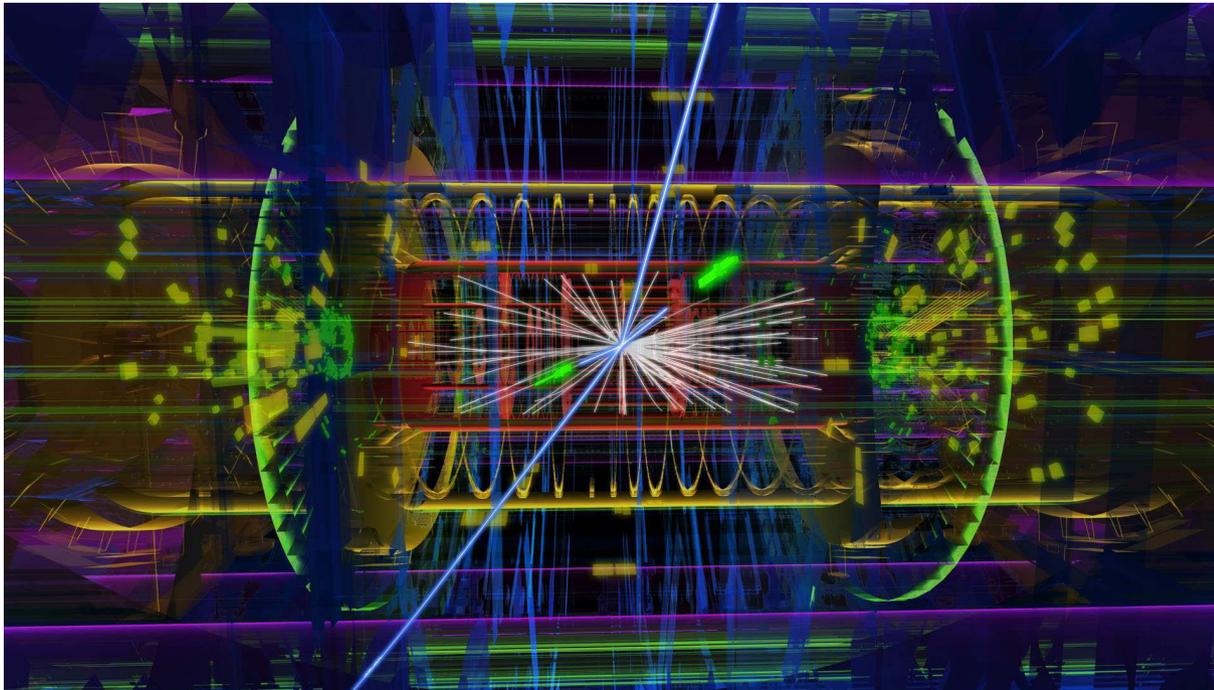


Electroweak Physics at the LHC

— Lecture 3 —

Electroweak Di-boson Production



Stefan Dittmaier

Albert-Ludwigs-Universität Freiburg



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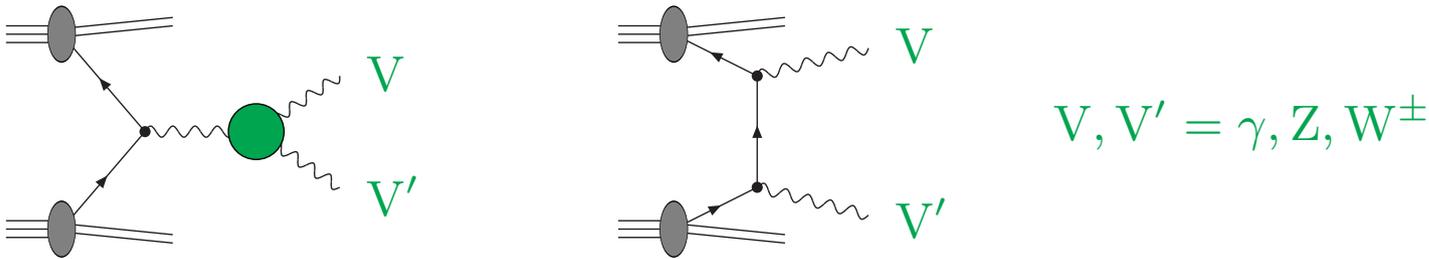
Outlook to electroweak tri-boson production

Electroweak di-boson production

brief overview



EW di-boson production



Physics issues:

- triple-gauge-boson couplings, especially at high momentum transfer
 - ◇ EW corrections significant
 - ◇ anomalous TGC: “formfactor approach” to switch off unitarity violation
 - ↪ element of arbitrariness, avoid when possible
- important background processes
 - ◇ to Higgs production, $H \rightarrow WW^*/ZZ^* \rightarrow 4f$
 - ↪ invariant masses below VV thresholds,
 - proper description of off-shell $V^*V^* \rightarrow 4f$ production required !
 - ◇ to searches at high invariant masses
 - ↪ EW corrections

State-of-the-art predictions

$W\gamma/Z\gamma$ (with leptonic decays)

- NNLO QCD [Grazzini, Kallweit, Rathlev '14,'15](#)
- NLO EW [Denner, S.D., Hecht, Pasold '14](#) ($Z\gamma$ in preparation)

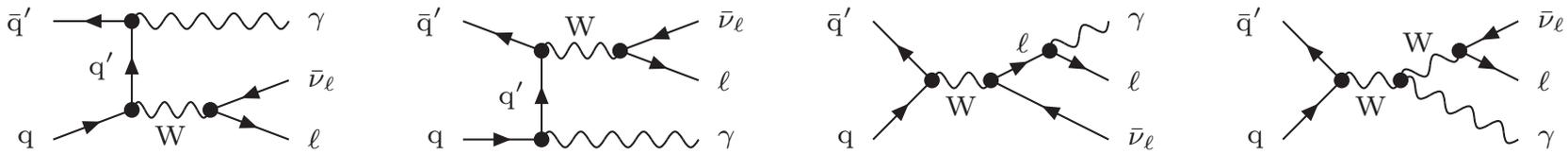
WW, WZ, ZZ

- NNLO QCD
 - ◇ ZZ (on-shell and off-shell) [Cascioli et al. '14; Grazzini, Kallweit, Rathlev '15](#)
 - ◇ WW (on-shell) [Gehrmann et al. '14](#)
 - ◇ $gg \rightarrow VV \rightarrow 4$ leptons [Binoth et al. '05,'06](#)
- NLO EW
 - ◇ stable W/Z bosons [Bierweiler, Kasprzik, Kühn '12/'13](#)
[Baglio, Le, Weber '13](#)
 - ◇ $pp \rightarrow WW \rightarrow 4$ leptons in DPA [Billoni, S.D., Jäger, Speckner '13](#)
 - ◇ approximative inclusion in **HERWIG++** [Gieseke, Kasprzik, Kühn '14](#)
 - ◇ full off-shell calculation in progress [Denner et al.](#)

$W\gamma / Z\gamma$ production

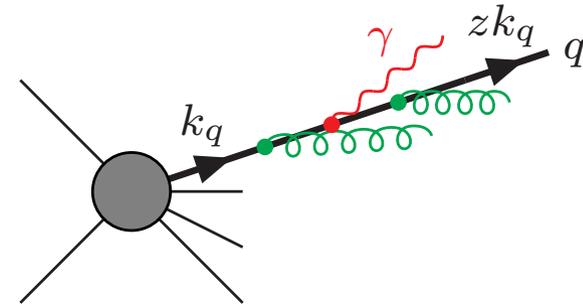


Example of $W\gamma$ production



Issues / physics goals:

- clean **photon–jet separation**
 \hookrightarrow quark-to-photon fragmentation function
Glover, Morgan '94
 or Frixione isolation Frixione '98



- stronger bounds on **anomalous $WW\gamma$ coupling**:

$$\begin{aligned}
 & \begin{array}{l} W_{\mu}^{+}(q) \\ W_{\nu}^{-}(\bar{q}) \end{array} \begin{array}{l} \text{---} \\ \text{---} \end{array} \text{---} \gamma_{\rho}(p) = e \left\{ \bar{q}^{\mu} g^{\nu\rho} \left(\Delta\kappa^{\gamma} + \lambda^{\gamma} \frac{q^2}{M_W^2} \right) - q^{\nu} g^{\mu\rho} \left(\Delta\kappa^{\gamma} + \lambda^{\gamma} \frac{\bar{q}^2}{M_W^2} \right) \right. \\
 & \left. + (\bar{q}^{\rho} - q^{\rho}) \frac{\lambda^{\gamma}}{M_W^2} \left(p^{\mu} p^{\nu} - \frac{1}{2} g^{\mu\nu} p^2 \right) \right\} \times \left(1 + \frac{M_{W\gamma}^2}{\Lambda^2} \right)^2
 \end{aligned}$$

ATLAS limits '12: $\Delta\kappa^{\gamma} = 0.41$, $\lambda^{\gamma} = 0.074$ for $\Lambda = 2 \text{ TeV}$

Why?

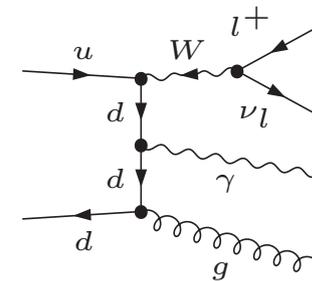
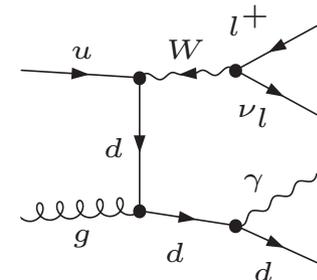
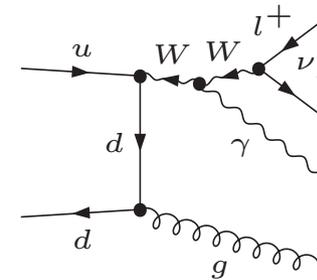
- QCD radiation cannot be suppressed by cuts
 \hookrightarrow treat at least soft/collinear jets inclusively

- separation of collinear quarks and photons leads to IR-unstable corrections $\propto \ln(m_q^2/Q^2)$
 \hookrightarrow recombine collinear quarks and photons

- quark and gluon jets cannot be distinguished event by event
 \hookrightarrow common recombination required for quarks/gluons with photons

$$\Rightarrow \underbrace{(\mathbf{g}_{\text{hard}} + \boldsymbol{\gamma}_{\text{soft}})}_{\text{EW corr. to } X+\text{jet}} \text{ and } \underbrace{(\mathbf{g}_{\text{soft}} + \boldsymbol{\gamma}_{\text{hard}})}_{\text{QCD corr. to } X+\boldsymbol{\gamma}} \text{ both appear as 1 jet}$$

Problem: signatures of $X+\text{jet}$ and $X+\boldsymbol{\gamma}$ overlap !



Photon–jet separation via photon fragmentation function $D_{q \rightarrow \gamma}$ Glover, Morgan '94

Solution:

- **idea:** declare photon/jet systems as photon or jet according to energy share

- determine photon energy fraction $z_\gamma = \frac{E_\gamma}{E_{\text{jet}} + E_\gamma}$ of photon/jet system

↪ event selection:

$$z_\gamma > z_0: \quad \text{photon}$$

$$z_\gamma < z_0: \quad \text{jet} \quad (\text{typical value } z_0 = 0.7)$$

- **but:** cut on z_γ destroys inclusiveness needed for KLN theorem

↪ collinear singularity $\propto \alpha \ln m_q$ remains (but are universal!)

- absorb universal collinear singularity in “fragmentation function” $D_{q \rightarrow \gamma}(z_\gamma)$

↪ subtract convolution of LO cross section with

$$D_{q \rightarrow \gamma}^{\overline{\text{MS}}}(z_\gamma, \mu_{\text{fact}}) \Big|_{\text{mass.reg.}} = \frac{\alpha Q_q^2}{2\pi} P_{q \rightarrow \gamma}(z_\gamma) \left[\ln \frac{m_q^2}{\mu_{\text{fact}}^2} + 2 \ln z_\gamma + 1 \right] \leftarrow \text{cancels coll. singularities}$$

$$+ D_{q \rightarrow \gamma}^{\text{ALEPH}}(z_\gamma, \mu_{\text{fact}}) \leftarrow \text{non-perturbative part fitted to ALEPH data}$$

where $P_{q \rightarrow \gamma}(z_\gamma) = \frac{1+(1-z_\gamma)^2}{z_\gamma} =$ quark-to-photon splitting function

Idea: suppress jets inside collinear cone around photons:

$$p_{T,\text{jet}} < \varepsilon p_{T,\gamma} \left(\frac{1 - \cos R_{\gamma\text{jet}}}{1 - \cos R_0} \right) \quad (R_0 = \text{fixed cone size})$$

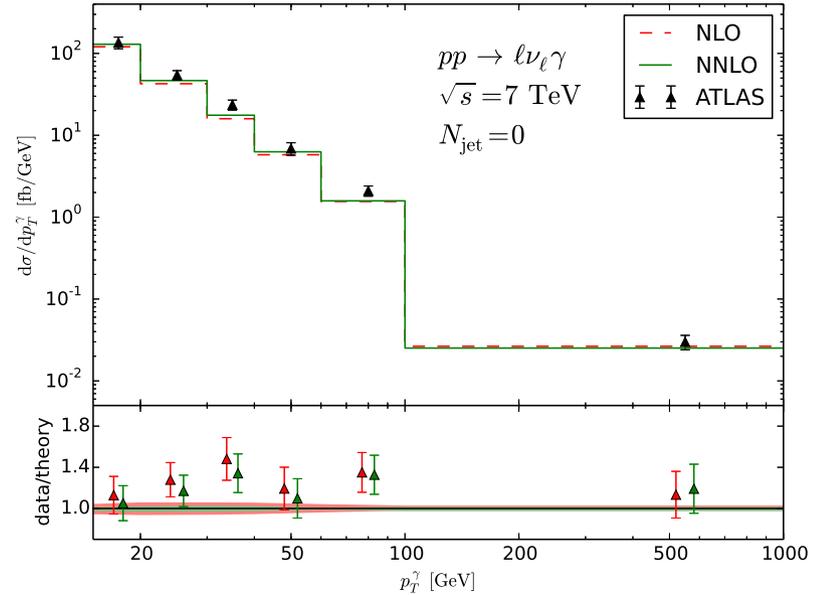
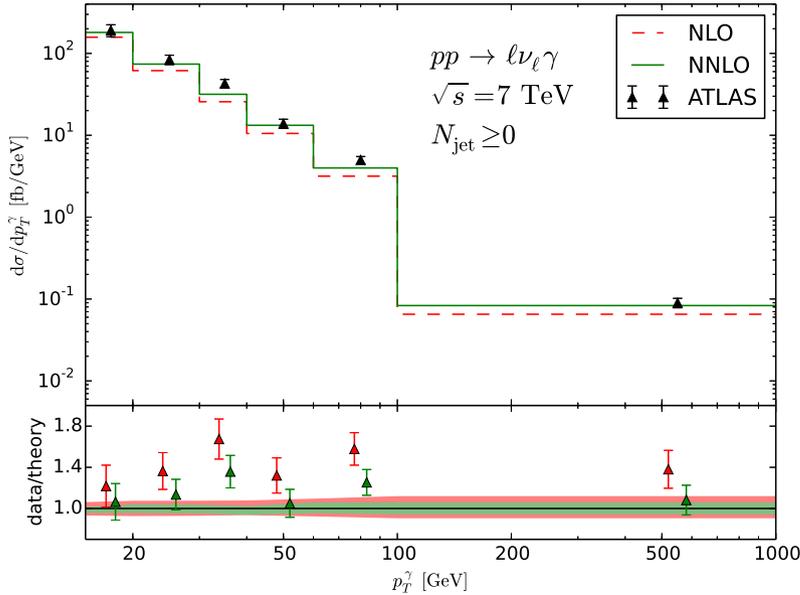
- photon and jet collinear ($R_{\gamma\text{jet}} \rightarrow 0$) \rightarrow event discarded
- photon soft or collinear to beams ($p_{T,\gamma} \rightarrow 0$) \rightarrow event discarded
- jet soft or collinear beams ($p_{T,\text{jet}} \rightarrow 0$) \rightarrow event kept \Rightarrow IR safety

Comments:

- Frixione isolation simple to implement theoretically, but problematic experimentally
- cleaner isolation of non-perturbative effects by fragmentation function
- approximate relation between the two methods:

$$z_\gamma \sim \frac{p_{T,\gamma}}{p_{T,\gamma} + p_{T,\text{jet}}} > \frac{1}{1 + \varepsilon \frac{1 - \cos R_{\gamma\text{jet}}}{1 - \cos R_0}} \sim \frac{1}{1 + \varepsilon} \quad \text{for } R_{\gamma\text{jet}} \sim R_0$$

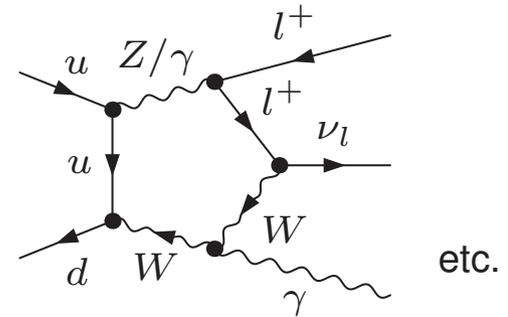
\hookrightarrow methods yield quite similar results for $z_0 \sim \frac{1}{1 + \varepsilon}$



- good agreement of experimental results with NNLO QCD (no EW corrections included)
- QCD uncertainties: (for small/moderate $p_{T,\gamma}$)
 scale: 4–5%, PDF: 1–2% (increasing with $p_{T,\gamma}$)
- LHC run 2: higher energy reach & higher statistics
 ↪ EW corrections important

- NLO EW corrections calculated with full W off-shell/decay effects (complex-mass scheme)

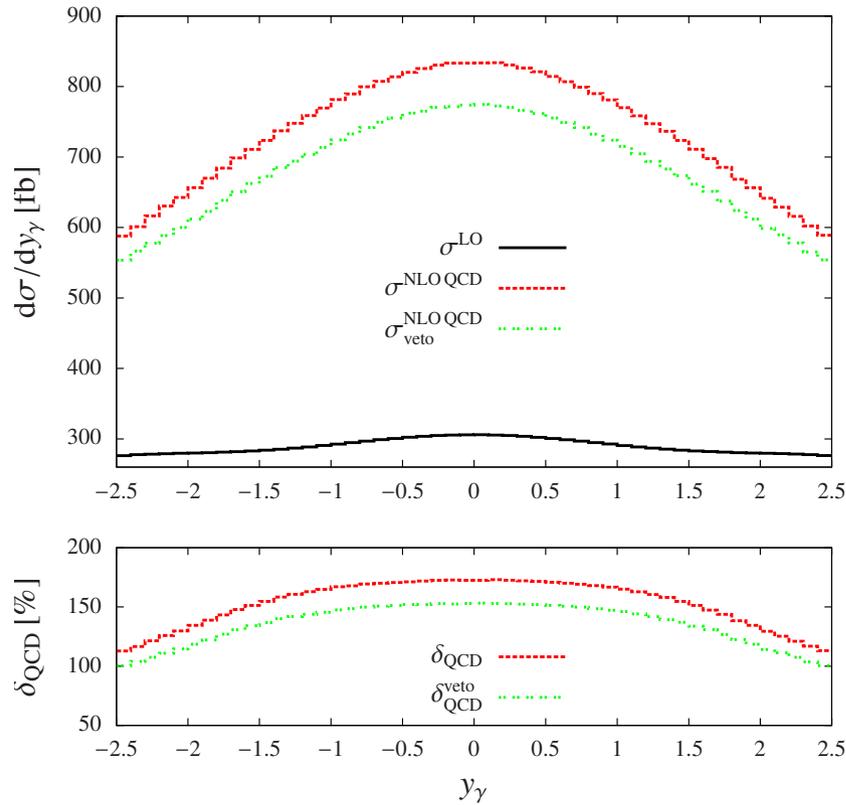
↪ more + more complicated diagrams than in QCD



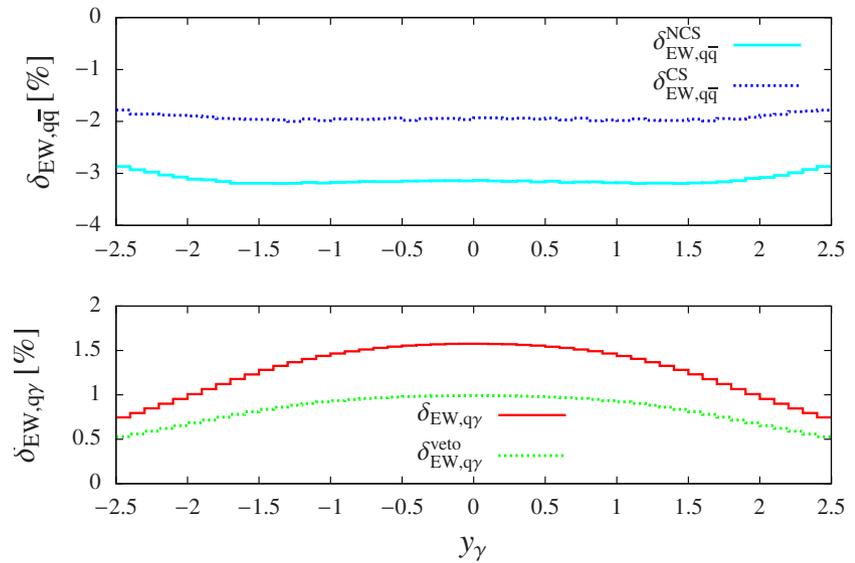
- particular focus on:

- ◇ high energies (e.g. large p_T):
large EW corrections ↔ sensitivity to anomalous couplings
↪ missing corrections could fake anomalous couplings
- ◇ photon-induced contributions

$pp \rightarrow l^+ \nu_l \gamma$ (jet)



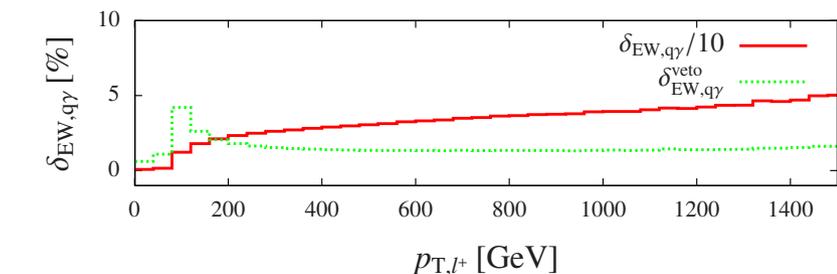
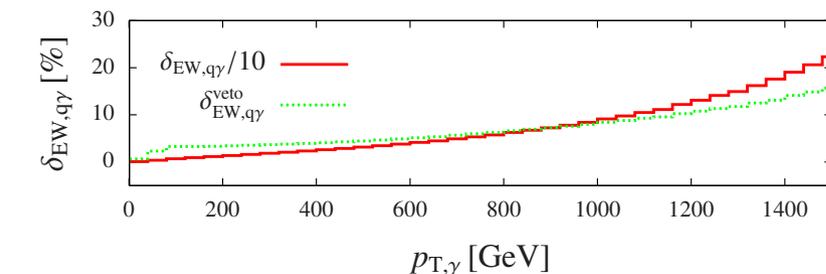
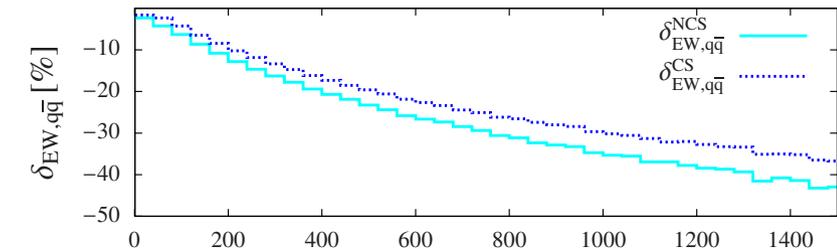
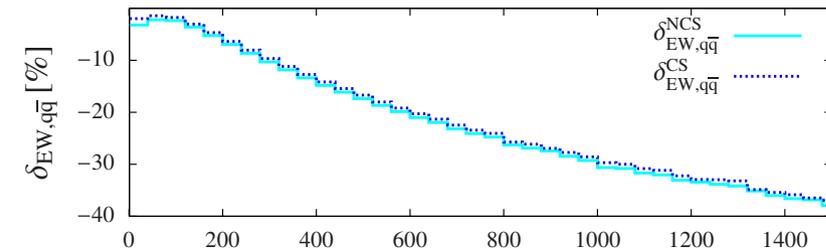
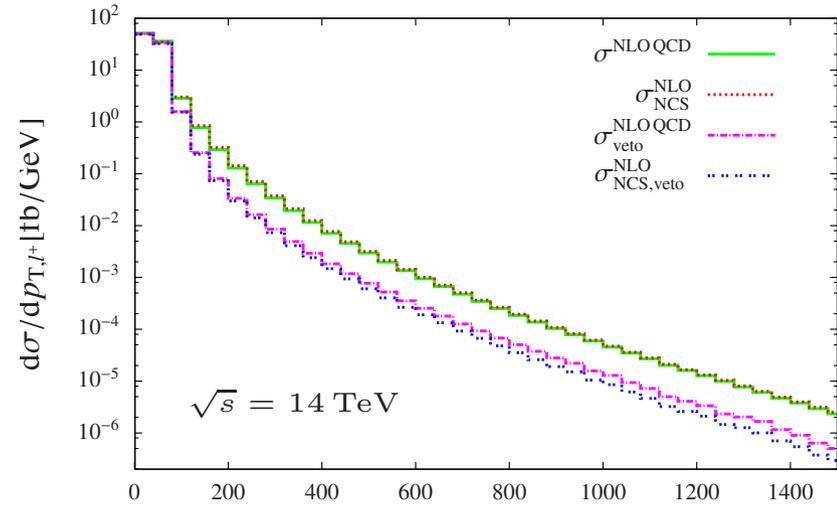
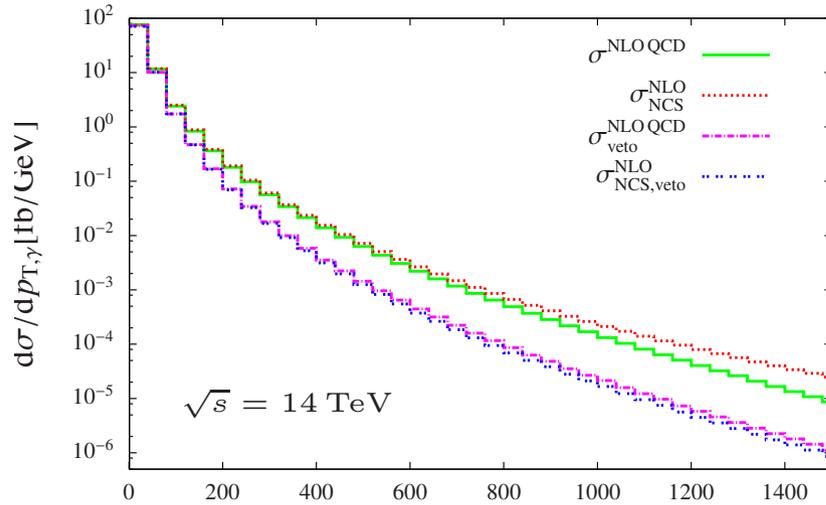
$\sqrt{s} = 14 \text{ TeV}$



- huge QCD corrections ($\sim 100\%$), only mildly reduced by jet veto $p_{\text{T,jet}} < 100 \text{ GeV}$
- EW corrections and $q\gamma$ channels (few %) small and flat (CS=collinear-safe, NCS=non-collinear-safe)
 \hookrightarrow resemble corrections to integrated cross section

$pp \rightarrow l^+ \nu_l \gamma (\gamma/\text{jet})$

$pp \rightarrow l^+ \nu_l \gamma (\gamma/\text{jet})$

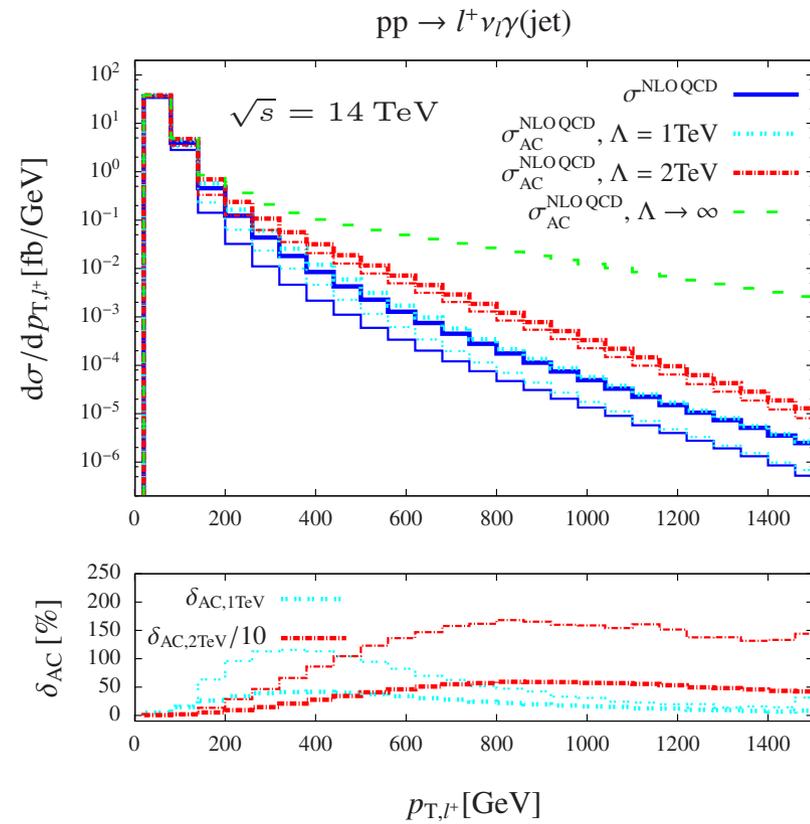
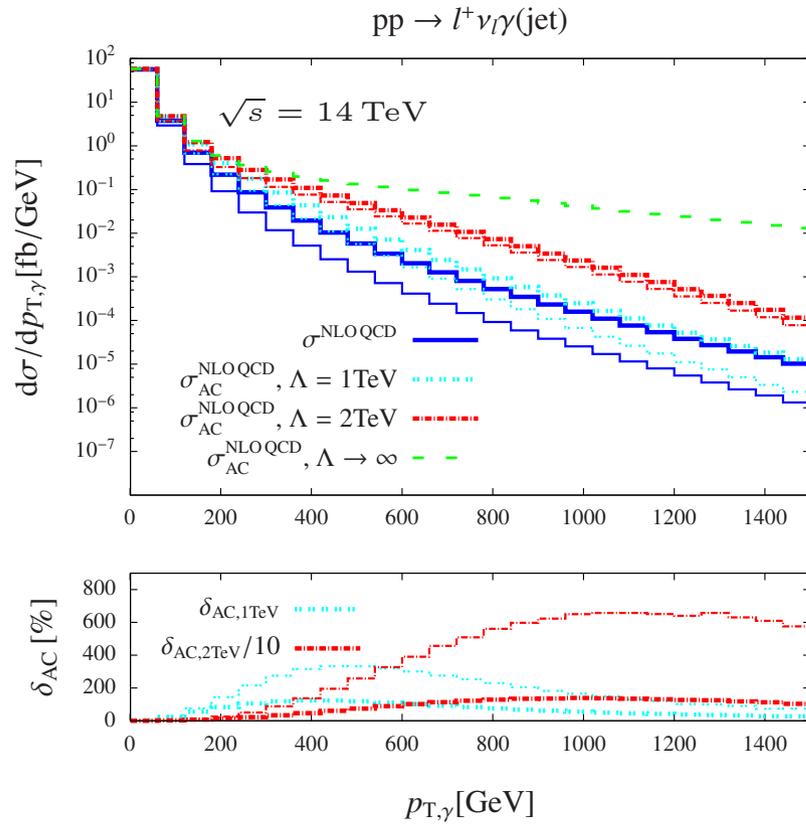


• EW corrections $\sim -30\%$ in TeV range

(CS=collinear-safe, NCS=non-collinear-safe)

• γ -induced corrections non-negligible in TeV range (even with jet veto)

↪ reduction of γ PDF uncertainties mandatory !



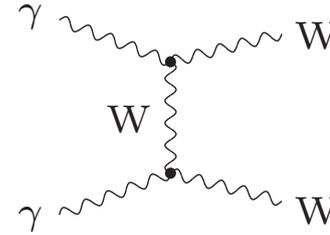
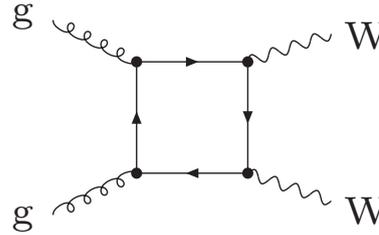
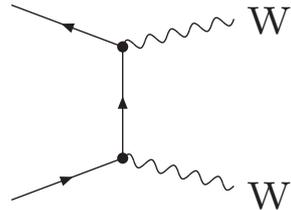
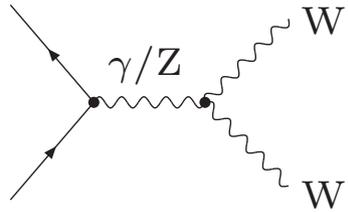
- results shown without and with jet veto on $p_{T,\text{jet}} > 100 \text{ GeV}$
- ATLAS values of 2012 used: $\Delta\kappa^\gamma = 0.41, \lambda^\gamma = 0.074$
 \hookrightarrow much tighter limits expected at LHC run 2

WW / WZ / ZZ production

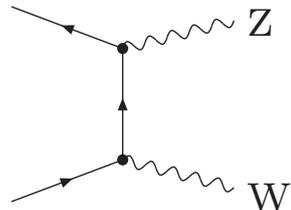
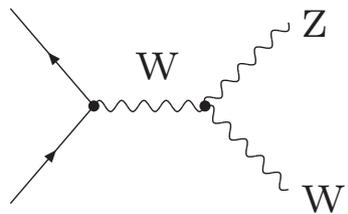


Complementarity in WW / WZ / ZZ production

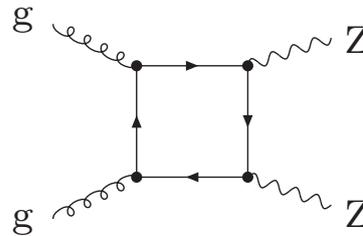
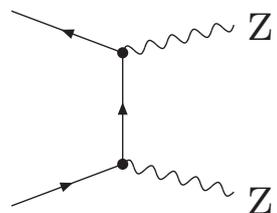
WW production:



WZ production:

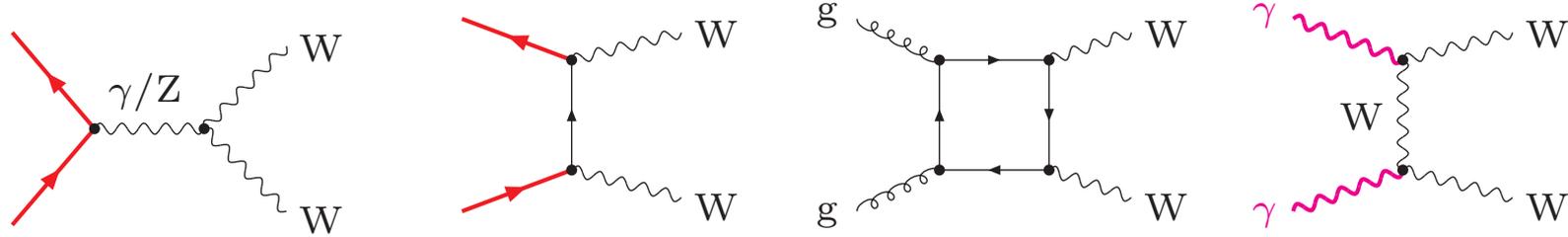


ZZ production:

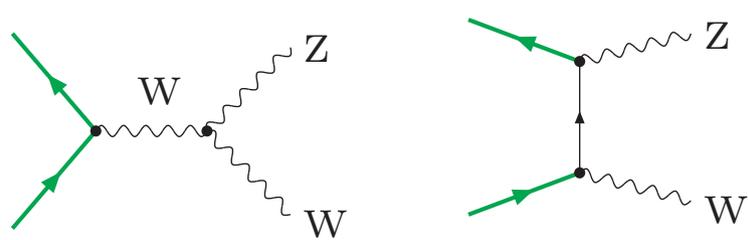


Complementarity in WW / WZ / ZZ production

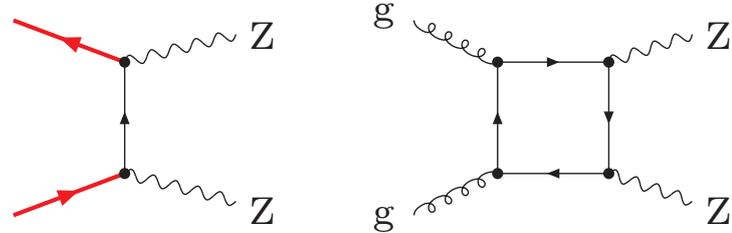
WW production:



WZ production:



ZZ production:

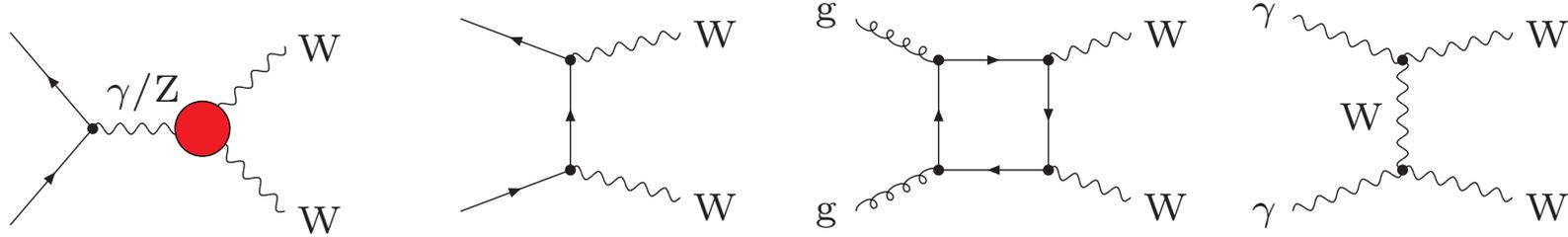


Sensitivity to different PDF combinations:

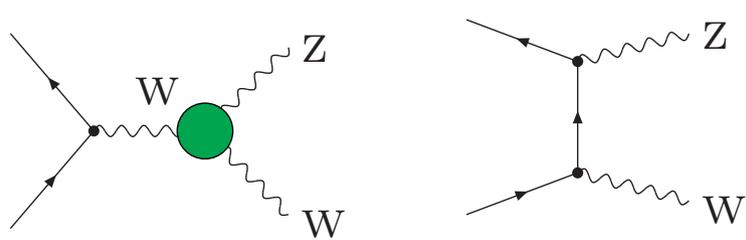
- $q\bar{q}$ in WW/ZZ
- $u\bar{d}/d\bar{u}$ in W^+Z/W^-Z
- $\gamma\gamma$ in WW

Complementarity in WW / WZ / ZZ production

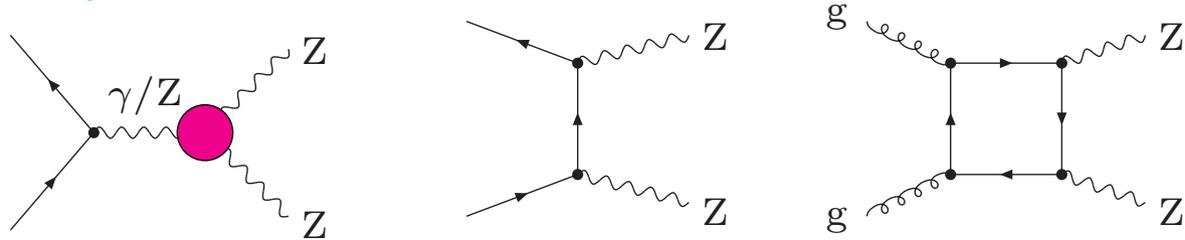
WW production:



WZ production:



ZZ production:

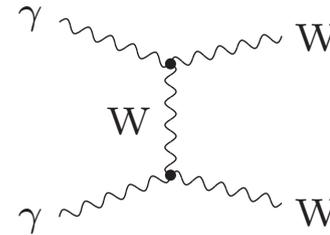
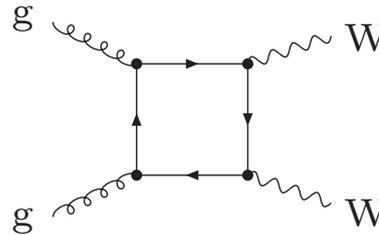
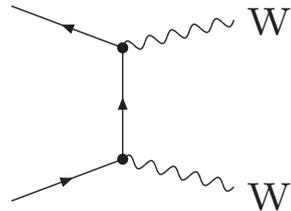
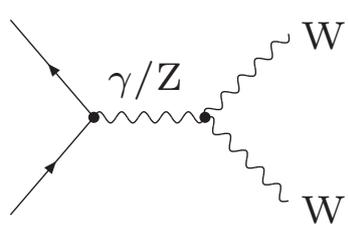


Sensitivity to different anomalous TGCs:

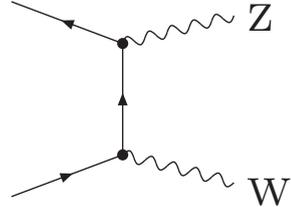
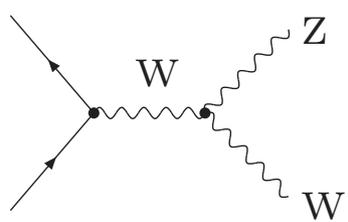
- overlay of $\gamma WW / ZWW$ in WW
- only ZWW in WZ
- $\gamma ZZ / ZZZ$ in ZZ

Complementarity in WW / WZ / ZZ production

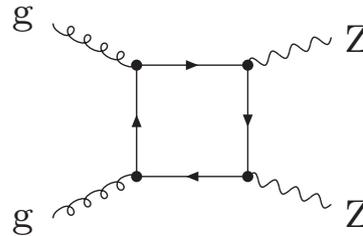
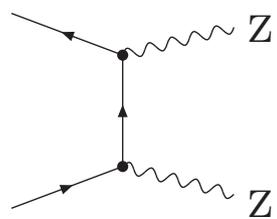
WW production:



WZ production:

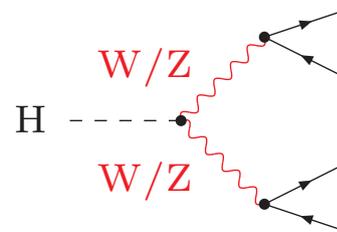


ZZ production:



Background to Higgs production
in channel $H \rightarrow WW^*/ZZ^* \rightarrow 4f$

↪ off-shell calculation
particularly important for WW/ZZ !

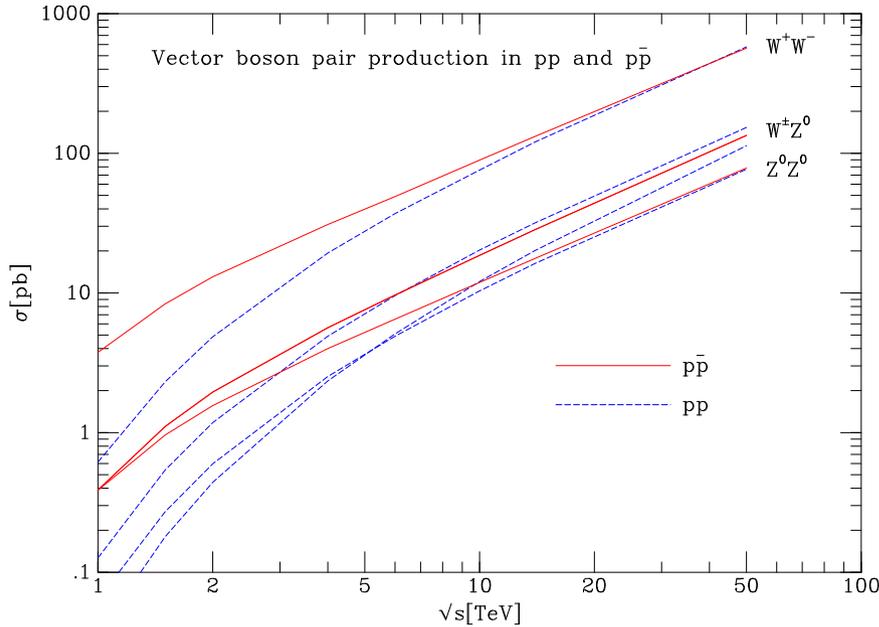


QCD corrections to WW, WZ, ZZ, W γ , Z γ production

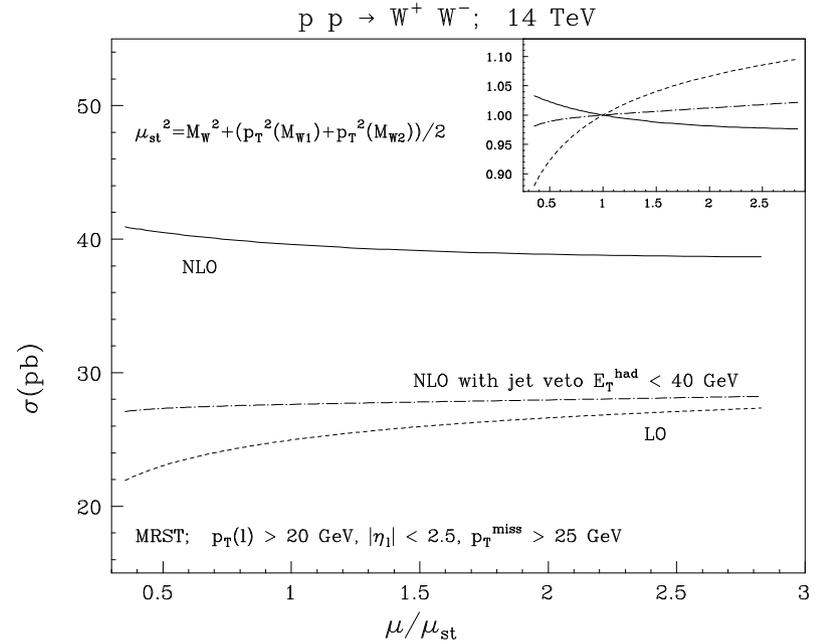
NLO QCD calculated (including leptonic W/Z decays)

Baur, Han, Ohnemus '93-'98
 Dixon, Kunszt, Signer '99
 Campbell, R.K.Ellis '99
 DeFlorian, Signer '00

Campbell, R.K.Ellis et al. '99

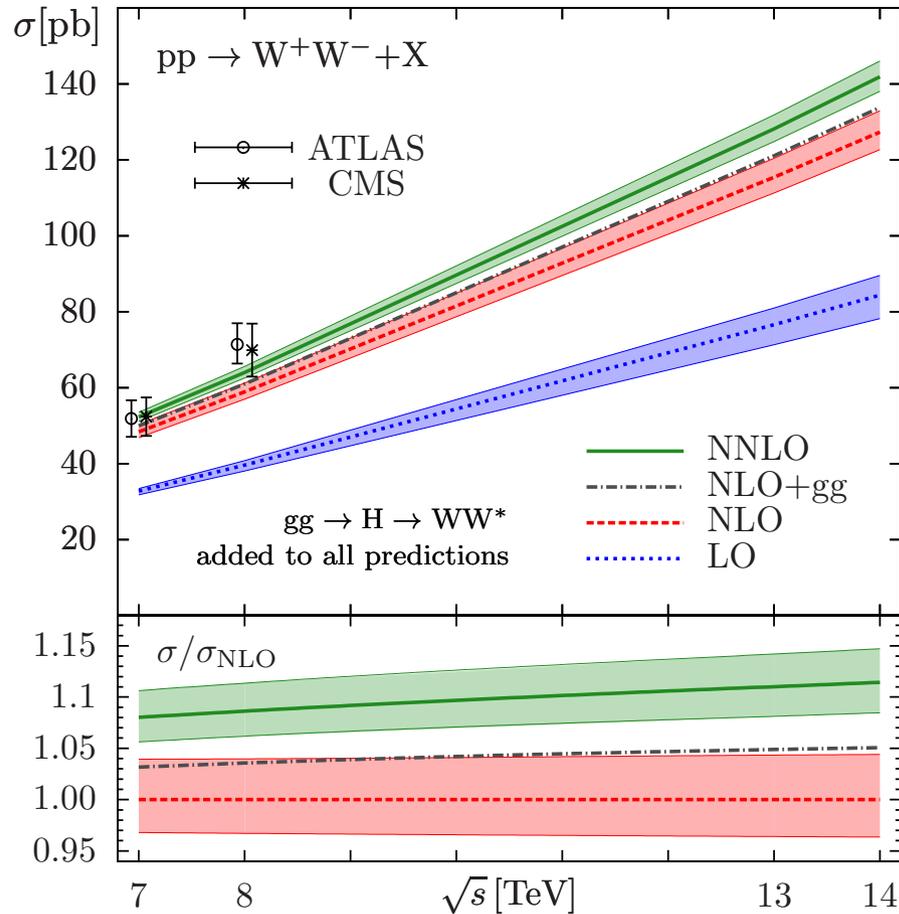


Haywood et al. '00



Large positive corrections due to jet radiation, i.e. $VV + \text{jet}$ production

- reduction of corrections and scale dependence by jet veto: $p_{T,\text{jet}} < \text{cut} ?$
 \hookrightarrow include QCD resummation for veto
- NNLO QCD corrections important

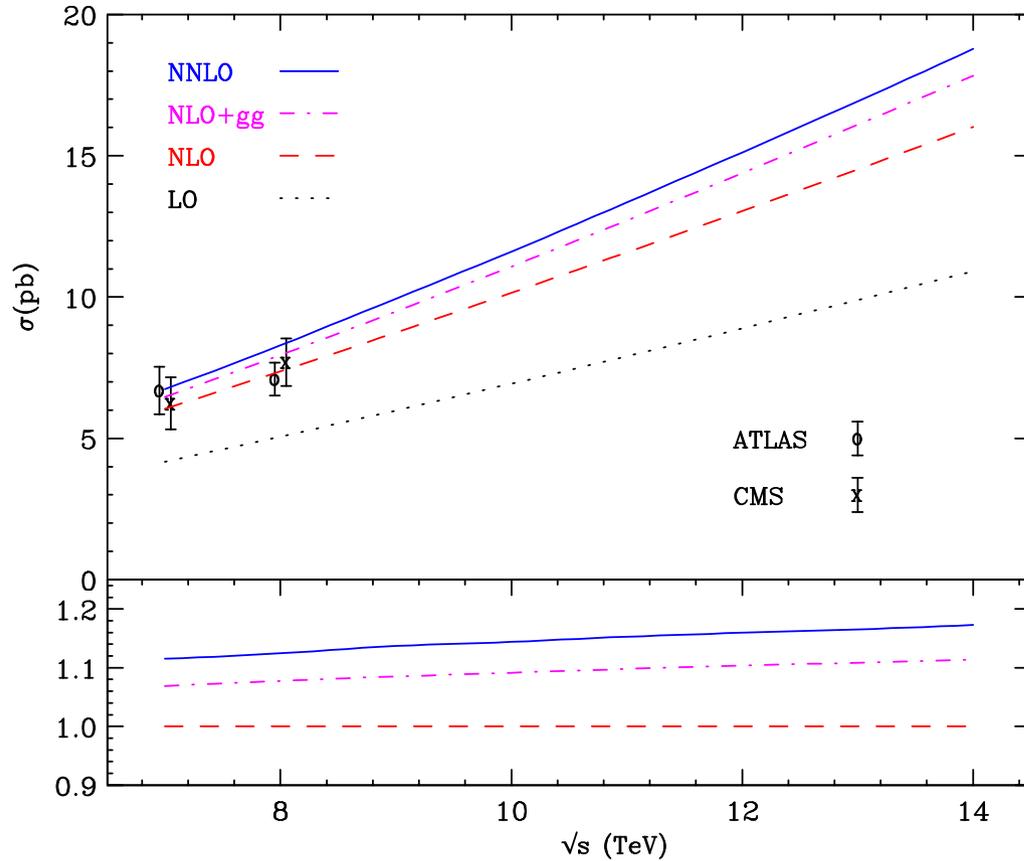


Subtlety:

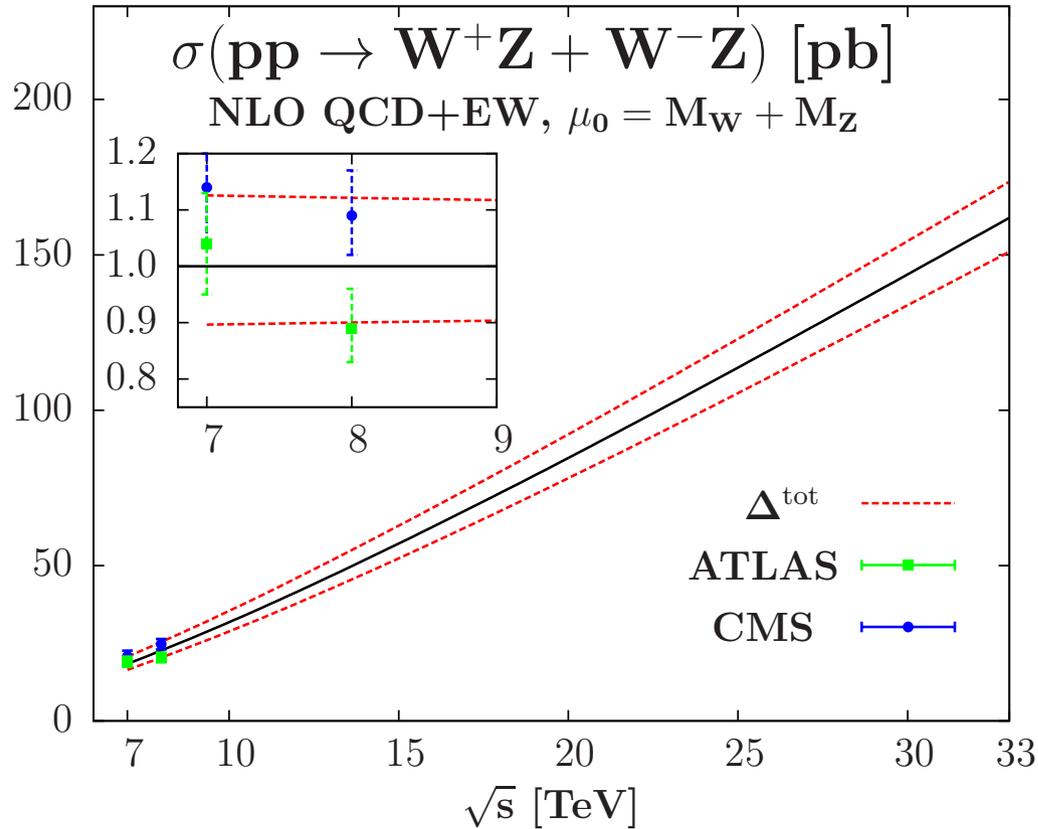
Separation of single- t and $t\bar{t}$ contributions @ NNLO QCD

\hookrightarrow b-jet veto, etc.

- good agreement of experimental results with NNLO QCD
- NNLO QCD correction $\sim 7(12)\%$ @ 8(13) TeV, scale uncertainty $\lesssim 3\%$
- gg contribution $\sim 7(8)\%$ @ 8(13) TeV
- LHC run 2: higher energy & higher statistics \rightarrow EW corrections important



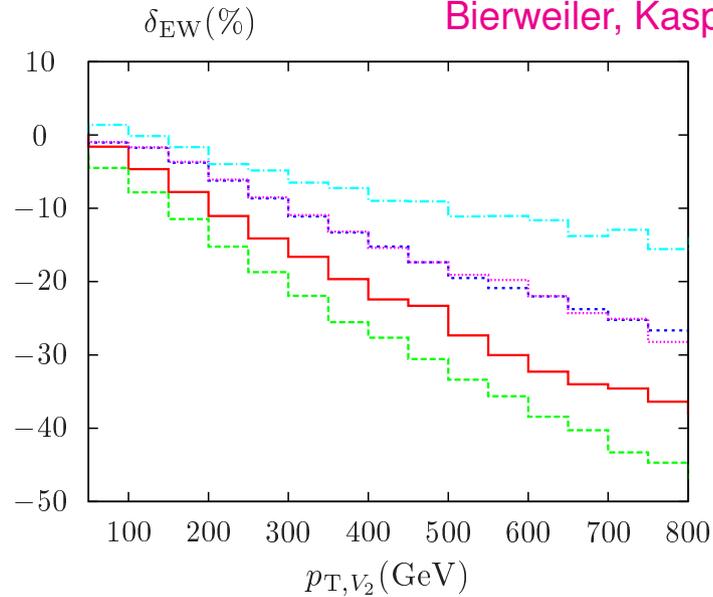
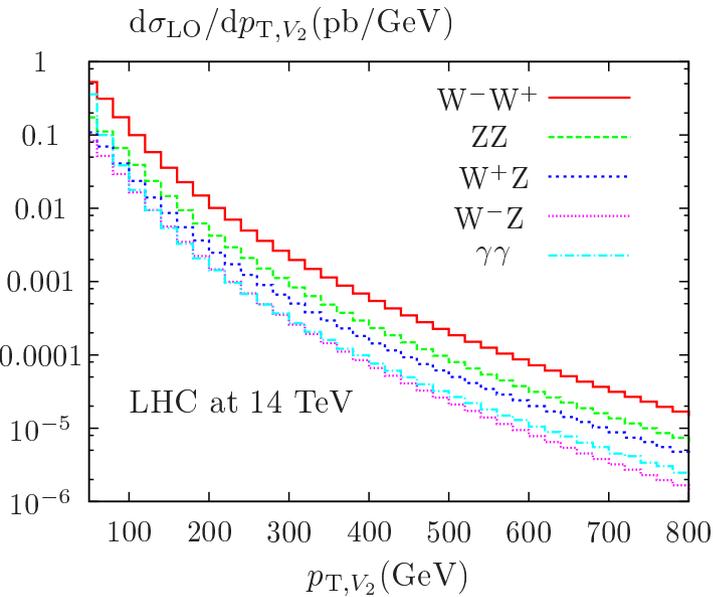
- good agreement of experimental results with NNLO QCD
- NNLO QCD correction $\sim 12(17)\%$ @ 8(13) TeV, scale uncertainty $\lesssim 3\%$
- gg contribution $\sim 7(10)\%$ @ 8(13) TeV
- LHC run 2: higher energy & higher statistics \rightarrow EW corrections important



- good agreement of experimental results with NLO QCD
- NLO QCD scale uncertainty $\sim 3\%$, $\Delta_{\text{PDF}+\alpha_s} \sim 4\%$
- LHC run 2: higher energy & higher statistics
 \hookrightarrow NNLO QCD and NLO EW corrections important

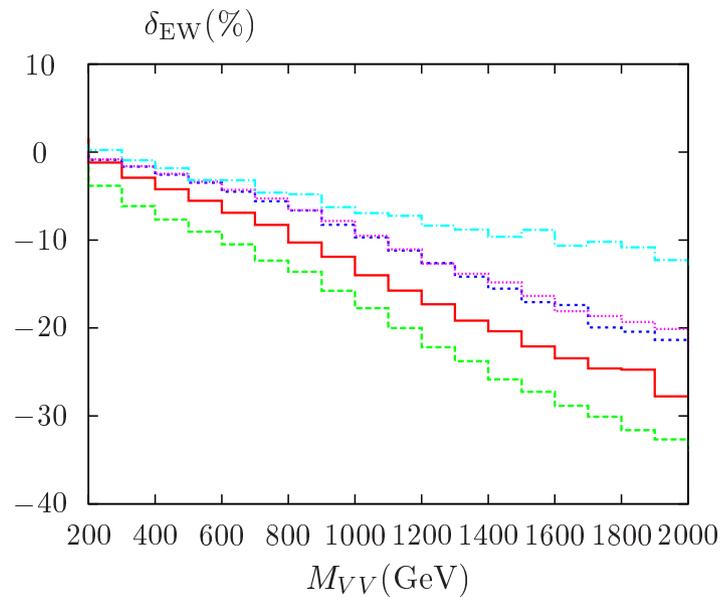
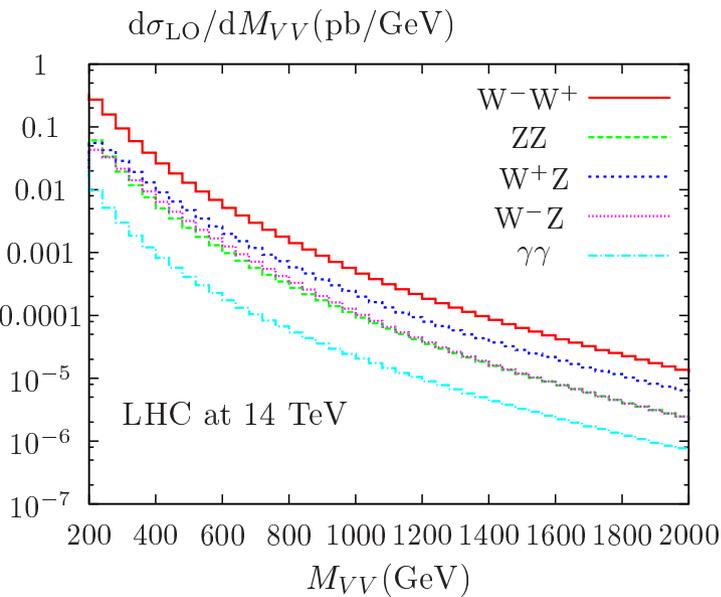
EW corrections to massive di-boson production

Bierweiler, Kasprzik, Kühn '13



EW corrections

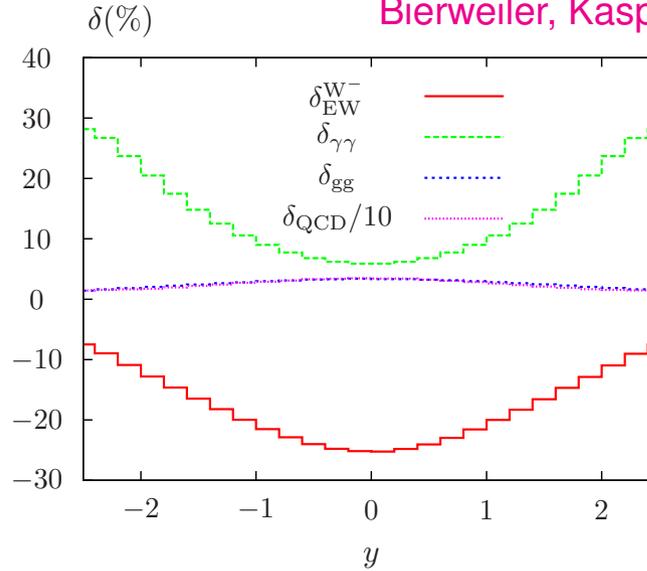
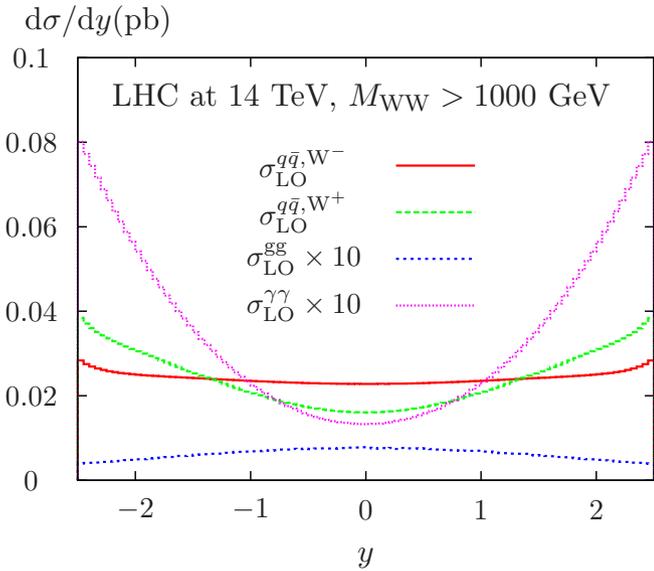
- small for integrated XS
- growing in distributions for larger scales



Note:

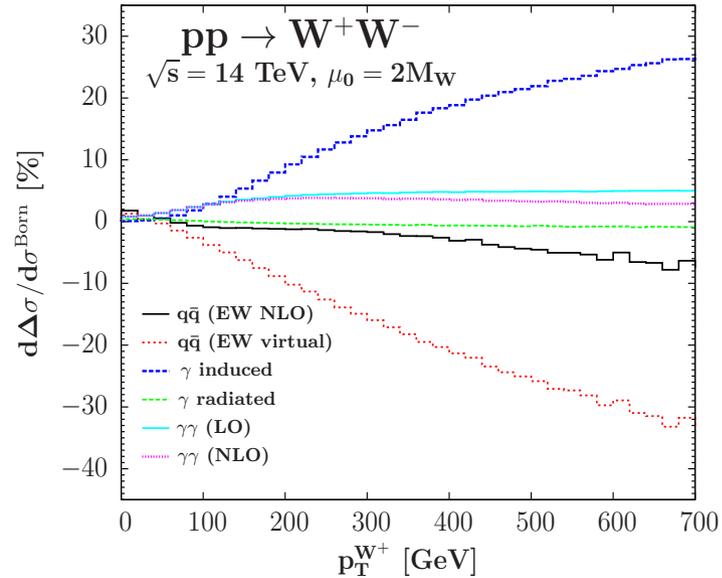
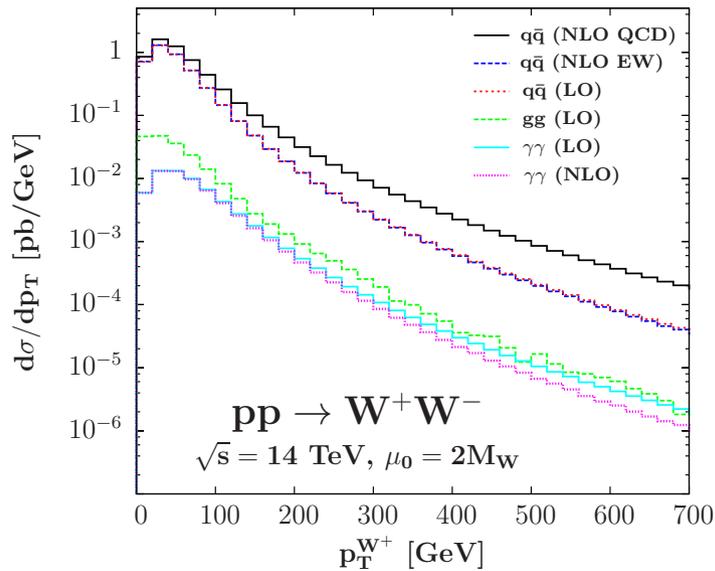
- M_{VV} not accessible for W final states
- on-shell approximation not applicable for $M_{VV} < M_{V_1} + M_{V_2}$

Survey of corrections to WW production (stable/on-shell W bosons)



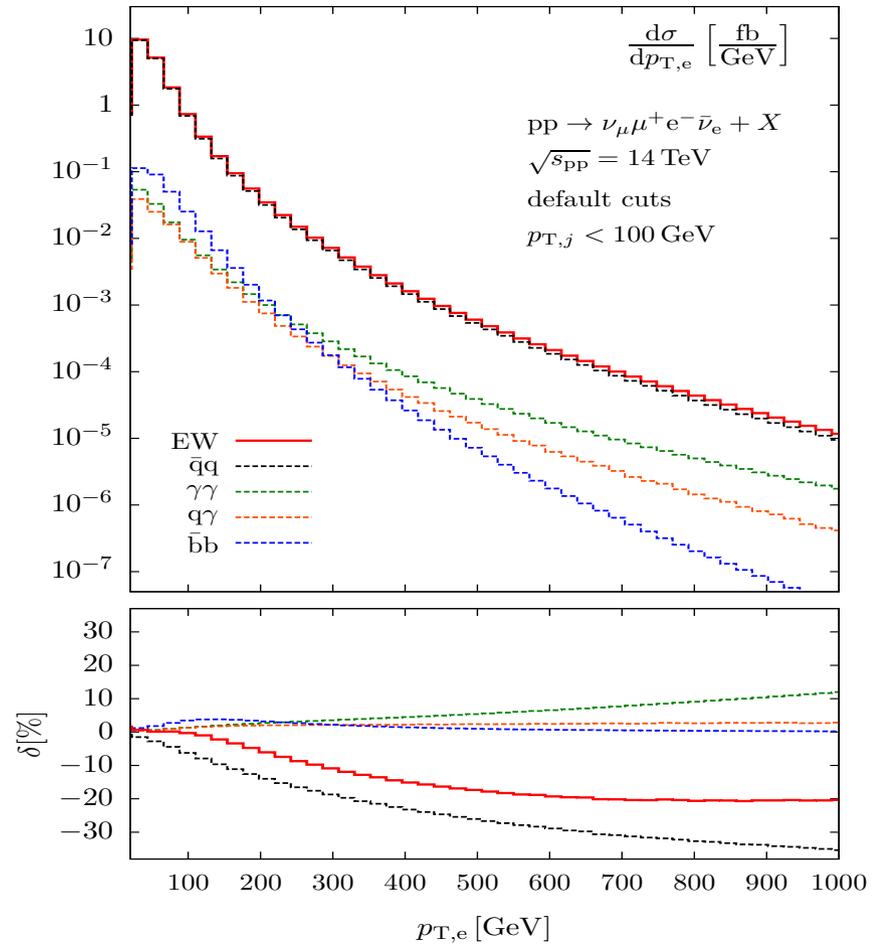
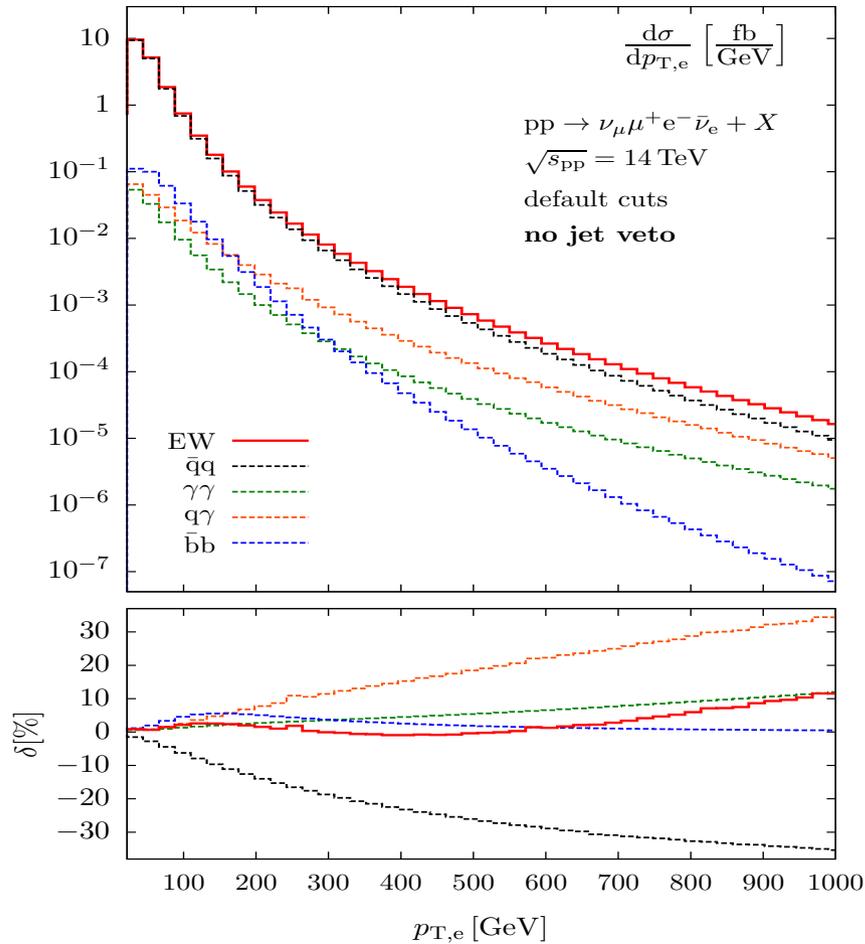
Bierweiler, Kasprzik, Kühn '12

Note:
large contribution by $\gamma\gamma$ channel for high invariant WW masses!

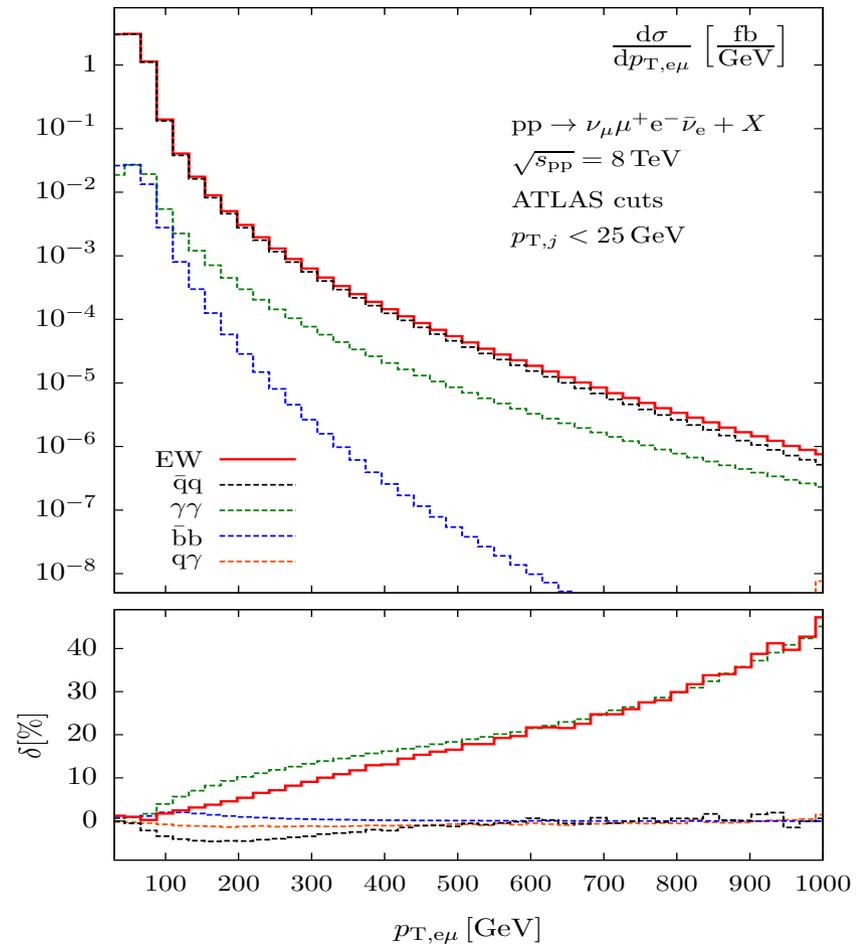
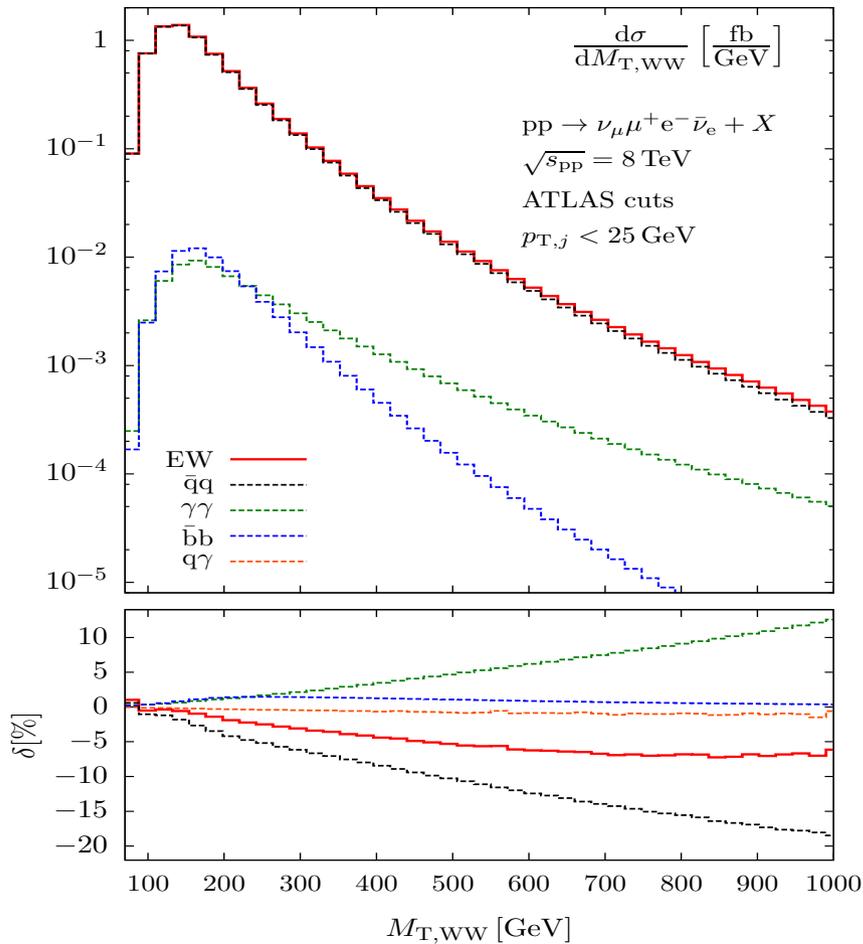


Baglio, Le, Weber '13

Large impact of $q\gamma$ collisions?



- many observables not accessible without W decays
- **sizeable influence of W decays** on EW corrections
- **$\gamma\gamma$ contribution significant** for large energies
- **$q\gamma$ contribution suppressed** by jet veto (otherwise overwhelmed by QCD corrections)

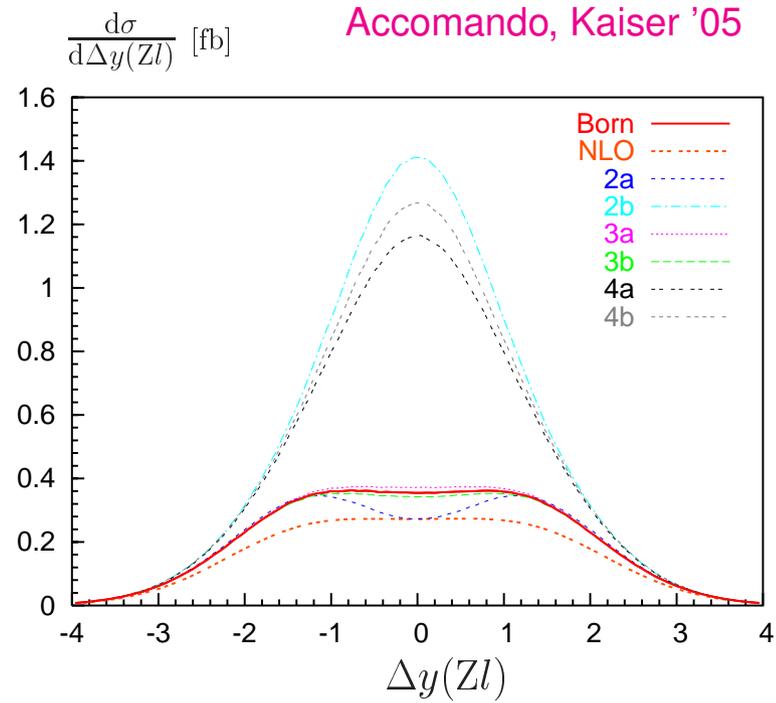
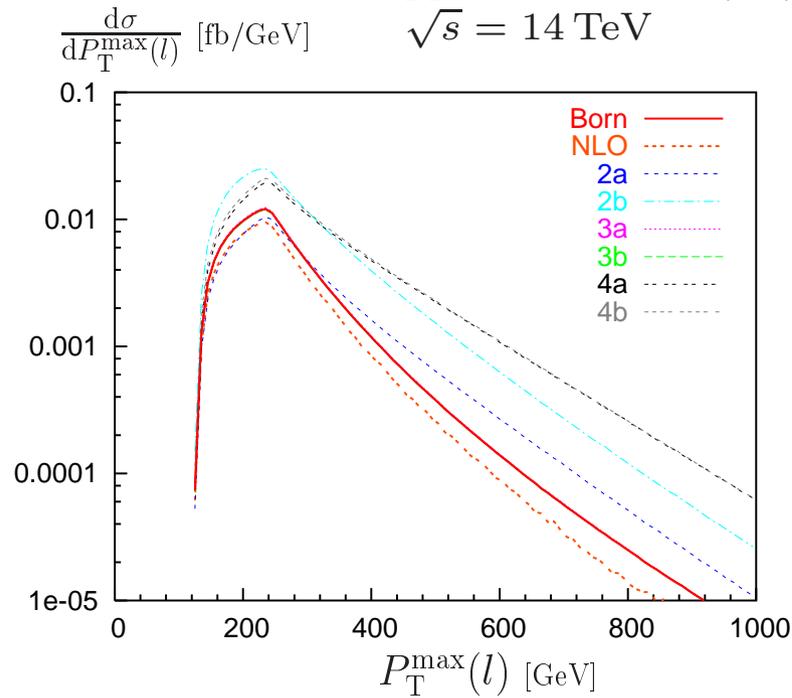


- EW corrections reach already 10–20% at scales $\sim 500\text{--}1000 \text{ GeV}$
- $\gamma\gamma$ contribution sizeable for large energies
- Special situation in $p_{T,e\mu}$:
 large positive corrections due to WW recoiling against hard γ radiation

EW corrections vs. anomalous TGCs in gauge-boson pair production

$$pp \rightarrow WZ \rightarrow e\nu_e\mu^+\mu^-$$

$$\sqrt{s} = 14 \text{ TeV}$$



Accomando, Kaiser '05

Scenario	Δg_1^Z	$\Delta \kappa_\gamma$	λ_γ
Born	0	0	0
2a/2b	± 0.02	0	0
3a/3b	0	± 0.04	0
4a/4b	0	0	± 0.02

$$\lambda_Z = \lambda_\gamma, \quad \Delta \kappa_Z = \Delta g_1^Z - \tan^2 \theta_W \Delta \kappa_\gamma$$

formfactor rescaling ($\Lambda = 1 \text{ TeV}$):

$$\Delta Y \rightarrow \frac{\Delta Y}{(1 + \hat{s}/\Lambda^2)^2}, \quad \Delta Y = \Delta g_1^Z, \Delta \kappa_\gamma, \lambda_\gamma$$

- Note:**
- EW corrections and anomalous couplings distort distributions
 - neglect of EW corrections can mimick anomalous couplings

Gauge-invariance issues in EW multi-boson production



Gauge invariance implies...

- **Slavnov–Taylor or Ward identities**
= algebraic relations of or between Greens functions
↔ guarantee cancellation of unitarity-violating terms,
crucial for proof of unitarity of S -matrix
- **Nielsen identities** (compensation of gauge-fixing artefacts)
↔ gauge-parameter independence of S -matrix
although Greens function (e.g. self-energies) are gauge dependent

Both statements hold order by order in standard perturbation theory !

Implications:

- **Resonances** require Dyson summation of resonant propagators
↔ perturbative orders mixed → **gauge invariance jeopardized !**
Gauge-invariance-violating terms $\propto \Gamma$ are formally of higher order,
but can be dramatically enhanced if unitarity cancellations disturbed
- **Anomalous couplings** potentially enhanced
if effective operator not gauge invariant

Important Ward identities for processes with EW gauge bosons:

Elmg. U(1) gauge invariance implies

$$k^\mu \gamma_\mu \text{ (wavy line)} \rightarrow \text{circle} \rightarrow \begin{matrix} F_1 \\ \vdots \\ F_n \end{matrix} = 0 \quad \text{for any on-shell fields } F_l$$

↪ Identity becomes crucial for collinear light fermions:

for fermion momenta $p_1 \sim c p_2$:

$$\begin{matrix} p_1 \\ \swarrow \\ \bullet \\ \nwarrow \\ p_2 \end{matrix} \begin{matrix} k = p_1 - p_2 \\ \rightarrow \\ \text{wavy line} \end{matrix} = \bar{u}_2(p_2) \gamma^\mu u_1(p_1) \propto k^\mu$$

A typical situation: quasi-real space-like photons

$$\begin{matrix} e \rightarrow \text{---} \bullet \text{---} e \\ \downarrow \\ \gamma \text{ (wavy line)} \\ \downarrow \\ k \\ \downarrow \\ \text{circle} \end{matrix} \sim \frac{1}{k^2} k^\mu T_\mu^\gamma \quad \text{for } k^2 \rightarrow \mathcal{O}(m_e^2) \ll E^2$$

Identity $k^\mu T_\mu^\gamma = 0$ needed to cancel $1/k^2$,

otherwise gauge-invariance-breaking terms enhanced by E^2/m_e^2 ($\sim 10^{10}$ for LEP2)

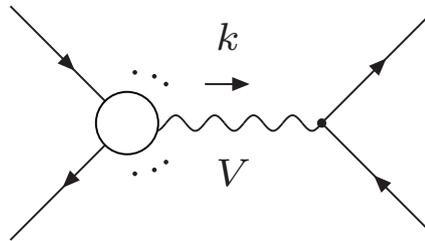
Electroweak SU(2) gauge invariance implies

$$\begin{aligned}
 k^\mu \text{---} Z_\mu \text{---} \text{---} \text{---} \begin{matrix} F_1 \\ \vdots \\ F_n \end{matrix} &= iM_Z \text{---} \chi \text{---} \text{---} \begin{matrix} F_1 \\ \vdots \\ F_n \end{matrix} \\
 k^\mu \text{---} W_\mu^\pm \text{---} \text{---} \text{---} \begin{matrix} F_1 \\ \vdots \\ F_n \end{matrix} &= \pm M_W \text{---} \phi^\pm \text{---} \text{---} \begin{matrix} F_1 \\ \vdots \\ F_n \end{matrix}
 \end{aligned}$$

F_l = on-shell fields
 χ, ϕ^\pm = would-be Goldstone fields

A typical situation: high-energetic quasi-real longitudinal vector bosons

↪ fermion current attached to $V(k)$ again $\propto k^\mu$



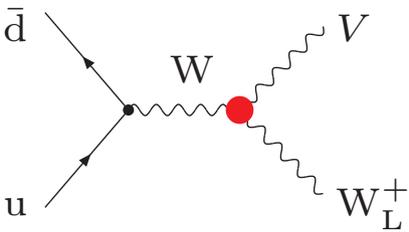
$$\sim \frac{1}{k^2 - M_V^2} k^\mu T_\mu^V \quad \text{for } k^0 \gg M_V$$

Identity $k^\mu T_\mu^V = c_V M_V T^S$ needed to cancel factor k^0 ,
 otherwise gauge-invariance/unitarity-breaking terms enhanced by k^0/M_V

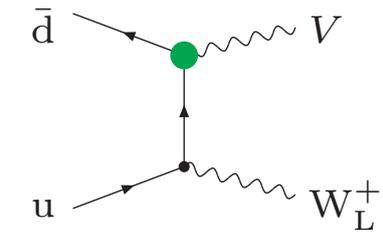
For on-shell V : $\varepsilon_{V_L}^\mu(k) = \frac{k^\mu}{M_V} + \mathcal{O}(M_V/k^0)$

Illustration of unitarity cancellations for WV production ($V = Z/\gamma$)

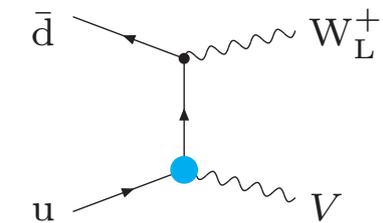
Leading behaviour of amplitudes with $\varepsilon_{W_L^+}^\mu(k) = \frac{k^\mu}{M_W} + \dots$ for $k^0 \gg M_W$:



$$\sim \frac{-ie^2 g_{VWW}}{2\sqrt{2}s_W M_W} [\bar{v}_{\bar{d}} \gamma_\mu \omega - u_u] \left\{ g_1^V \left[\varepsilon_V^{*\mu} - k^\mu \frac{\varepsilon_V^* \cdot k}{s} \right] + \kappa_V \left[\varepsilon_V^{*\mu} + k^\mu \frac{\varepsilon_V^* \cdot k}{s} \right] \right\}$$



$$\sim \frac{ie^2 g_{Vdd}^-}{\sqrt{2}s_W M_W} [\bar{v}_{\bar{d}} \not{\varepsilon}_V^* \omega - u_u], \quad g_{Zdd}^- = -\frac{s_W}{c_W} Q_d - \frac{1}{2s_W c_W}, \quad g_{\gamma dd}^- = -Q_d$$



$$\sim \frac{-ie^2 g_{Vuu}^-}{\sqrt{2}s_W M_W} [\bar{v}_{\bar{d}} \not{\varepsilon}_V^* \omega - u_u], \quad g_{Zuu}^- = -\frac{s_W}{c_W} Q_u + \frac{1}{2s_W c_W}, \quad g_{\gamma uu}^- = -Q_u$$

Cancellation (unitarity!) of sum demands:

$$g_{Vdd}^- - g_{Vuu}^- - \frac{g_{VWW}}{2} (g_1^V + \kappa_V) \stackrel{!}{=} 0, \quad g_1^V \stackrel{!}{=} \kappa_V$$

\hookrightarrow SM provides unique solution: $g_1^Z = \kappa_Z = g_1^\gamma = \kappa_\gamma = 1$

Note: no constraint on coupling λ_V , since effective operator gauge invariant !

Width schemes for LO calculations and gauge invariance

Naive propagator substitutions in full tree-level amplitudes:

$$\frac{1}{k^2 - m^2} \rightarrow \frac{1}{k^2 - m^2 + im\Gamma(k^2)} \quad \text{in all propagators}$$

- constant width $\Gamma(k^2) = \text{const.}$ \rightarrow U(1) respected, SU(2) “mildly” violated
- running width $\Gamma(k^2) \neq \text{const.}$ \rightarrow U(1) and SU(2) violated
 \hookrightarrow results can be totally wrong !

Fudge factor approaches:

Multiply full amplitudes without widths with

$$\text{factors } \frac{p^2 - m^2}{p^2 - m^2 + im\Gamma} \text{ for each potentially resonant propagator}$$

\hookrightarrow gauge invariant, but spurious factors of $\mathcal{O}(\Gamma/m)$

Complex-mass scheme: (see lecture 1)

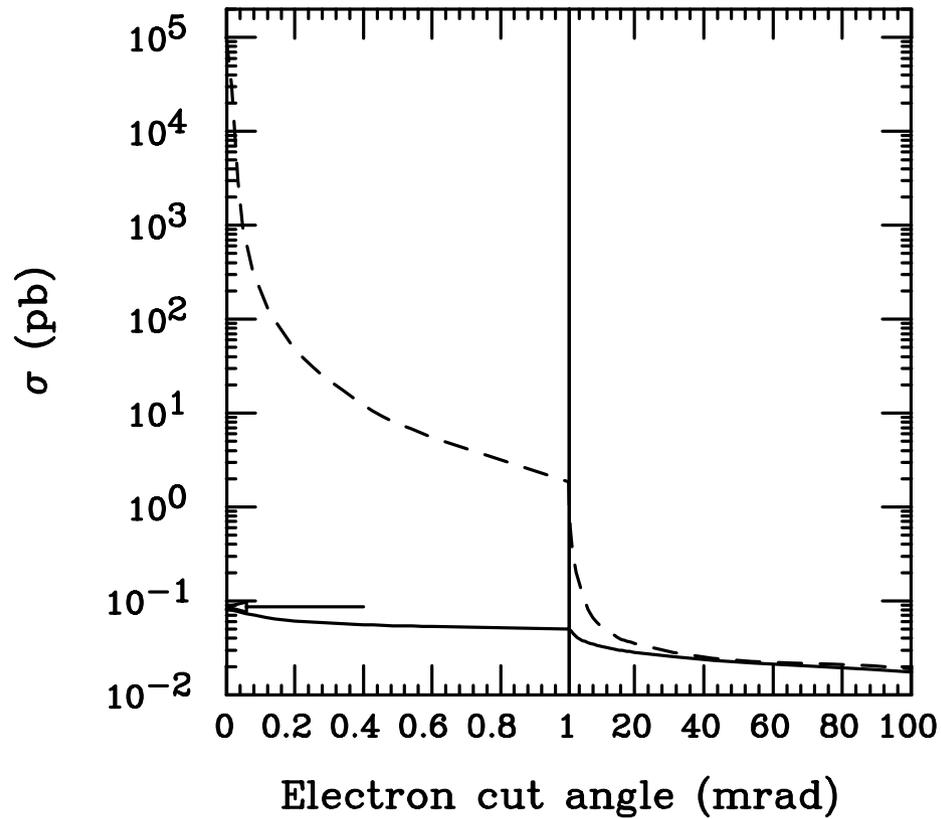
Consistent use of complex masses everywhere (including couplings)

$$\text{For W/Z bosons: } M_V^2 \rightarrow \mu_V^2 = M_V^2 - iM_V\Gamma_V, \quad V = W, Z$$

$$\text{complex weak mixing angle: } c_W^2 = 1 - s_W^2 = \frac{\mu_W^2}{\mu_Z^2}$$

\hookrightarrow gauge invariance fully respected

An example: $e^-e^+ \rightarrow e^- \bar{\nu}_e u \bar{d}$ result of Kurihara, Perret-Gallix, Shimizu '95



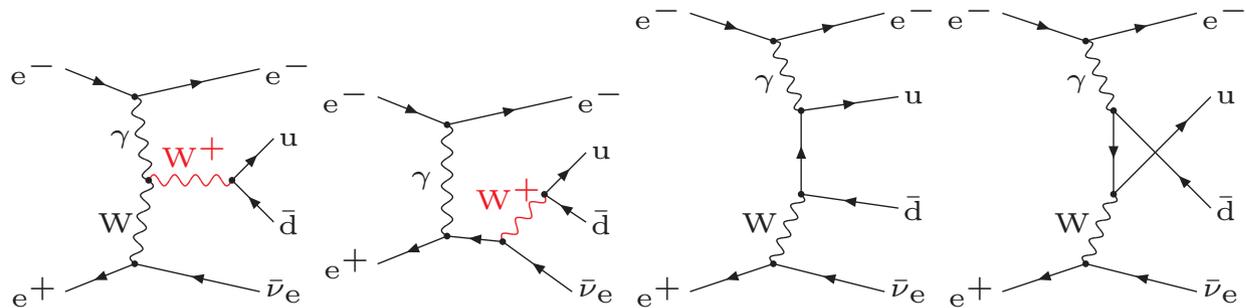
$$\sqrt{s} = 180 \text{ GeV}$$

solid: gauge-invariant
(fudge factor) scheme

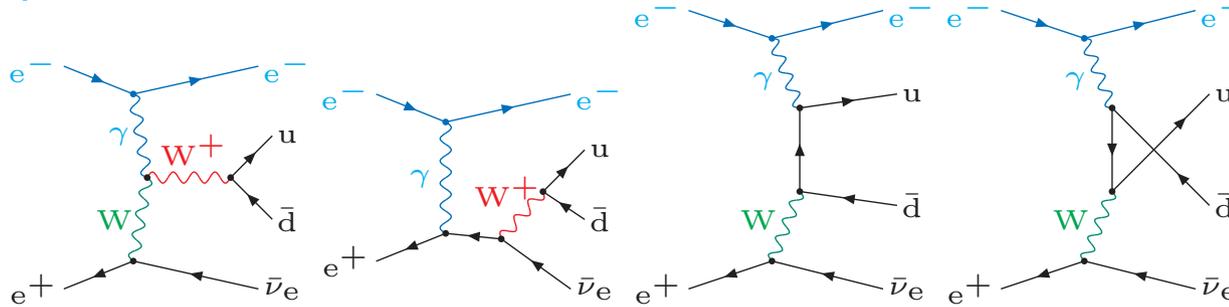
dashed: constant width
only in resonant propagator
↪ crude U(1) gauge-invariance
violation

Dominant diagrams:

nearly real photon !



Example continued:



Partial amplitude from above “photon diagrams”:

$$\mathcal{M}_\gamma = Q_e e \bar{u}_e(k_e) \gamma^\mu u_e(p_e) \frac{1}{k_\gamma^2} T_\mu^\gamma$$

Elmg. Ward identity:

$$0 \stackrel{!}{=} k_\gamma^\mu T_\mu^\gamma \propto (p_+^2 - p_-^2) Q_W P_W(p_+^2) P_W(p_-^2) + Q_e P_W(p_+^2) - (Q_d - Q_u) P_W(p_-^2)$$

With $Q_W = Q_e = Q_d - Q_u$ and $P_W(p^2) = [p^2 - M_W^2 + iM_W \Gamma_W(p^2)]^{-1}$
 one obtains: $\Gamma_W(p_+^2) \stackrel{!}{=} \Gamma_W(p_-^2)$

↪ Elmg. gauge invariance demands

common width on s - and t -channel propagators in “naive fixed width scheme”

Examples from e^+e^- physics: RACOONWW (Denner et al. '99-'01) and LUSIFER (S.D.,Roth '02)

- σ [fb] for $e^+e^- \rightarrow u\bar{d}\mu^-\bar{\nu}_\mu$

\sqrt{s}	189 GeV	500 GeV	2 TeV	10 TeV
constant width	703.5(3)	237.4(1)	13.99(2)	0.624(3)
running width	703.4(3)	238.9(1)	34.39(3)	498.8(1)
complex mass	703.1(3)	237.3(1)	13.98(2)	0.624(3)

- σ [fb] for $e^+e^- \rightarrow u\bar{d}\mu^-\bar{\nu}_\mu + \gamma$ (separation cuts for “visible” γ : $E_\gamma, \theta_{\gamma f} > \text{cut}$)

$\sqrt{s} =$	189 GeV	500 GeV	2 TeV	10 TeV
constant width	224.0(4)	83.4(3)	6.98(5)	0.457(6)
running width	224.6(4)	84.2(3)	19.2(1)	368(6)
complex mass	223.9(4)	83.3(3)	6.98(5)	0.460(6)

- σ [fb] for $e^+e^- \rightarrow \nu_e\bar{\nu}_e\mu^-\bar{\nu}_\mu u\bar{d}$ (phase-space cuts applied)

\sqrt{s}	500 GeV	800 GeV	2 TeV	10 TeV
constant width	1.633(1)	4.105(4)	11.74(2)	26.38(6)
running width	1.640(1)	4.132(4)	12.88(1)	12965(12)
complex mass	1.633(1)	4.104(3)	11.73(1)	26.39(6)

Gauge-invariant width schemes @ NLO

Problem much more complicated than at LO ! (would fill own lectures)

Complex-Mass Scheme (CMS) Denner, S.D., Roth, Wieders '05

- complex, but straightforward renormalization
- NLO everywhere in phase space
- loop integrals with complex masses

Pole Approximation (PA) (= leading term of pole expansion)

- corrections decomposed into two types
 - ◇ factorizable: corrections to on-shell production / decay
 - ◇ non-factorizable: soft photon/gluon exchange between production / decays
- NLO in neighbourhood of resonances
- PA involves less diagrams than CMS → higher multiplicities possible

Effective Field Theories Beneke et al. '03,'04; Hoang,Reisser '04

- involves pole expansions → NLO in neighbourhood of resonances
- formal elegance → e.g. combination with resummations

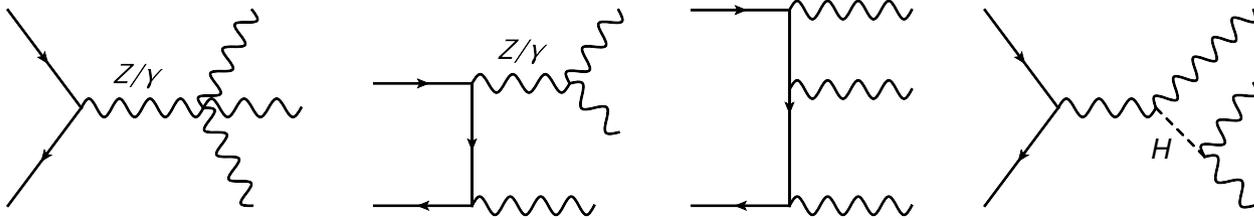
↪ **For details & examples see literature ...**

Outlook to electroweak tri-boson production



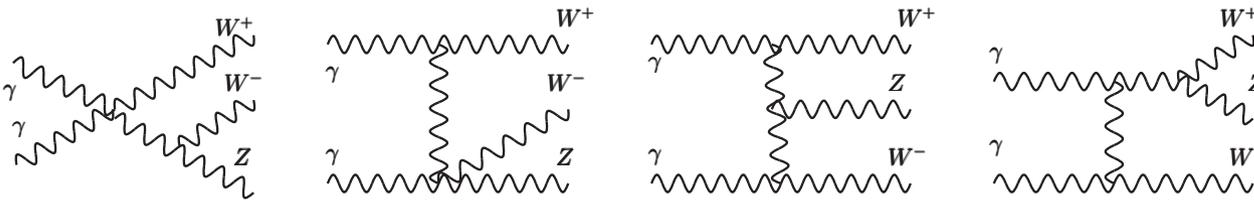
Electroweak tri-boson production – overview

Typical LO diagrams (example of WWZ production):



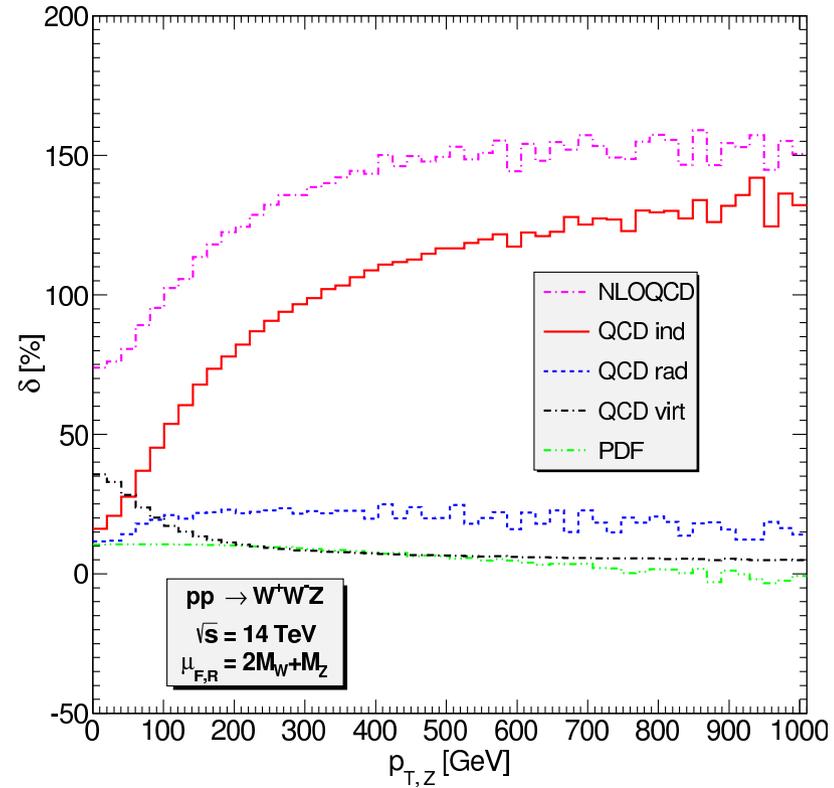
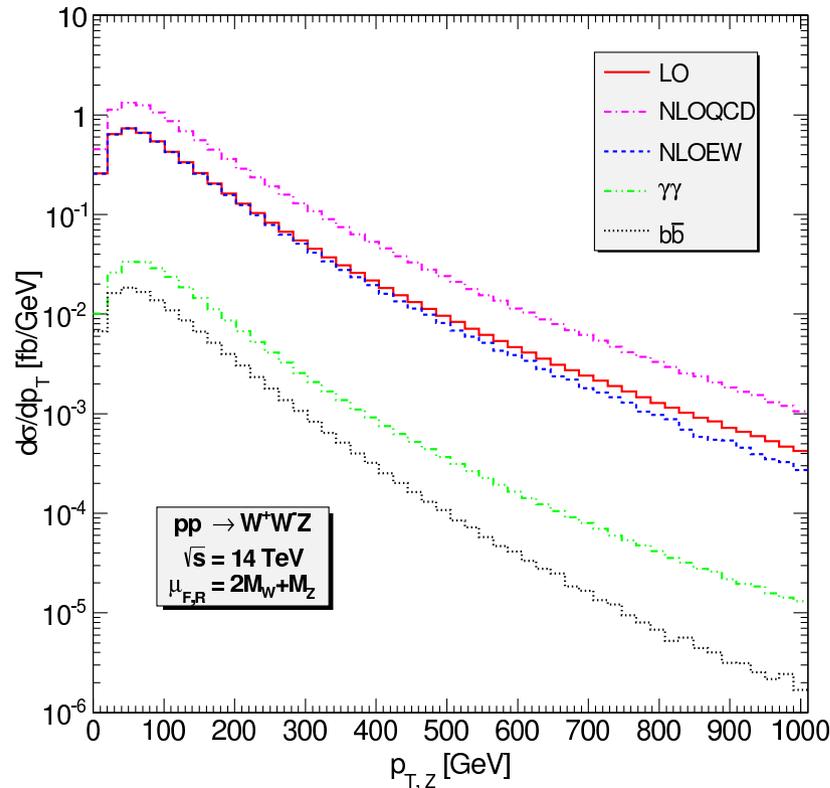
- **similarity/complementarity to vector-boson scattering** (crossed kinematics)
 - ◇ sensitivity to quartic gauge couplings
 - ◇ sensitivity to electroweak symmetry breaking
- background to WH/ZH production with $H \rightarrow VV^*$ (if accessible)

$\gamma\gamma$ channel for WWZ/ γ production:



QCD corrections to WWZ production

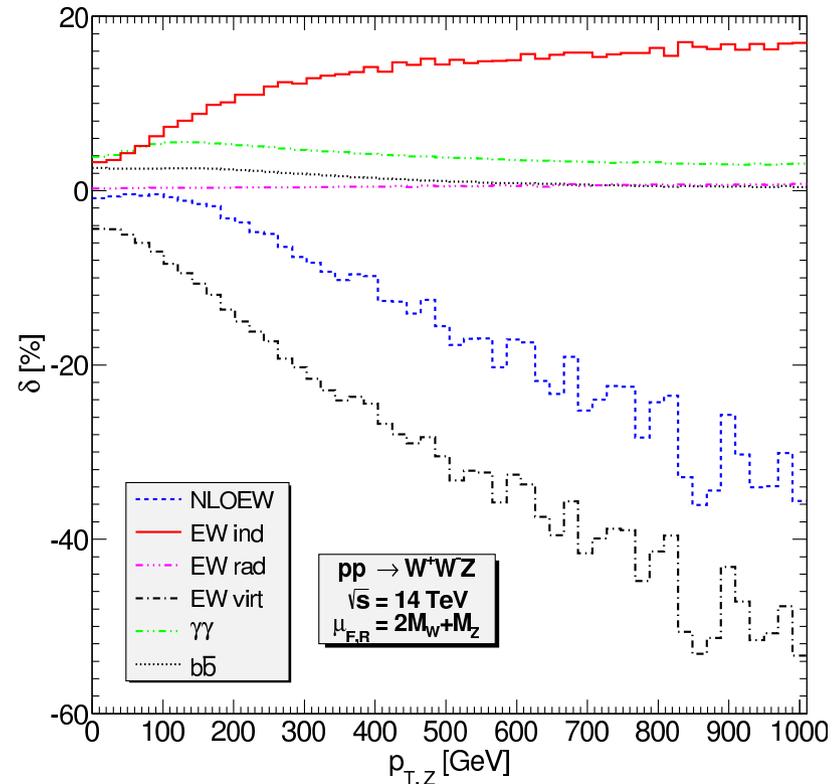
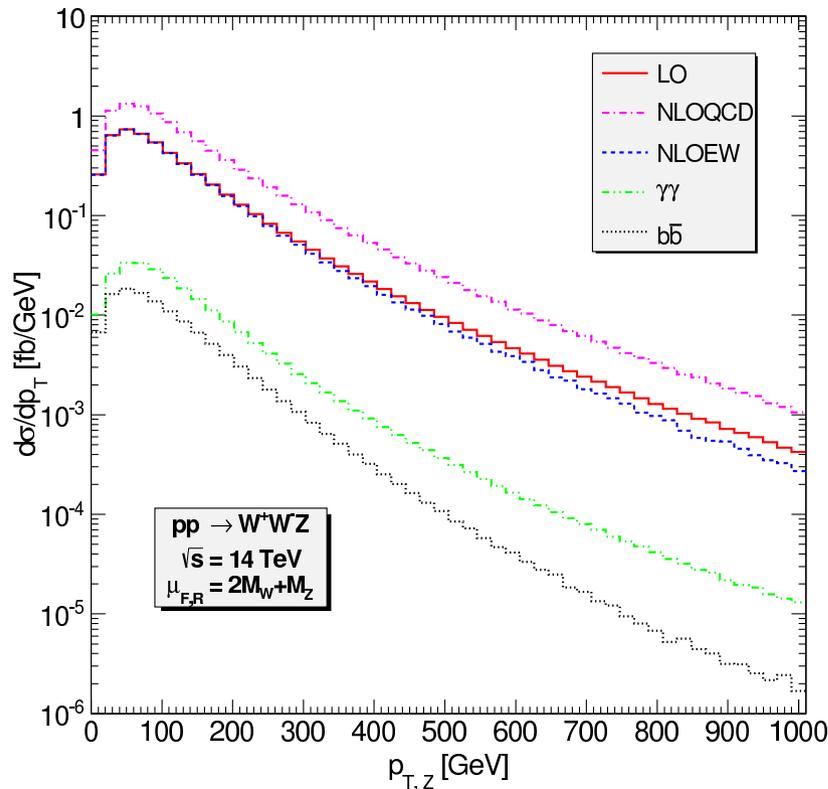
Nhung, Le, Weber '13



- inclusive cross section $\sim 200 \text{ fb}$ @ $\sqrt{s} = 14 \text{ TeV}$
- **QCD corrections $\sim 100\%$**
 - ◇ other final states WWW, WZZ, etc. known to NLO QCD as well
Lazopoulos, et al. '07; Hankele/Zepfenfeld '07; Binoth et al. '08; Nhung et al. '13
 - ◇ analyze possible jet vetoes
 - ◇ W/Z decays partially included in NWA

EW corrections to WWZ production

Nhung, Le, Weber '13



- sizeable EW corrections in TeV range (as expected from di-boson case)
- EW corrections only known for on-shell (stable) WWZ production
 - ↪ homework for theorists to ...
 - ◇ consider the other cases WWW, WZZ, etc. as well
 - ◇ include W/Z decays
 - ◇ combine NLO QCD (known) and EW corrections