mu \mu^+ jj$	$W^+W^+$	$m_T^{WW} > 300 \text{ GeV}$	0.1358	x2	27
$pp \rightarrow e^- \bar{\nu_e} \mu^- \bar{\nu_\mu} j j$	$W^-W^-$	$m_T^{WW} > 300 \text{ GeV}$	0.0440	x2	9
$pp \rightarrow \nu_e e^+ \mu^- \mu^+ \mu^+ j j$	$W^+Z$	$m_T^{WZ} > 300 \text{ GeV}$	0.0492	x4	20
$pp \rightarrow e^- \bar{\nu_e} \mu^- \mu^+ jj$	$W^-Z$	$m_T^{WZ} > 300 \text{ GeV}$	0.0242	x4	10
$pp \rightarrow l^- l^+ \nu_l \bar{\nu}_l j j$	ZZ	$m_T^{ZZ} > 300 \text{ GeV}$	0.0225	x6	14
$pp \rightarrow l^- l^+ \nu_l \bar{\nu}_l j j$	ZZ	$m_T^{WW} > 300 \text{ GeV}$	0.0181	x6	11
$pp \rightarrow e^- e^+ \mu^- \mu^+ j j$	ZZ	$m_{4l} > 300~{\rm GeV}$	0.0218	x2	4

**Table 3.** Electroweak ( $\mathcal{O}(\alpha^6)$ ) cross sections at  $\sqrt{s} = 13$  TeV, under the cuts given in Eqs. (2.2)– (2.6) and the off-shell definition specified in the table. The factor gives the approximate number by which the result shown for specific lepton flavours must be multiplied to account for two flavours of charged leptons,  $e, \mu$  and three flavours of neutral leptons,  $\nu_e, \nu_\mu, \nu_\tau$ .

D	NT 1	<u></u>	[0]]	D (	E (	254 events
Process	Nominal	$\operatorname{Cut}$	$\sigma \text{ [fb]} \\ O(\alpha^4 \alpha_s^2)$	Factor	Events in 100 $fb^{-1}$	
	process		$O(\alpha^{-}\alpha_{s}^{-})$		III 100 ID -	
$pp \rightarrow e^- \mu^+ \nu_\mu \bar{\nu}_e jj$	$W^-W^+$	$m_T^{WW} > 300 \text{ GeV}$	0.2227	x4	89	
$pp \rightarrow \nu_e e^+ \nu_\mu \mu^+ jj$	$W^+W^+$	$m_T^{WW} > 300 \text{ GeV}$	0.0079	x2	2	
$pp \rightarrow e^- \bar{\nu_e} \mu^- \bar{\nu_\mu} j j$	$W^-W^-$	$m_T^{WW} > 300 \text{ GeV}$	0.0025	x2	0	
$pp \rightarrow \nu_e e^+ \mu^- \mu^+ \mu^+ jj$	$W^+Z$	$m_T^{WZ} > 300 \text{ GeV}$	0.0916	x4	37	
$pp \rightarrow e^- \bar{\nu_e} \mu^- \mu^+ jj$	$W^-Z$	$m_T^{WZ} > 300 \text{ GeV}$	0.0454	x4	18	W+W+
$pp \rightarrow l^- l^+ \nu_l \bar{\nu}_l j j$	ZZ	$m_T^{ZZ} > 300 \text{ GeV}$	0.0143	x6	9	
$pp \rightarrow l^- l^+ \nu_l \bar{\nu}_l j j$	ZZ	$m_T^{WW} > 300 \text{ GeV}$	0.0118	x6	7	
$pp \rightarrow e^- e^+ \mu^- \mu^+ jj$	ZZ	$m_{4l} > 300~{\rm GeV}$	0.0147	x2	3	

**Table 4.** Mixed QCD-electroweak ( $\mathcal{O}(\alpha^4 \alpha_e^2)$ ) cross sections at  $\sqrt{s} = 13$  TeV, under the cuts given in Eqs. (2.2)-(2.6) and the off-shell definition specified in the table.

#### Ignore other sources of background, W+jet, QCD.....

- W+W+

c.f. ttbar